

The Role of Problem Solving in Introductory Physics – Why, What, and How?



Ken Heller

**School of Physics and Astronomy
University of Minnesota**

25 year continuing project to improve undergraduate education with contributions by:

Many faculty and graduate students of U of M Physics Department

In collaboration with U of M Physics Education Research (PER) Group

Current PER group: Bijaya Aryal, Evan Frodermann, Ken Heller, Leon Hsu, Christy Krouse, Jia-Ling Lin, Eugene Park, Steve Pliam, Qing Xu, Jie Yang

Details at <http://groups.physics.umn.edu/physed/>



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and the University of Minnesota



Problem Solving in Introductory Physics

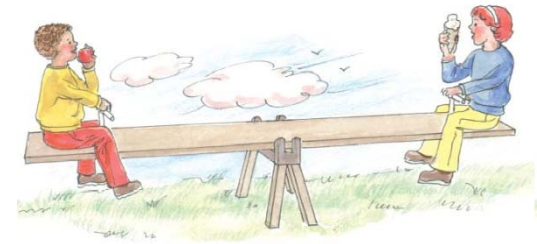
A Guide for Discussion

1. Designing Improvement
2. Why Problem Solving?
3. System Components

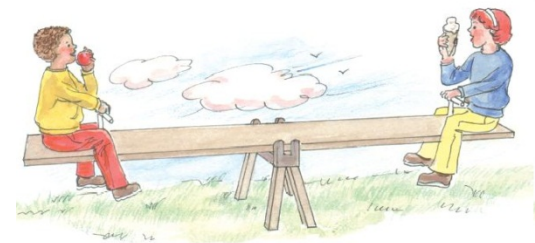
- Course (content & structure)
- Students (characteristics & difficulties)
- Instructors (beliefs & values)
- Customers (expectations & desires)

4. Some Data

generalities details



Reality Hindsight



What Students Show Us After Instruction



callcentertoday.com

**We are not happy.
Neither are our students.**

Solution

- Get better students
- Get better teachers
- **Do things differently**

**Students do not think
the same way we do**

**We are experts
They are novices**

Handwritten student work on lined paper showing a physics problem and solution. The problem involves a rock thrown from a height of 500m with an initial velocity of 71.4 m/s at an angle of 11 degrees. The student uses kinematic equations to find the time of flight and the final velocity.

Diagram: A rock is thrown from a height of 500m. The initial velocity is 71.4 m/s at an angle of 11 degrees. The horizontal distance is 100m. The final velocity is 76.4 m/s.

Equations used:

$$t = \frac{0}{A}$$

$$\theta = \tan^{-1} \frac{100}{500} = 11.3^\circ$$

$$V_f = V_0 + at$$

$$X_y = V_0 t + \frac{1}{2} at^2 = 500$$

$$X_y = at^2 \quad t = \frac{X}{V}$$

$$t^2 = \frac{500}{9.8 \text{ m/s}^2} = 51.0 \text{ s}$$

$$t = 7.14 \text{ sec.} \quad (7.14 \text{ sec.})$$

$$500^2 + 100^2 = \sqrt{260000} = 509.9 \text{ m}$$

$$X = X_0 + V_0 t + \frac{1}{2} at^2 \quad a = g = 9.8 \text{ m/s}^2$$

Diagram: A velocity vector diagram showing the final velocity $V_f = 76.4 \text{ m/s}$ at an angle of 11 degrees. The horizontal component is $V_{0x} = 71.4 \text{ m/s}$ and the vertical component is $V_{0y} = 13.9 \text{ m/s}$.

Equations used:

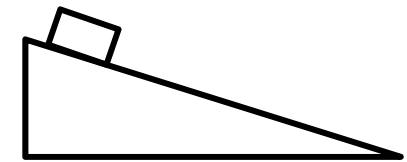
$$X - X_0 = V_0 t + \frac{1}{2} at^2$$

$$\frac{X - X_0}{t} = V_0 + \frac{1}{2} at$$

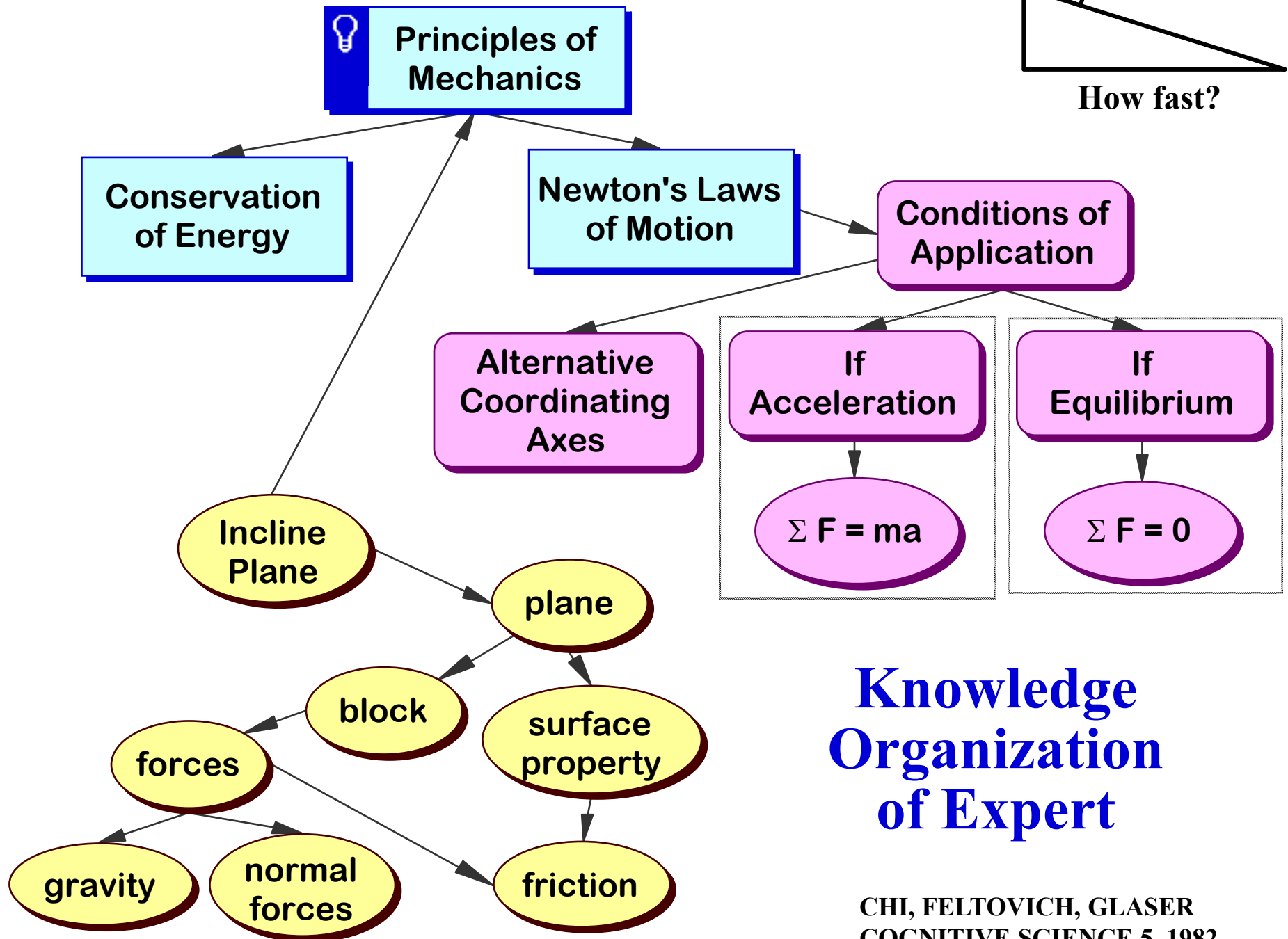
$$\frac{500 - 100}{7.14} = 71.4 + \frac{1}{2} (9.8) (7.14)$$

