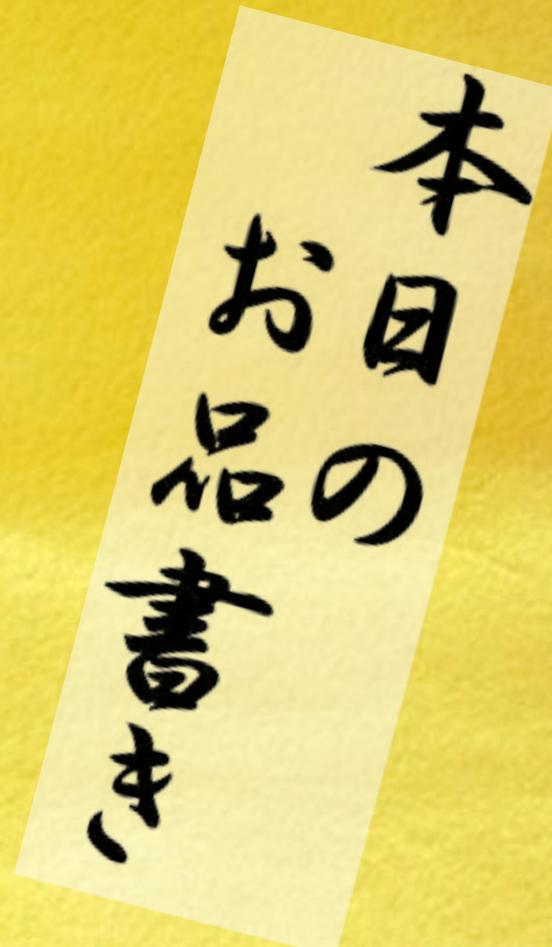


# Study of the suppressed decay $B^- \rightarrow D^- K^-$ and $B^- \rightarrow D^{(*)}_{CP} K^-$ decays at Belle

Naoki Kikuchi  
(Tohoku Univ)  
on behalf of Belle collaboration

# Today's menu

1. CKM model
2.  $\phi_3$  measurement
3. GLW method  
&  $B^- \rightarrow D^{(*)}_{CP} K^-$  result
4. ADS method  
&  $B^- \rightarrow D_{ADS} K^-$  result
5. Summary



# 1. CKM model

## Weak interaction

$$L = -\frac{g}{\sqrt{2}} \overline{U}_L \gamma^\mu V_{CKM} D_L W_\mu$$

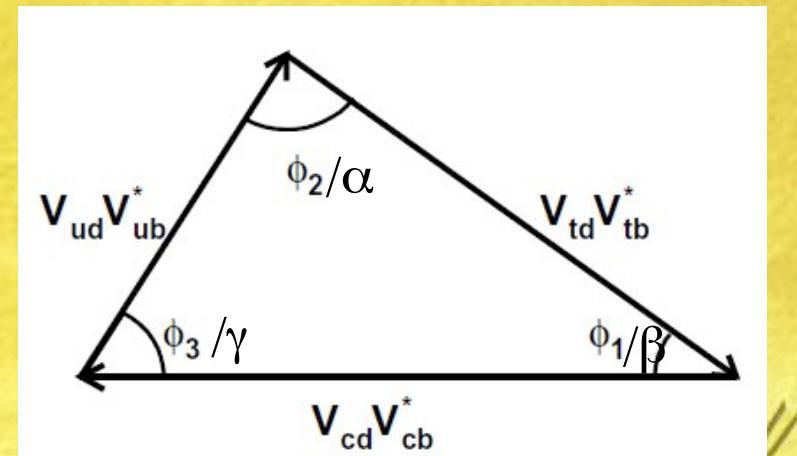
$$V_{CKM} \equiv \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Complex component