$$V_y = 76.4 \text{ m/s}$$

Final result: he would have to roll the rock at 13.9 m/s

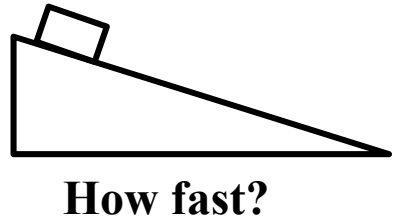


How fast?

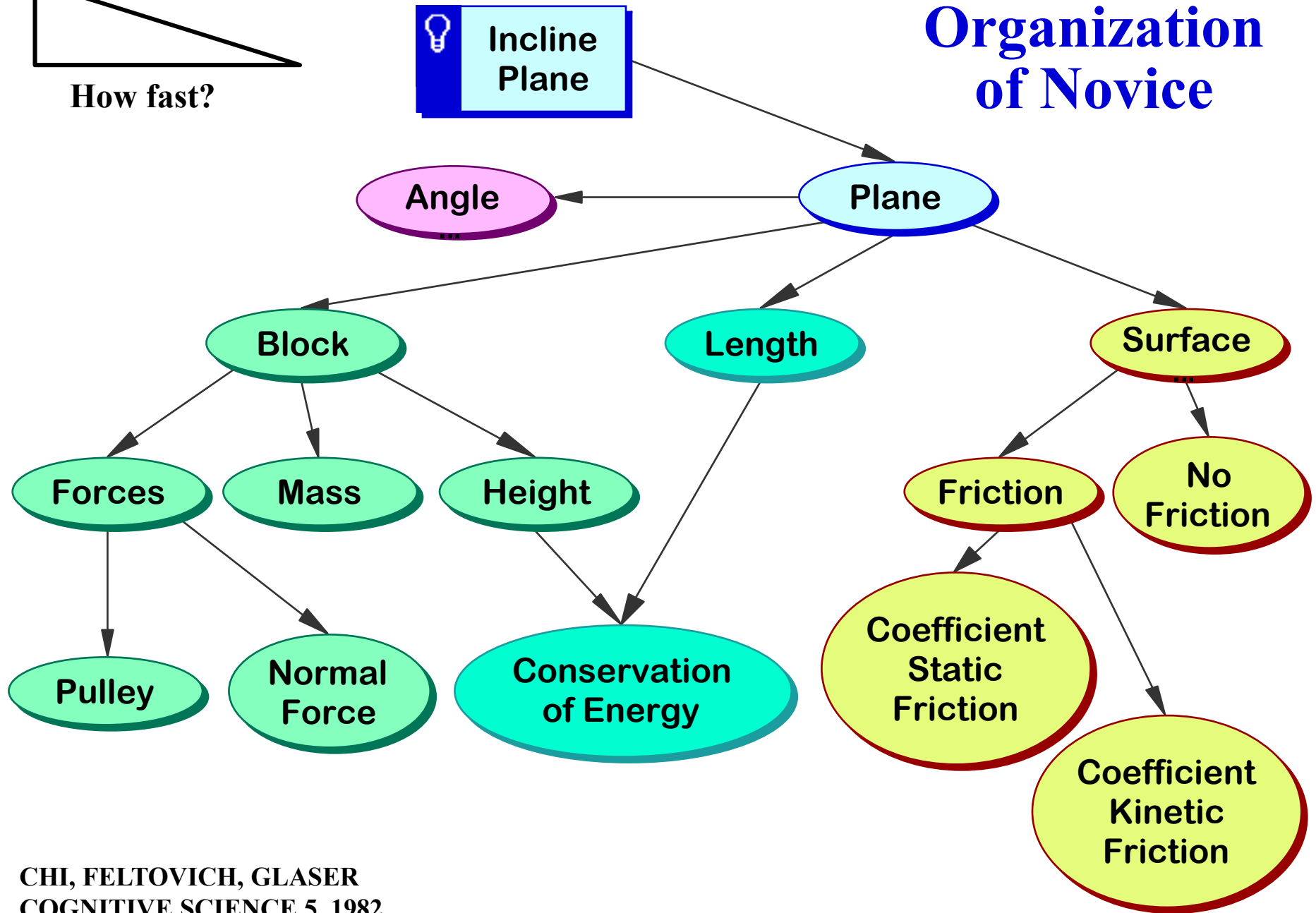


Knowledge Organization of Expert

CHI, FELTOVICH, GLASER
COGNITIVE SCIENCE 5, 1982



Knowledge Organization of Novice



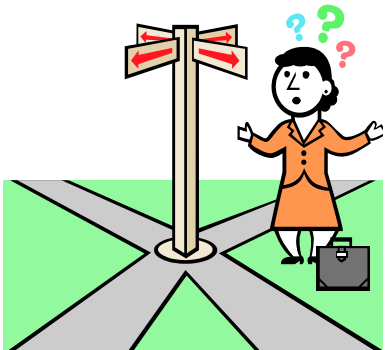
To Succeed You Need a Goal



University of Minnesota
Women's Hockey Team
NCAA Champions 2012 &
2013

There are several possible goals of an introductory physics course.

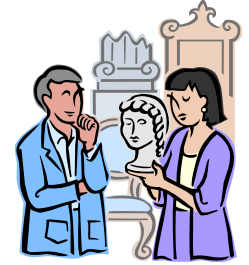
You cannot accomplish them all



- Qualitative ↔ Quantitative
- Concepts ↔ Problem Solving
- Breadth ↔ Depth
- Applied ↔ General
- Topic 1 ↔ Topic 2

**Decisions are
necessary**

Define the Goals



Who are the customers?

- The country.
- Faculty who require their students to take the class.
- The discipline of physics.
- The physics department.
- Students who take the class.

Design a questionnaire for faculty in other departments

Overall Goals

Free response

List with rating scale (1 to 5)

Content

Forced selection of chapters from a standard text.

Type of Labs

Free response

List with rating scale

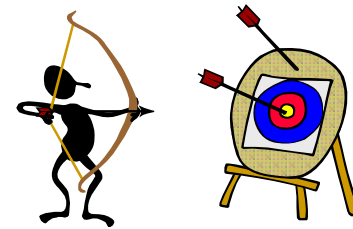
Type of Discussion Section

Free response

List with rating scale



Faculty Goals



Many different goals could be addressed through this course. Would you please rate each of the following possible goals in relation to its importance for your students on a scale of 1 to 5?