## Unitarity condition

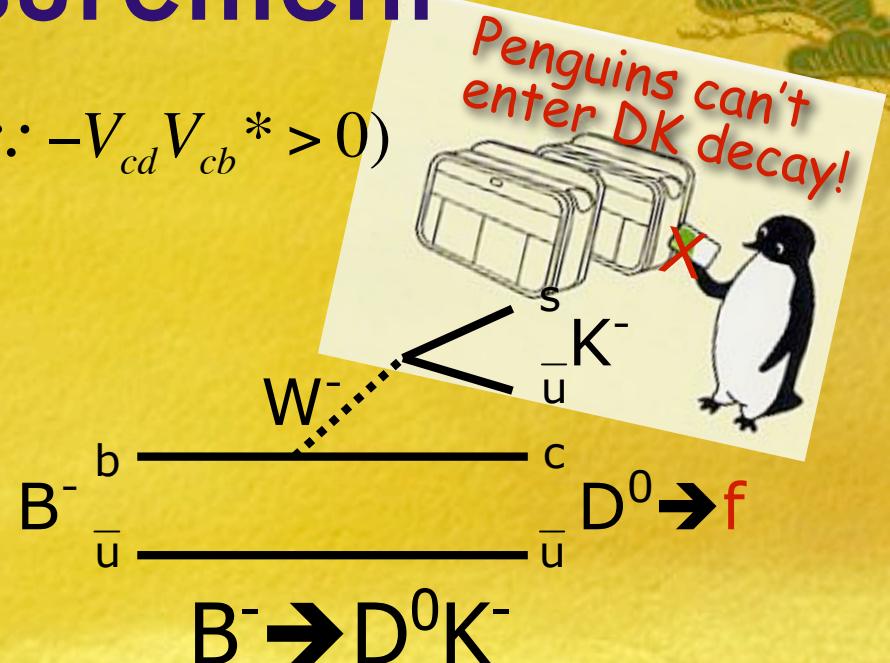
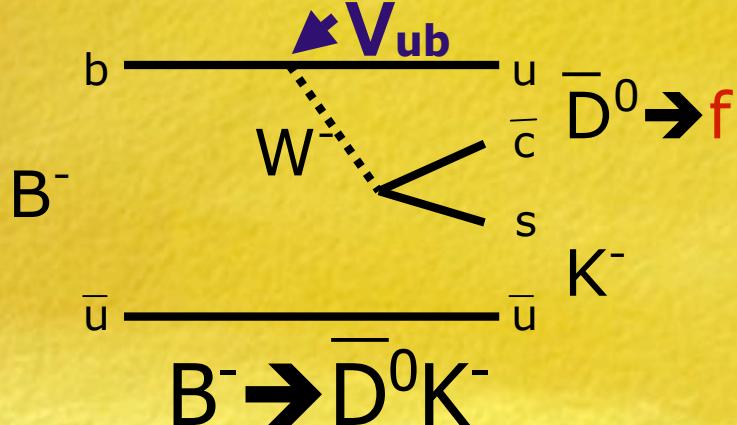
$$V_{CKM}^\dagger V_{CKM} = 1$$

$$\Rightarrow V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$



## 2. $\phi_3$ measurement

$$\phi_3 \equiv \arg\left(\frac{V_{ud} V_{ub}^*}{-V_{cd} V_{cb}^*}\right) \approx \arg(V_{ub}^*) \quad (\because -V_{cd} V_{cb}^* > 0)$$



- $D^0$  and  $\bar{D}^0$  decay into common final state,  $f$ .  
→ Determine  $\phi_3$  through interference term.
- $r_B$  determines the size of interference by  $\phi_3$ .
- Choice of final state
  - $f = [K_S \pi^+ \pi^-]$  : Dalitz analysis → P.Krokovny's talk
  - $f = D_+ [K^+ K^-, \pi^+ \pi^-], D_- [K_S \pi^0, K_S \omega, K_S \phi \dots]$  : GLW method
  - $f = D_{ADS} [K^+ \pi^-]$  / suppressed decay: ADS method

$$r_B \equiv \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right|$$

# 3. GLW method

M.Gronau and D. London, PLB **253**, 483 (1991)  
 M. Gronau and D. Wyler, PLB **265**, 172 (1991)

- Direct CPV

$$A_{\pm} = \frac{\Gamma(D_{\pm}K^-) - \Gamma(D_{\pm}K^+)}{\Gamma(D_{\pm}K^-) + \Gamma(D_{\pm}K^+)} = \frac{\pm 2r_B \sin \phi_3 \sin \delta}{R_{\pm}}$$

$$D_{\pm} \equiv \frac{D^0 \pm \bar{D}^0}{\sqrt{2}}$$

- Decay rate average

$$R_{\pm} = 2 \frac{\Gamma(D_{\pm}K^-) + \Gamma(D_{\pm}K^+)}{\Gamma(D^0K^-) + \Gamma(\bar{D}^0K^+)} = 1 + r_B^2 \pm 2r_B \cos \phi_3 \cos \delta$$

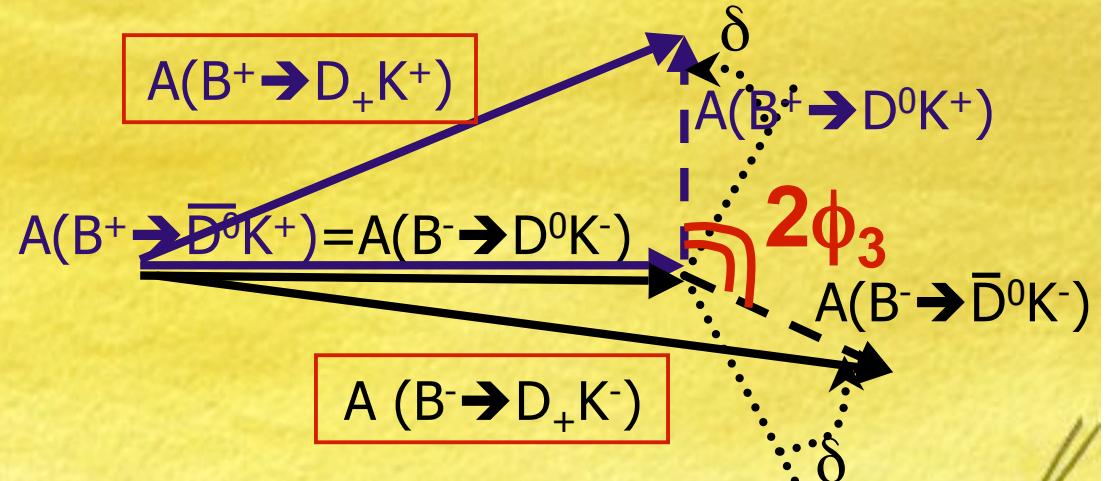
- D decay mode

- CP=+ mode  
◎  $K^+K^-$ ,  $\pi^+\pi^-$
- CP=- mode  
◎  $K_S\pi^0$ ,  $K_S\omega$ ,  $K_S\phi$

- Features

- Model independent
- High statistics
- Low sensitivity for  $r_B$

3 unknowns  $r_B, \delta, \phi_3$



# 3.1. Analysis procedure

## ● 2 independent kinematic variables

- $\Delta E$  : Energy difference

$$\Delta E \equiv E_D^* + E_K^* - E_{beam}^*$$

- $M_{bc}$  : Beam energy constrained mass

$$M_{bc} \equiv \sqrt{E_{beam}^{*2} - (\vec{p}_D^* + \vec{p}_K^*)^2}$$

Variables with \* are evaluated in CM system

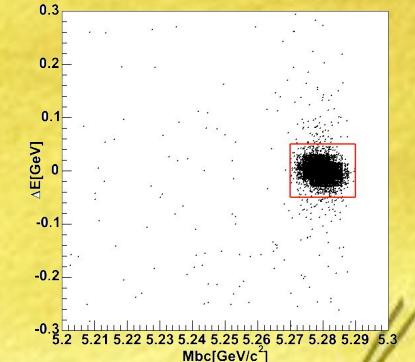
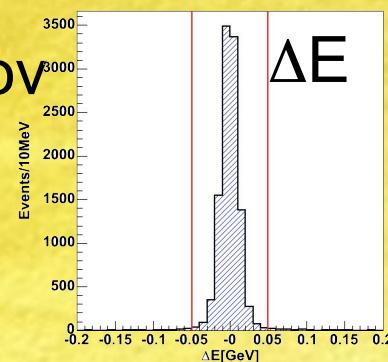
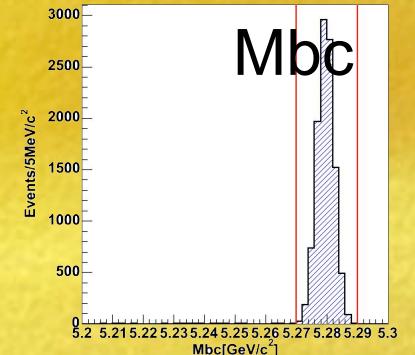
## ● D reconstruction