Algebra-based Course (24 different majors) 1987

- 4.7 Basic principles behind all physics
- 4.2 General qualitative problem solving skills
- 4.2 Overcome misconceptions about physical world
- 4.0 General quantitative problem solving skills
- 4.0 Apply physics topics covered to new situations

Problem Solving is Important



What Do Other Faculty Want? (5 pt scale)

Goals: Calculus-based Course (88% engineering majors) 1993

- 4.5 Basic principles behind all physics
- 4.5 General qualitative problem solving skills
- 4.4 General quantitative problem solving skills
- 4.2 Apply physics topics covered to new situations
- 4.2 Use with confidence



Goals: Algebra-based Course (24 different majors) 1987

- 4.7 Basic principles behind all physics
- 4.2 General qualitative problem solving skills
- 4.2 Overcome misconceptions about physical world
- 4.0 General quantitative problem solving skills
- 4.0 Apply physics topics covered to new situations

Goals: Biology Majors Course 2003

- 4.9 Basic principles behind all physics
- 4.4 General qualitative problem solving skills
- 4.3 Use biological examples of physical principles
- 4.2 Overcome misconceptions about physical world
- 4.1 General quantitative problem solving skills
- 4.0 Apply physics topics covered to real world situations
- 4.0 Know range of applicability of physics principles



Topics - Physics for Biology Majors

%T	%*
90	✓ 15
85	✓ 15
85	✓ 20
85	✓ 15
85	✓ 13
80	✓ 0
80	✓ 0
75	✓ 15
75	✓ 5
75	✓ 0
75	5
75	✓ 9
70	0
70	✓ 9
65	✓ 0
65	0
65	4
65	✓ 15
65	✓ 0
60	✓ 4
60	✓ 0
55	✓ 0
55	✓ 4

Potential energy and conservation of energy
Kinetic energy and work
Entropy and the second law of thermodynamics
Electric charge and force
Electric potential
Linear motion
Forces and Newton's Laws
Units, dimensions and vectors
Temperature and ideal gas
Electric field
Molecules and gases (e.g. probability distributions of velocity)
Mirrors and lenses
Momentum and collisions
Nuclear physics and radioactive decay
Two dimensional motion
Gravitation
Currents in materials (e.g. resistance, insulator, semiconductors)
Heat flow and the first law of thermodynamics
Magnetic forces and fields
Geometrical optics (e.g. reflection and refraction)
Diffraction
Oscillatory motion
Currents and DC circuits

Making Hard Choices



19/23 Chapters

Topics - Physics for Biology Majors

%T	%*
50	✓ 0
45	✓ 5
45	0
45	0
45	✓ 4
45	✓ 0
40	✓ 5
40	5
40	✓ 0
40	4
40	0
35	✓ 4
35	✓ 0
30	0
30	✓ 0
30	0
30	9
30	0
20	0
15	0
15	0
0	0

~~Rotations and torque~~

Applications of Newton's laws

Angular momentum

Gauss' law

Currents and magnetic fields (e.g. Ampere's law, ~~Biot-Savart law~~)

Interference

Fluid mechanics

Properties of solids (e.g. stress, strain, thermal expansion)

~~Capacitors and dielectrics~~

Maxwell's equations and electromagnetic waves

Relativity

Faraday's law

Superposition and interference of waves

Mechanical waves

Statics

Magnetism and matter (e.g. ferromagnetism, diamagnetism)

AC circuits

Atomic physics

Quantum physics

Magnetic Inductance

Particle physics

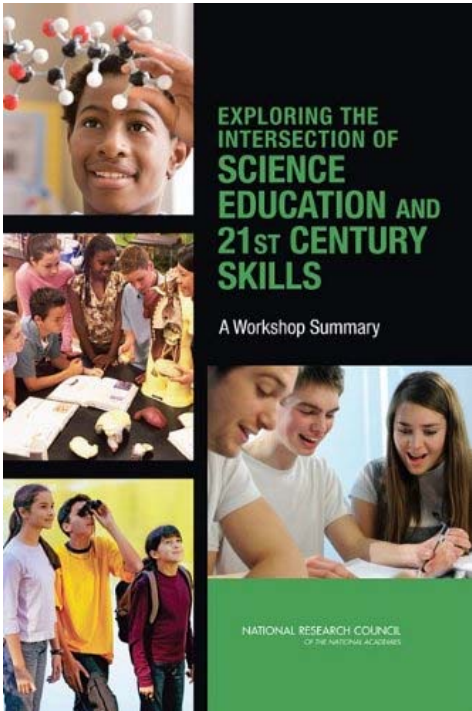
Other. Please specify.

9/21 Chapters

2 semesters (28 wks) = 28 Chapters

The Country Needs An Educated Workforce

21st Century Skills



**NATIONAL
RESEARCH
COUNCIL OF
THE NATIONAL
ACADEMIES
(2010)**

- **Adaptability:**
- **Complex communication/social skills:**
- **Self-management/self-development:**
- **Systems thinking:**
- **Non-routine problem solving:**
 - Diagnose the problem.
 - Link information.
 - Reflect on solution strategy.
 - Switch strategy if necessary.
 - Generate new solutions.
 - Integrate seemingly unrelated information.

Problem Solving Is Not Just For Science & Engineering

Science department of a large national law firm

Physics Department
Open House 11/11/10

What's a Physicist
Doing in a Law Firm?

Milena Higgins

Chief Scientist

U of Mn PhD 1996

Biophysics

ROBINS, KAPLAN, MILLER & CIRESI L.L.P.



Milena Higgins Ph.D.



Tim Streed, Ph.D.

Physics
&
Astronomy



Steve Giron, Ph.D.



Samuel LaRoque, Ph.D.



Kurt Torgersen, Ph.D.

Biochemistry, Molecular
Biology & Biophysics



Deborah Winters, Ph.D.



Alice Ribbens, Ph.D.

Material Science
& Engineering



Shelley Gilliss, Ph.D.



Lisa Dorn

Patent
Specialist

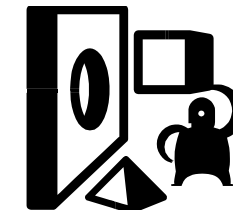


Janae Fabini

Chemistry

Q: How has Physics Helped You?

A: "It's all problem solving!"



University of Minnesota Strategic Planning - 2007

At the time of receiving a bachelor's degree, students will demonstrate the following qualities:



- 1. the ability to identify, define, and solve problems**
- 2. the ability to locate and evaluate information**
- 3. mastery of a body of knowledge and mode of inquiry**
- 4. an understanding of diverse philosophies and cultures in a global society**
- 5. the ability to communicate effectively**
- 6. an understanding of the role of creativity, innovation, discovery, and expression in the arts and humanities and in the natural and social sciences**
- 7. skills for effective citizenship and life-long learning.**

The syllabus for every course must say which of these 7 it addresses

Intro Physics Contributes to 1, 2, 3, 5, 7

What is a Problem?

A problem is a situation that you do not know how to resolve.

If you know **how** to do it, it is **not** a problem.