- $|M_{rec} - M_D| < 2.5\sigma$

- PID  $\leftarrow dE/dx + \text{TOF} + \text{Cherenkov}$

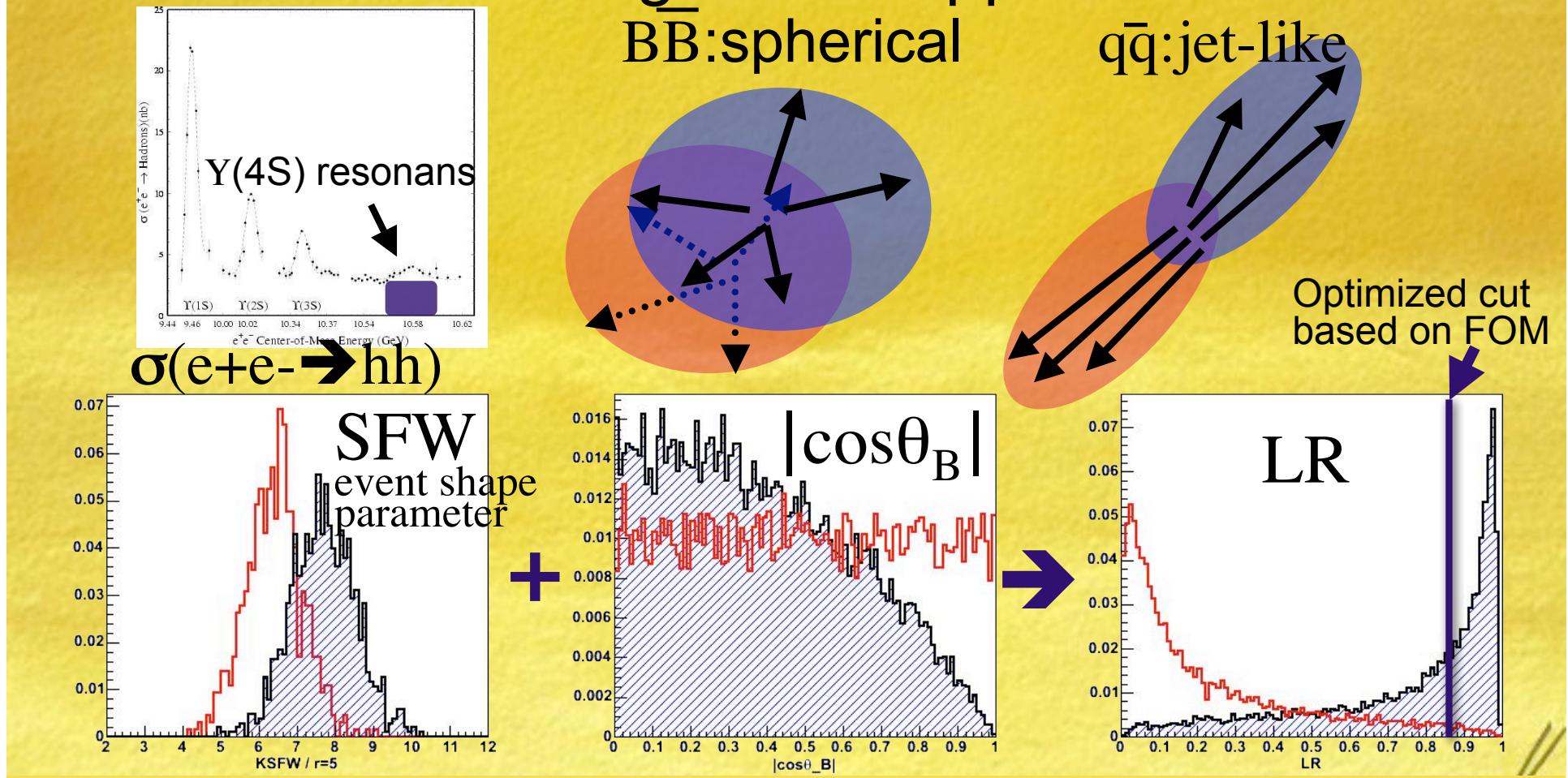
For K,  $LR(K/\pi) > 0.4$

For  $\pi$ ,  $LR(K/\pi) < 0.7$



# 3.1. Analysis procedure (cont'd)

## Continuum background suppression



Study of the suppressed decays  $B^- \rightarrow D^- K^-$  and  $B^- \rightarrow D_{CP}^- K^-$  decays at Belle

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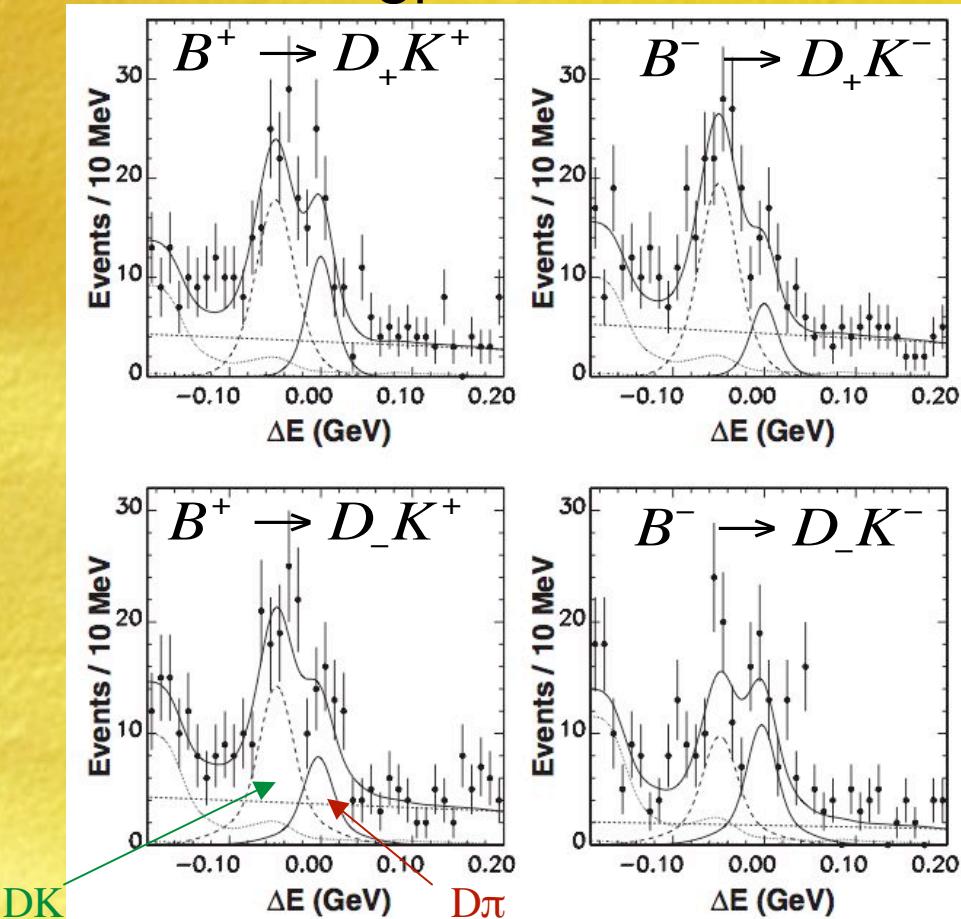
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## 3.2. Result on $D_{CP}K$

$\bullet B^- \rightarrow D_{CP}K^-$  w/Belle 274M BB

PRD 73, 051106 (2006)



Study of the suppressed decays  $B^- \rightarrow DK^-$  and  $B^- \rightarrow D_{CP}K^-$  decays at Belle

Naoki KIKUCHI

DPF/JPS 2006

$$\begin{aligned}
 A_+ &= 0.06 \pm 0.14 \pm 0.05 \\
 A_- &= -0.12 \pm 0.14 \pm 0.05 \\
 R_+ &= 1.13 \pm 0.16 \pm 0.05 \\
 R_- &= 1.17 \pm 0.14 \pm 0.05
 \end{aligned}$$

Yield:

$$\begin{aligned}
 D_+ K &: 143.3 \pm 21.9 \quad (12.4\sigma) \\
 D_- K &: 149.5 \pm 19.0 \quad (9.2\sigma)
 \end{aligned}$$

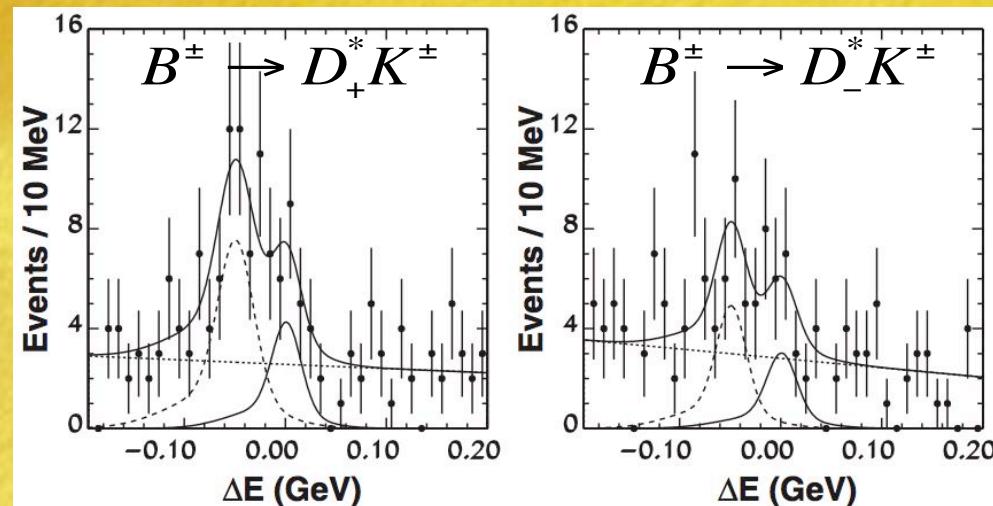
Signals are established!  
Significant deviations of  
 $A \pm \sim 0, R \pm \sim 1$  are not seen.



## 3.2. Result on $D^*_{CP}K$

•  $B^- \rightarrow D^*_{CP}K^-$  w/Belle 274M BB  
Using  $D^* \rightarrow D\pi^0$  mode

PRD 73, 051106 (2006)



$$\begin{aligned} A_+ &= -0.2 \pm 0.22 \pm 0.04 \\ A_- &= 0.13 \pm 0.3 \pm 0.08 \\ R_+ &= 1.41 \pm 0.25 \pm 0.06 \\ R_- &= 1.15 \pm 0.31 \pm 0.12 \end{aligned}$$

Yield:

$$\begin{aligned} D^*_+ K &: 43.9 \pm 10.2 \text{ (5.2σ)} \\ D^*_- K &: 32.7 \pm 10.0 \text{ (3.3σ)} \end{aligned}$$

Signals are established!  
Significant deviations of  
 $A \pm \sim 0, R \pm \sim 1$  are not seen.

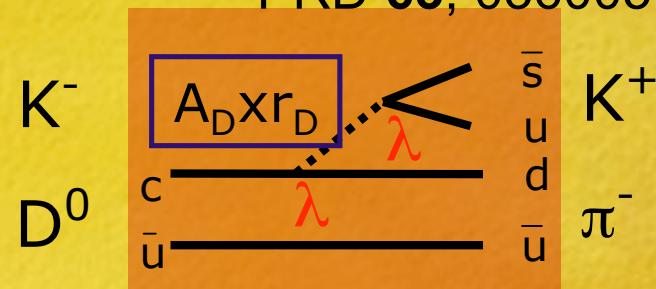
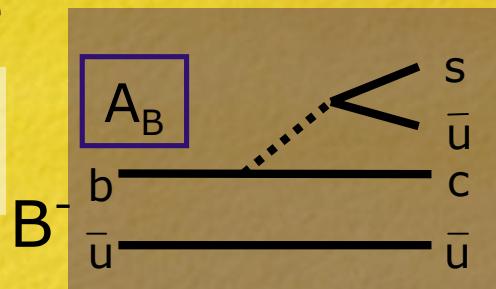
# 4. ADS method

D. Atwood, I. Dunietz and A. Soni, PRL **78**, 3357 (1997)

PRD **63**, 036005 (2001)