Solving a problem requires making **decisions** that connect what you know in new ways.



M. Martinez, Phi Delta Kappan, April, 1998

Solving Physics Problems

Expert: Solving a problem requires constructing a set of decisions that logically connect the situation to the goal using basic principles.



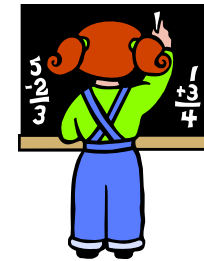
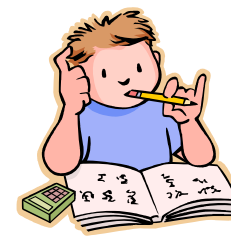
In Physics these decisions are typically about

- Visualizing a situation
- Specifying goals
- Making assumptions
- Identifying useful ideas
- Learning new ideas
- Connecting ideas using techniques such as diagrams, logic, mathematics
- Evaluating the process and its results

Novice: Solving a problem requires a following a recipe that connects the situation to the goal.



Novice Problem-solving Framework



STEP 1

What Kind of Problem is This?

Which pattern does it match?

STEP 2

What Equations Are Needed?

One should match this situation

STEP 3

Do Some Math

Plug in numbers

STEP 4

Do Some More Math

Manipulate equations to get an answer.

STEP 5

Is It Done?

Did I get an answer?

Problem-solving Framework Used by experts in all fields



G. Polya, 1945

Chi, M., Glaser, R., & Rees, E. (1982)

STEP 1

Recognize the Problem

What's going on and what do I want?

**Not a linear sequence.
Requires continuous
reflection and iteration.**

STEP 2

Describe the problem in terms of the field

What does this have to do with ?

STEP 3

Plan a solution

How do I get what I want?

“I was a student in first year physics you taught 20 years ago. Since those days I have made a good living as an RF integrated circuit design engineer. I am writing to let you know not a week goes by without a slew of technical problems to be solved, and the first thing that comes to mind is the "define the problem" which I recently reminded myself that it was you who instilled this ever so important step in problem solving. I would like to thank you because your influence has helped me excel and become a better engineer.”

STEP 4

Execute the plan

Let's get the answer.

STEP 5

Evaluate the solution

Can this be true?

email received June 22, 2012

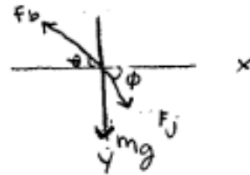
Problem Solving After Instruction

knowns

$$\theta = 80^\circ$$

$$V_m = 3.76 L = 3760 \text{ ml}$$

force diagram



Target: F_j = force of joint

Approach: Use Forces

$$\sum F_x = 0$$

$$\sum F_y = 0$$

Use Torque

$$\sum \tau = 0$$

$$V = \frac{m}{\rho}$$

$$\rho V_m = m$$

assume density of milk

is similar to water. $= 1 \text{ g/cm}^3 = 1 \text{ g/ml} = .001 \text{ kg/ml}$

$$\sum F_x = 0$$

$$F_{jx} - F_{bx} = 0$$

$$\sum F_y = 0$$

$$F_{by} - mg - F_{jy} = 0$$

$$\sum \tau = 0 \text{ (joint is pivot point)}$$

$$F_{by} (L/2) - mgL = 0$$

Trying to solve a problem by making logically connected decisions.

$$F_b \cos \theta = F_{bx}$$

$$F_b \sin \theta = F_{by}$$

$$F_{jy} = F_j \sin \phi$$

$$F_{jx} = F_j \cos \phi$$

$$F_j^2 = F_{jx}^2 + F_{jy}^2$$

equation

$$F_j^2 = F_{jx}^2 + F_{jy}^2$$

unknown F_{jx}, F_{jy}

$$F_{by} - mg - F_{jy} = 0 \quad 2 \quad F_{by}^3$$

$$F_{jx} - F_{bx} = 0 \quad 3 \quad F_{bx}^4$$

$$F_{by} (L/2) - mgL = 0 \quad 4$$

$$F_{bx} = F_b \cos \theta \quad 5 \quad F_b^5$$

$$F_{by} = F_b \sin \theta \quad 6$$

$$F_b = \frac{F_{by}}{\sin \theta}$$

$$\frac{F_{by}}{\sin \theta} \cos \theta = F_{bx}$$

$$6mg = F_{by}$$

$$F_{jx} = \frac{6mg \cos \theta}{\sin \theta}$$

$$F_{jy} = F_{by} - mg = 6mg - mg$$

$$F_j = \sqrt{\left(\frac{6mg \cos \theta}{\sin \theta}\right)^2 + (6mg - mg)^2}$$

43.3 N is the amount needed to lift an $\approx 1.3 \text{ kg}$ object straight up the ground this is reasonable

plug in ρV for m

$$F_j = \sqrt{\left(\frac{\rho V g}{\sin \theta} \cos \theta\right)^2 + (5 \rho V g)^2}$$

$$= \sqrt{\left(\frac{6(.001) 2760 g}{\sin 80} \cos 80\right)^2 + (5(.001)(3760 g))^2} =$$

$$\boxed{43.3 \text{ N}}$$

$$\text{units } \left(\frac{\text{kg}}{\text{ml}} \cdot \text{ml} \frac{\text{m}}{\text{s}^2}\right)^2 + \left(\frac{\text{kg}}{\text{ml}} \cdot \text{m} \cdot \frac{\text{m}}{\text{s}^2}\right)^2 = \sqrt{\frac{\text{kg}^2 \text{m}^2}{\text{s}^4}} = \text{kgm/s}^2 = \text{N} \quad \checkmark$$

Characterizing & Quantifying Expert-like Problem Solving

Almost Independent Dimensions

- **Useful Description**
 - organize information from the problem statement symbolically, visually, and/or in writing.
- **Physics Approach**
 - select appropriate physics concepts and principles
- **Specific Application of Physics**
 - apply physics approach to the specific conditions in problem
- **Mathematical Procedures**
 - follow appropriate & correct math rules/procedures
- **Logical Progression**
 - overall the solution progresses logically; it is coherent, focused toward a goal, and consistent (not necessarily linear)

J. Docktor (2009) based on previous work by:

J. Blue (1997); T. Foster (2000); T. Thaden-Koch (2005);

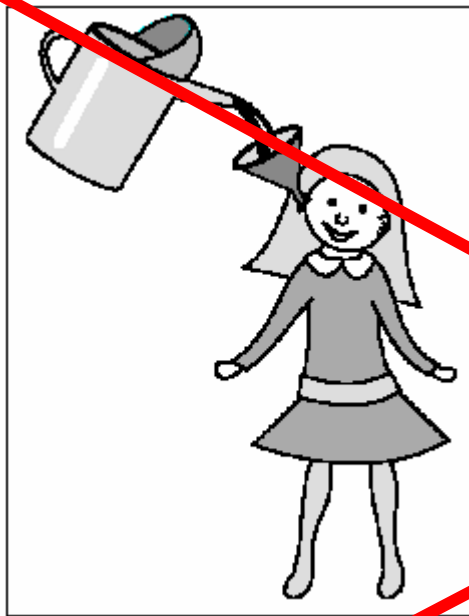
P. Heller, R. Keith, S. Anderson (1992)

The Teaching Process

The Clear Explanation Misconception



Common Source of Frustration of Faculty, TAs, Students, & Administrators



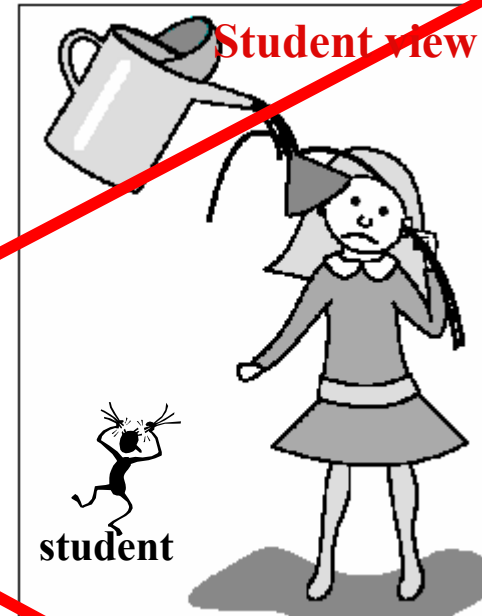
Instructor imparts knowledge to students by explaining things clearly.

Learning is much more complicated



Little knowledge is retained.

Student's Fault

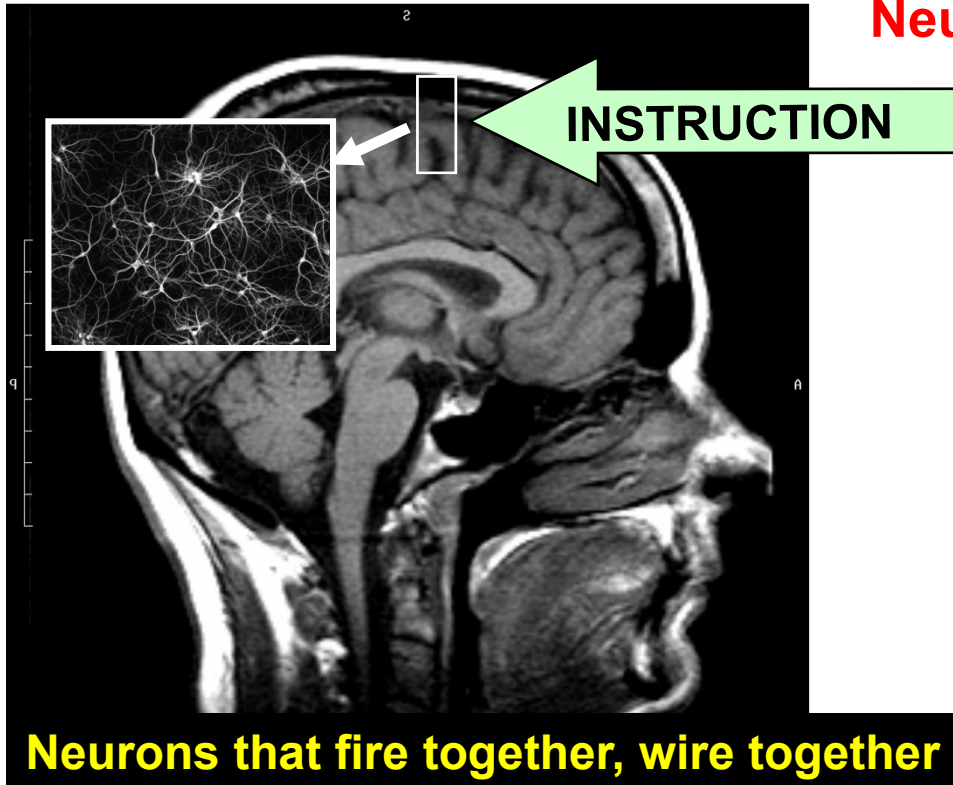


Impedance mismatch between student and instructor.

Instructor's Fault

Learning is a Biological Process

Neural Science Gives Constraints



Knowing is an individual's neural interconnections

Operationally, a student knows something if they can use it in novel (for them) situations and communicate that usage.

Learning is expanding and changing the network of neural connections

Teaching is putting the student in a situation that stimulates their neural activity to renovate the relevant network of neural connections.

Simplification of Hebbian theory:
Hebb, D (1949). *The organization of behavior*. New York: Wiley.

Brain MRI from Yale Medical School

Neuron image from Ecole Polytechnique Lausanne

Teaching requires forcing a student's **Mental Engagement**

Learning is Too Complex to Predetermine

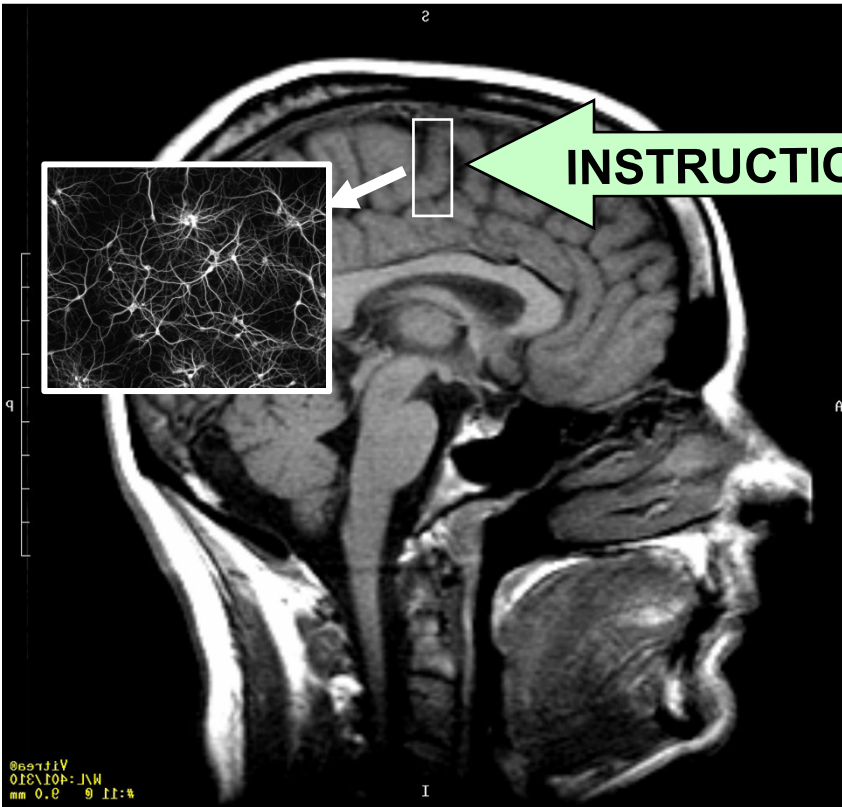
Apprenticeship Works



Cognitive Apprenticeship

Learning in the environment of expert practice

- Why it is important?
- How it is used?
- How is it related to what I already know?