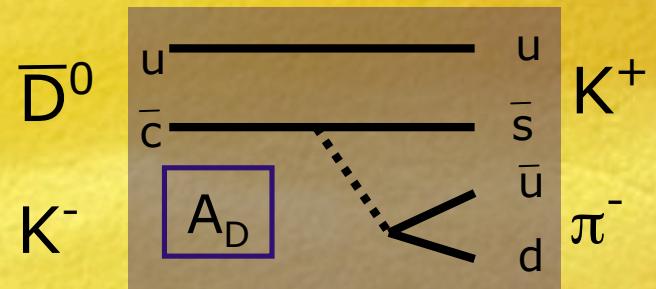
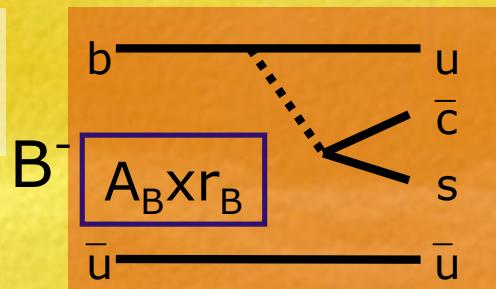
## ● Decay mode

$$B^- \rightarrow D^0 K^- \rightarrow K^+ \pi^-$$



**Color allowed x Doubly-Cabibbo sup.**

$$B^- \rightarrow \bar{D}^0 K^- \rightarrow K^+ \pi^-$$



**Color sup. x Cabibbo allowed**

$$\Gamma(B^- \rightarrow [K^+ \pi^-] K^-) = (r_B^2 + r_D^2 + 2r_B r_D \cos(\delta - \phi_3)) |A_B|^2 |A_D|^2$$

$$\Gamma(B^+ \rightarrow [K^- \pi^+] K^+) = (r_B^2 + r_D^2 + 2r_B r_D \cos(\delta + \phi_3)) |A_B|^2 |A_D|^2$$

## ● Features

- Low statistics
- High sensitivity

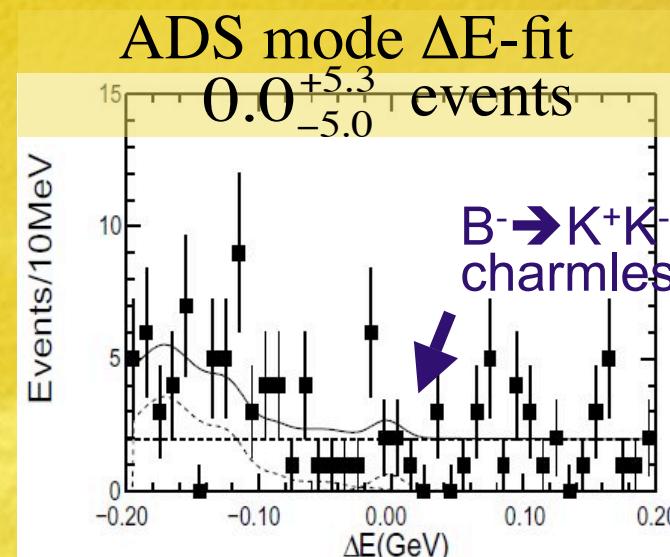
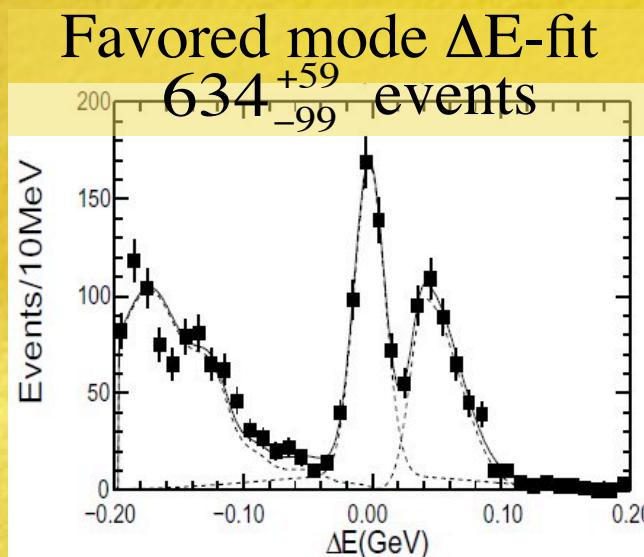
3 unknowns  $r_B, \delta, \phi_3$   
well measured  $r_D, A_B, A_D$



## 4.1. Result on $D_{ADS}K$

•  $B^- \rightarrow D_{ADS} K^-$  w/Belle 386M BB

hep-ex/0508048(2005)