Collins, Brown, & Newman
(1990)

Brain MRI from Yale Medical School
Neuron image from Ecole Polytechnique Lausanne



model



fade



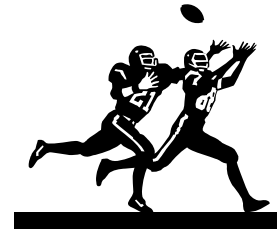
coach

Learning to Solve Problems Requires Practice

BUT

**“Practice does not make perfect.
Only perfect practice makes perfect.”**

Vince Lombardi (expert on coaching)



This is not perfect practice

A block of mass $m = 2.5$ kg starts from rest and slides down a frictionless ramp that makes an angle of $\theta = 25^\circ$ with respect to the horizontal floor. The block slides a distance d down the ramp to reach the bottom. At the bottom of the ramp, the speed of the block is measured to be $v = 12$ m/s.

- (a) Draw a diagram, labeling θ and d .
- (b) What is the acceleration of the block, in terms of g ?
- (c) What is the distance d , in meters?

**Robs students of practice making easy decisions
Does not reinforce motivation – reason to solve problems
Students do not practice linking to their existing information**

Original

A block of mass $m = 2.5$ kg starts from rest and slides down a frictionless ramp that makes an angle of $\theta = 25^\circ$ with respect to the horizontal floor. The block slides a distance d down the ramp to reach the bottom. At the bottom of the ramp, the speed of the block is measured to be $v = 12$ m/s.

- Draw a diagram, labeling θ and d .
- What is the acceleration of the block, in terms of g ?
- What is the distance d , in meters?

Better

A 2.5 kg block starts from the top and slides down a slippery ramp reaching 12 m/s at the bottom. How long is the ramp? The ramp is at 25° to the horizontal floor.

Practice making decisions

Practice making assumptions

Even Better

You are working with a design team to build a simple system to transport boxes from one part of a warehouse to another. In the design, boxes are placed at the top of the ramp so that they slide to their destination. A box slides easily because the ramp is covered with rollers. Your job is to calculate the maximum length of the ramp if the heaviest box is 25 kg and the ramp is at 5.0° to the horizontal. To be safe, no box should go faster than 3.0 m/s when it reaches the end of the ramp.

Requires student decisions.

Practice making assumptions.

Connects to student reality.

Has a motivation (why should I care?).

Context Rich Problem

The Dilemma

Start with complex problems so novice problem solving framework fails



Difficulty using an expert-like problem solving framework with challenging problems.

Why change?

Start with simple problems to learn expert-like problem solving framework.



Success using novice framework.

Why change?



Coaching is the necessary ingredient that allows students to use complex problems that require practicing an expert-like framework.

Cooperative Groups

Provide peer coaching and facilitates expert coaching

Allow success solving complex problems by practicing an expert-like problem solving framework from the beginning of the course.



Email 8/24/05

“Another good reason for cooperative group methods: this is how we solve all kinds of problems in the real world - the real academic world and the real business world. I wish they'd had this when I was in school. Keep up the great work.”

Vice President,
Handhelds Hewlett Packard

- ◆ Positive Interdependence
- ◆ Face-to-Face Interaction
- ◆ Individual Accountability
- ◆ Explicit Collaborative Skills
- ◆ Group Functioning Assessment

Johnson & Johnson, 1978

Cooperative Group Problem Solving is an Implementation of Cognitive Apprenticeship

There is no benefit in just having students work in groups.

Essential Elements

1. Demonstrate an Organized Framework for Problem Solving
2. Problems that Require Using an Organized Framework
3. Cooperative Groups to provide coaching to students while solving problems
4. Tests that Require Students to Solve Complex Problems Using an Organized Framework.
5. Appropriate Grading



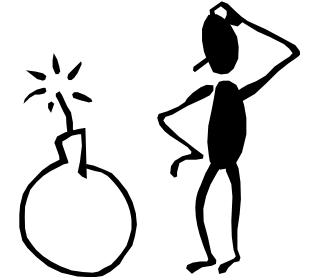
Peer coaching



Instructor coaching



Identify Critical Failure Points



1. Inappropriate Tasks

- Problems that have no obvious decisions.
- Problems that do not connect to student experience.
- Problems that one person can easily solve.

2. Inappropriate Grading

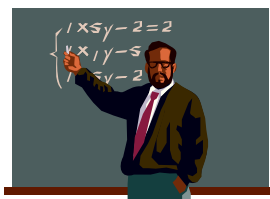
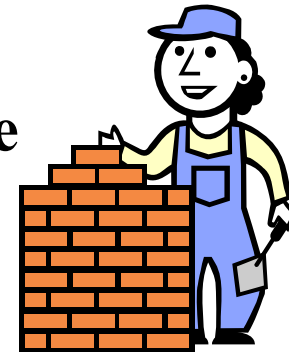
- Grading on the curve (penalize those who help others)
- No reward for both individual and group learning.
- Only the answer, not process, is rewarded.

3. Poor Structure and Management of Groups

- Students not required to search their own knowledge (use books & notes allowed)
- Students do not co-construct a solution, they work independently and compare results.

Building A Course Using Cognitive Apprenticeship

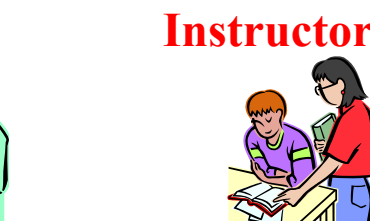
- **Demonstrate an Expert-like Problem Solving Framework**
 - **Emphasize making decisions using fundamental physics**
 - **Writing as working memory**
 - **Rule-based mathematics**
- **Practice & Test Using Problems that Require**
 - **An organized framework**
 - **Physics conceptual knowledge**
 - **Connection to existing knowledge**
- **Use Existing Course Structure**
 - **Lectures and web material MODELING**
 - **Discussion Sections COACHING**
 - **Labs COACHING**
- **Scaffolding to Support Problem Solving**



Modeling



Peer



Instructor

Coaching



Fading

Course Structure @ Minnesota

LECTURES

Three hours each week, sometimes with informal cooperative groups, **peer coaching**. **Model** constructing knowledge, **model** using the problem solving framework.

DISCUSSION SECTION

One hour each Thursday -- groups practice using problem-solving framework to solve context-rich problems. **Peer coaching, TA coaching**.

LABORATORY

Two hours each week -- **same** groups practice using framework to solve concrete experimental problems. **Same TA. Peer coaching, TA coaching**.