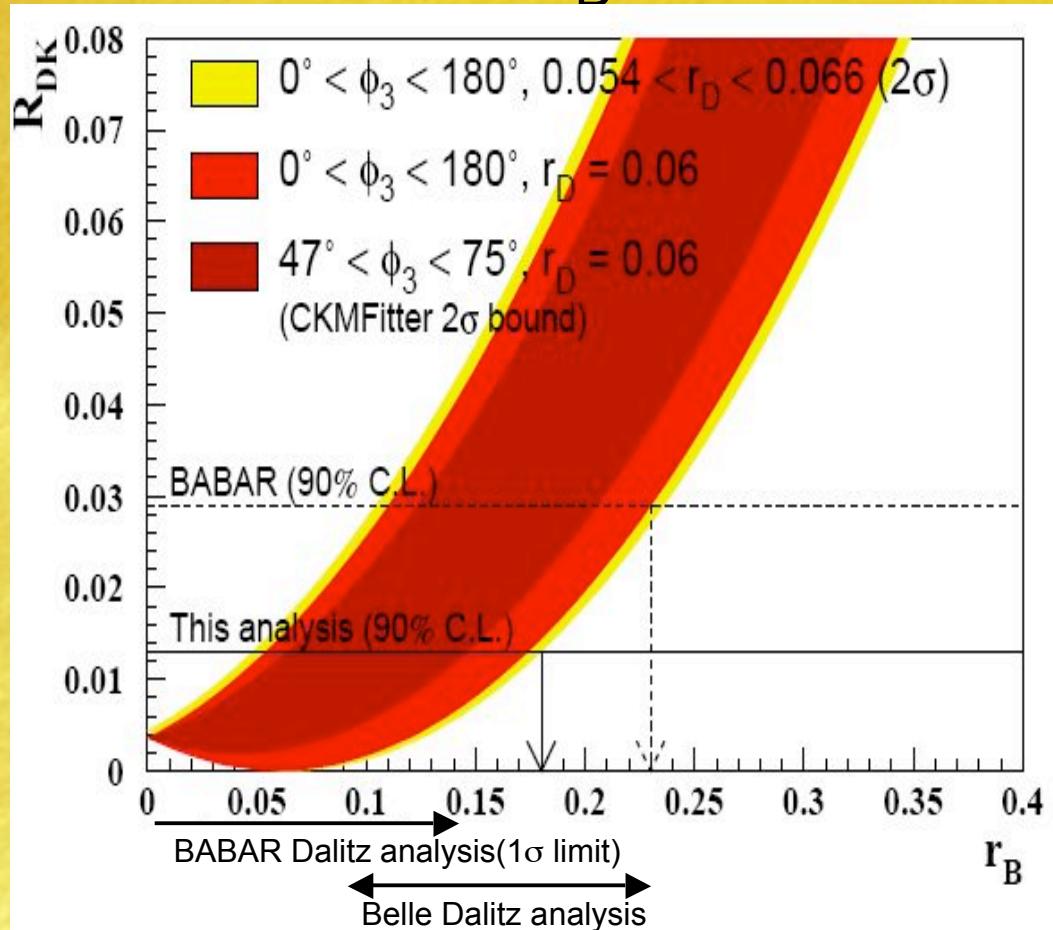
Favored mode

$$\Gamma(B^\mp \rightarrow D_{fav}[K^\mp \pi^\pm]K^\mp) \approx |A_B|^2 |A_D|^2$$

$$\begin{aligned} R_{DK} &\equiv \frac{\Gamma(B^\pm \rightarrow D_{ADS} K^\pm)}{\Gamma(B^\pm \rightarrow D_{fav} K^\pm)} \\ &= r_B^2 + r_D^2 + 2r_B r_D \cos\phi_3 \cos\delta \\ &= (0.0^{+8.4}_{-7.9} (\text{stat}) \pm 1.0 (\text{syst})) \times 10^{-3} \\ &< 0.014 (90\% \text{C.L.}) \end{aligned}$$

# 4.1. Result (cont'd)

## ● Constraint for $r_B$ with $B^- \rightarrow DK^-$ decay



Study of the suppressed decays  $B^- \rightarrow DK^-$   
and  $B^- \rightarrow D_{CP} K^-$  decays at Belle

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# 5. Summary

- GLW & ADS method are model independent methods to extract  $\phi_3$ .

- GLW

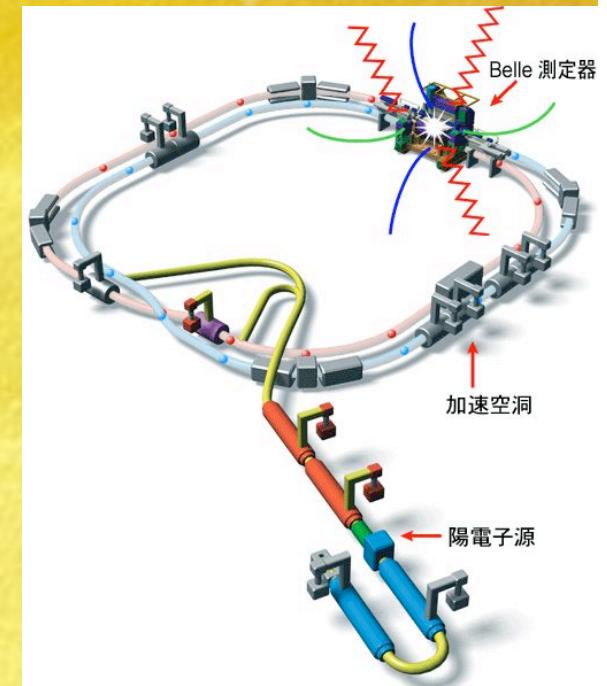
- Measurement for  $B^- \rightarrow D_{CP} K^- / D^*_{CP} K^-$
- Signals are established
- DCPV is not seen yet.