TESTS

Friday -- problem-solving quiz & conceptual questions (usually multiple choice) every three weeks. **Fading**

Scaffolding – computer reading tests, clickers, JITT, limit formula usage, sample quizzes, problem solving manual, context rich problems

Cooperative Group Problem Solving Propagates Slowly Through the Department

Introductory Physics

Algebra-based Course for Pre Professionals (24 different majors) 1987

Calculus-based Course for Engineering and Physical Science Students (88% engineering majors) 1993

Calculus based Course for Biology Majors (1/3 premeds) 2003

Upper Division Physics Major Courses 2002

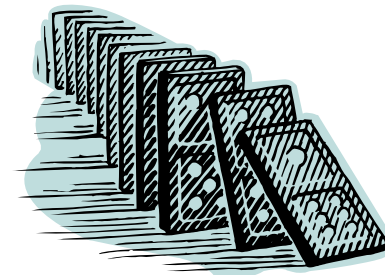
Analytic Mechanics

Electricity & Magnetism

Quantum Mechanics

Graduate Courses 2007

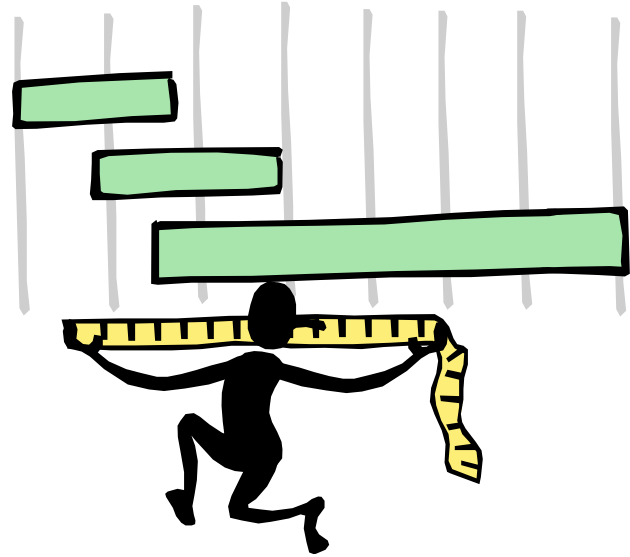
Quantum Mechanics



Budget constraints have prevented additional requested expansion into other courses

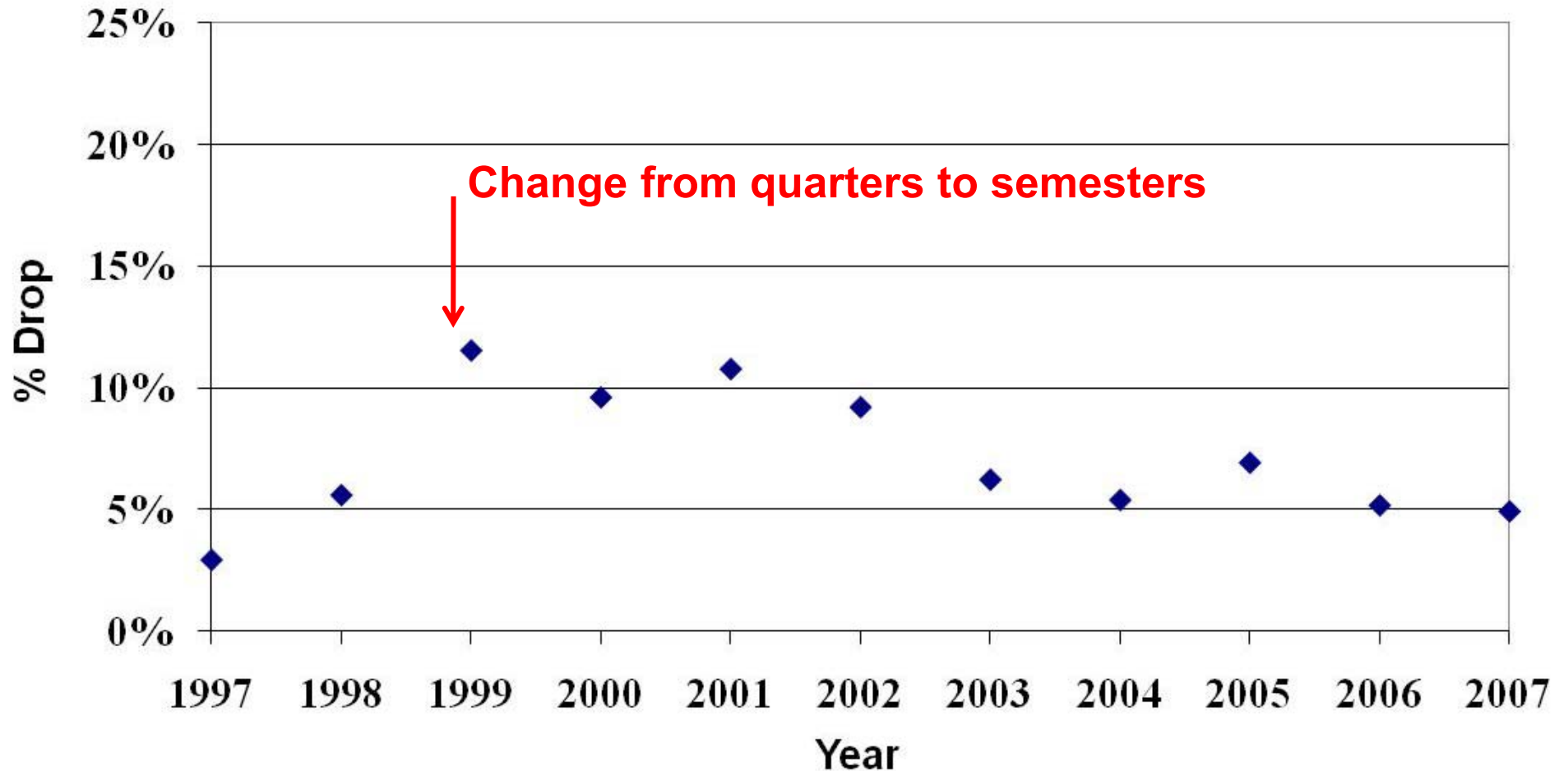
Assessment

- **Problem Solving Skill**
- **Drop out rate**
- **Failure rate**
- **National concept tests (FCI, BEMA)**
- **National attitude survey (CLASS)**
- **Math skills test**
- **What students value in the course**
- **Engineering student longitudinal study**
- **Faculty use**
- **Adoption by other institutions and other disciplines**