- ADS

- Search for  $B^- \rightarrow D_{ADS} K^-$
- Signal is not seen yet
- But we give a constraint on  $r_B$ .

- We need more  $B\bar{B}$ s.

$B\bar{B}$ s are being mass-produced!





# Backup

Study of the suppressed decays  $B^- \rightarrow D^- K^-$   
and  $B^- \rightarrow D_{CP}^- K^-$  decays at Belle

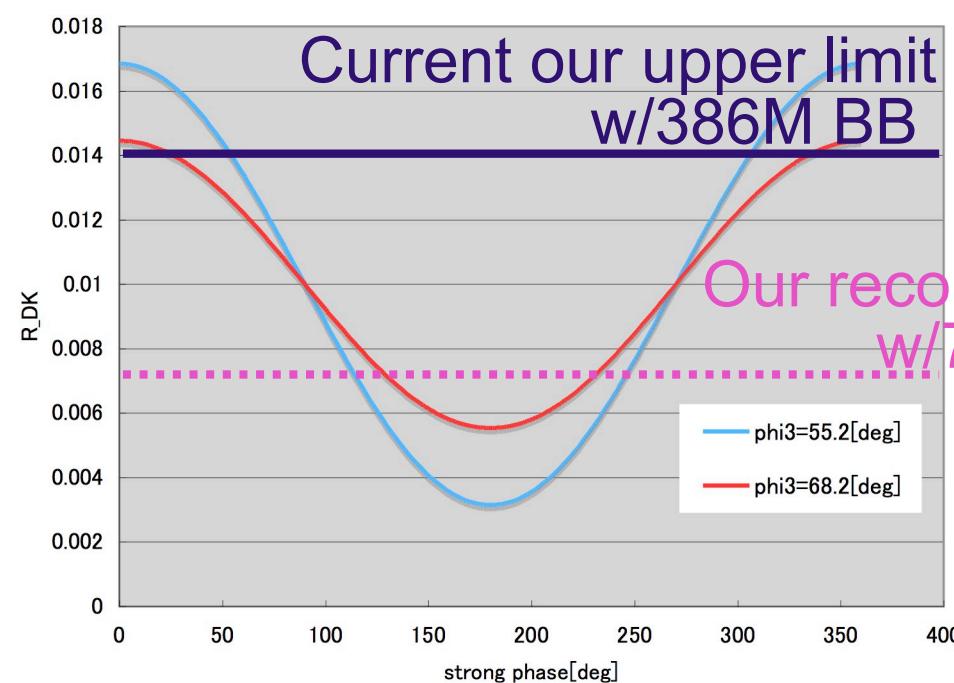
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# How much we need luminosity for $D_{ADS}K$ ?

## Assumptions

- $r_B = 0.1$  (Dalitz+ADS+Dalitz)
- $\phi_3 = 55.2 \sim 68.2^\circ$



Study of the suppressed decays  $B^- \rightarrow DK^-$   
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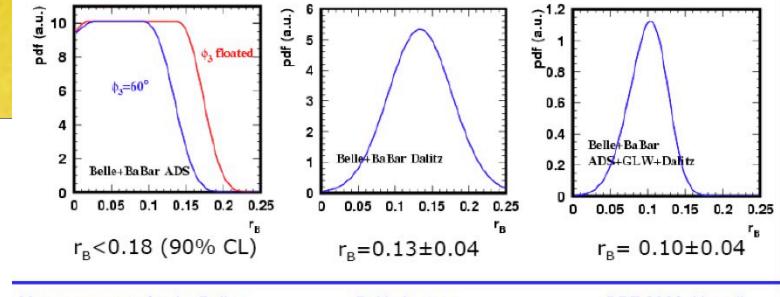


## Constraints to $r_B$

Estimates of  $r_B$  value from the combination of Belle and BaBar data

Construct PDF from different measurements using experimental observables:

- $A_{1,2}, R_{1,2}$  for GLW
  - $R_{DK}$  for ADS
  - $x_{\pm} = r \cos(\pm\phi_3 + \delta), y_{\pm} = r \sin(\pm\phi_3 + \delta)$  for Dalitz
- take strong phases  $\delta_B$  and  $\delta_D$  which maximize PDF  
 $\phi_3$  either floated or taken from indirect UT fit ( $\phi_3 = 60^\circ$ )



# $D^{(*)}_{CP}K$ systematics

	Signal fraction	1.3%
R	Yield extraction	6–8%
	Peaking background	1.3–2%
	Intrinsic detector bias	1%
A	Signal fraction	1.3%
	Yield extraction	2–4%
	Particle identification	1%