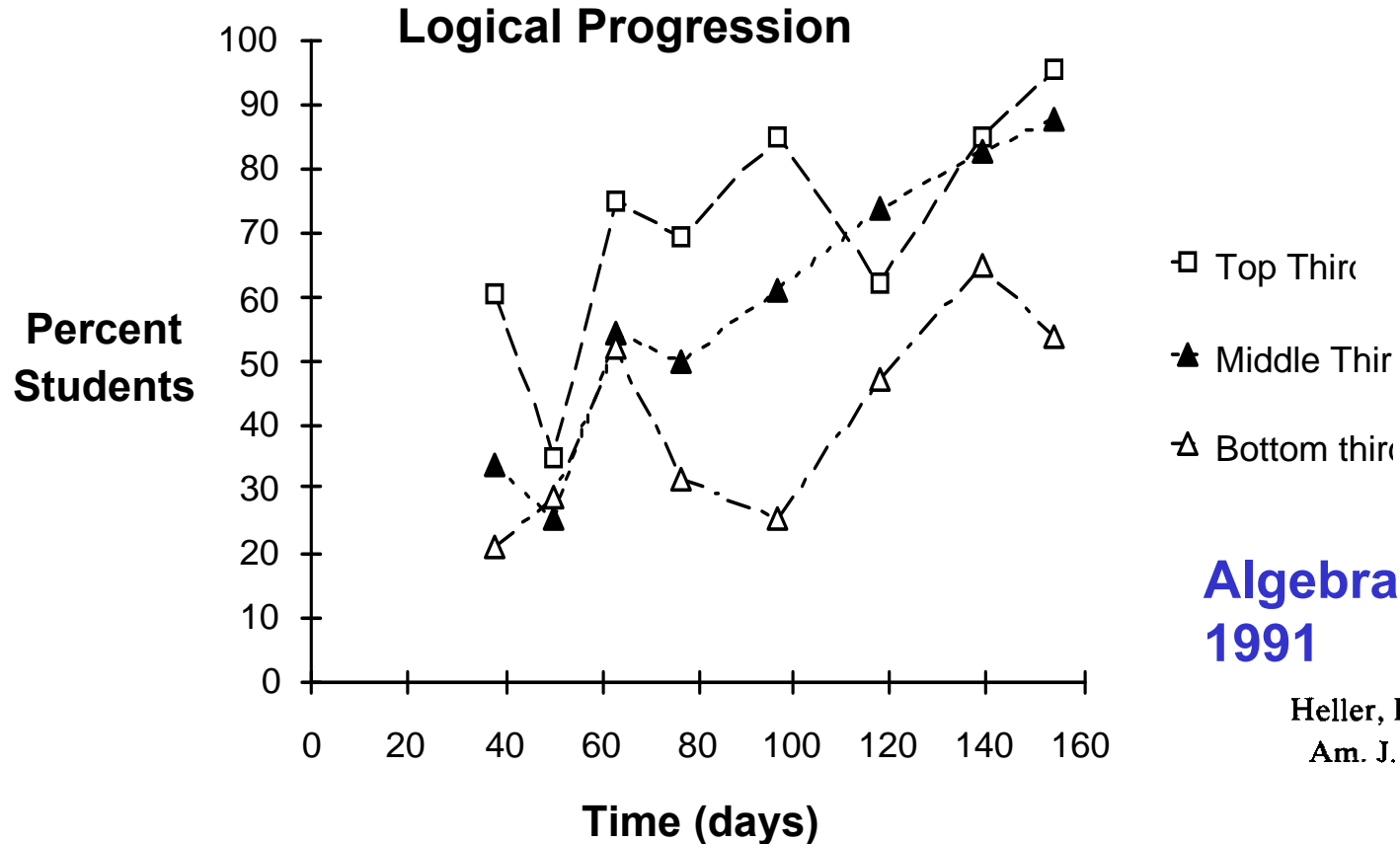
Retention after Implementation – Physics

Previous dropout + F/D rate was ~ 30%



Dropout rate ~ 6%, F/D rate ~ 3% in all classes

Improvement in Problem Solving



Algebra based physics 1991

Heller, Keith, and Anderson
Am. J. Phys., Vol. 60, No. 7, July 1992

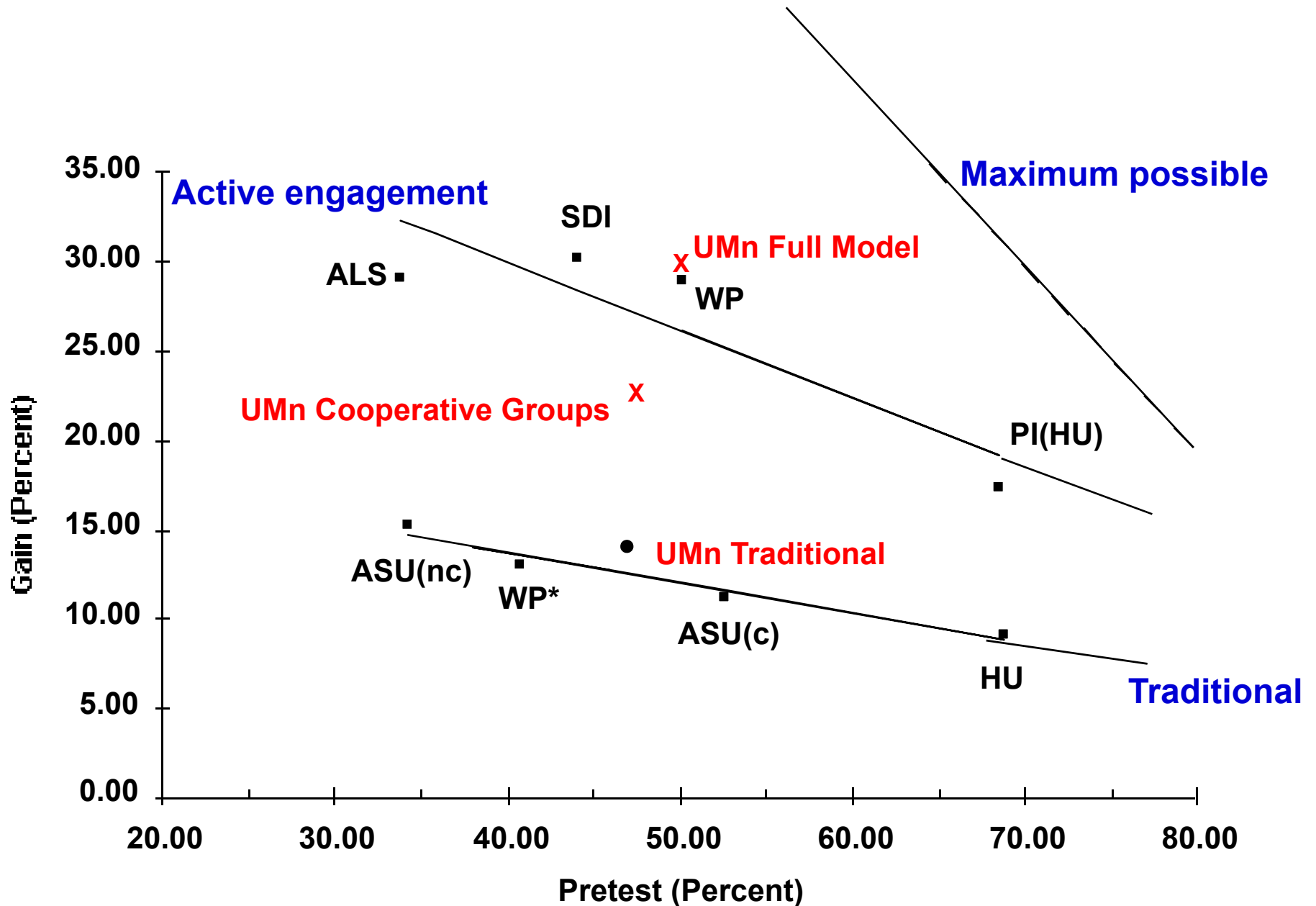
General Approach - does the student understand the physics

Specific Application of the Physics - starting from the physics they used, how did the student apply this knowledge?

Logical Progression - is the solution logically presented?

Appropriate Mathematics - is the math correct and useful?

Gain on Force Concept Inventory (Hake plot)



The End

**Please visit our website
for more information:**



<http://groups.physics.umn.edu/physed/>

The best is the enemy of the good.

"le mieux est l'ennemi du bien"

Voltaire