

# Semileptonic $D$ Results at CLEO-c

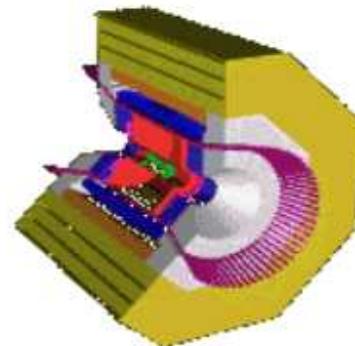
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Representing the CLEO Collaboration

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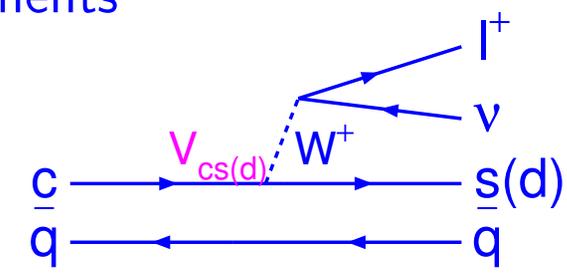


## Topics

- Inclusive  $D$  semileptonic decays (hep-ex/0604044)
- Form factors, and  $V_{cs}$ ,  $V_{cd}$  from  $D \rightarrow K/\pi e^+ \nu$
- First measurement of form factors in  $D \rightarrow \rho e^+ \nu$
- Form factors in  $D^+ \rightarrow K^- \pi^+ e^+ \nu$  (PRD **74**, 052001 (2006))
- First observation of rare decays  $D^+ \rightarrow \eta e^+ \nu$ ,  $D^0 \rightarrow K^- \pi^+ \pi^- e^+ \nu$
- Data Sample: 281 pb<sup>-1</sup> at the  $\psi(3770)$
- All results are preliminary except  $D^+ \rightarrow K^- \pi^+ e^+ \nu$  published

## Why $D$ Semileptonic Decays

- $D$  Semileptonic Decays and CKM matrix elements

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$


- Inclusive semileptonic Decays  $D \rightarrow X e^+ \nu$ 
  - Lepton spectra and BR's (theoretical predictions)
- Exclusive  $D^0 \rightarrow K^- e^+ \nu, \pi^- e^+ \nu$ , etc.:

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cq}|^2 p_P^3 |f_+(q^2)|^2$$

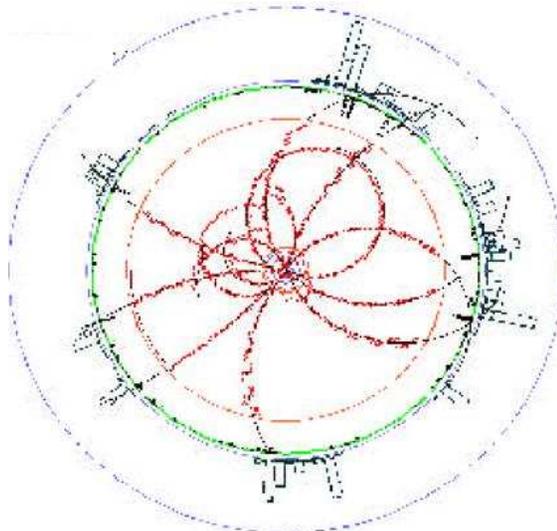
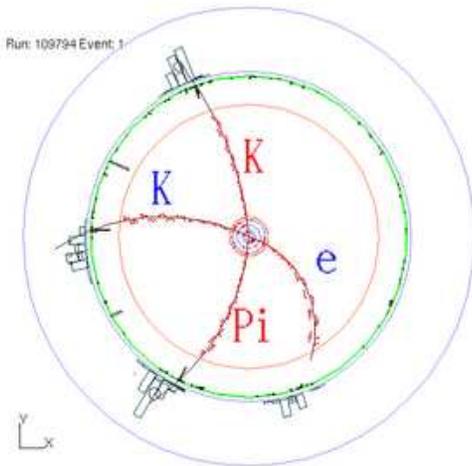
- $V_{cs}, V_{cd}$  and form factors (test LQCD)

# Advantages of $D\bar{D}$ production at the $\psi(3770)$

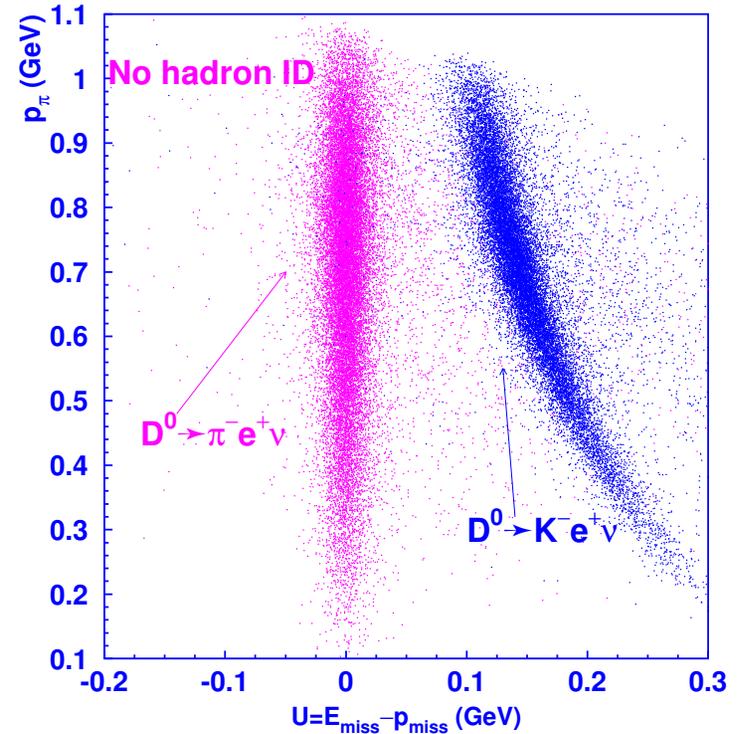
- large cross section ( $\sigma_{D\bar{D}} \sim 6$  nb), low multiplicity ( $\rightarrow$  clean events)

$$\sqrt{s} = \psi(3770)$$

$$\sqrt{s} = \Upsilon(4S)$$



- Unique kinematics: separate S/B



- many systematics cancel in  $\mathcal{B}$  (Double tag)

## Analysis Technique

- How to measure **absolute  $\mathcal{B}$** ?

1.  $D$  Tagging: one  $D$  hadronic decays to tag the  $\bar{D}$  semileptonic decays

$$\begin{aligned} \triangleright D \text{ Tag: } N_{tag} &= 2N_{D\bar{D}}\mathcal{B}_{tag}\epsilon_{tag} & \begin{cases} M_{bc} = \sqrt{E_{beam}^2 - p_D^2} \\ \Delta E = E_D - E_{beam} \end{cases} \\ \triangleright D \text{ Semilep: } N_{sig} &= 2N_{D\bar{D}}\mathcal{B}\mathcal{B}_{tag}\epsilon_{sig} & U = E_{miss} - p_{miss} \text{ peaks @0.} \end{aligned}$$

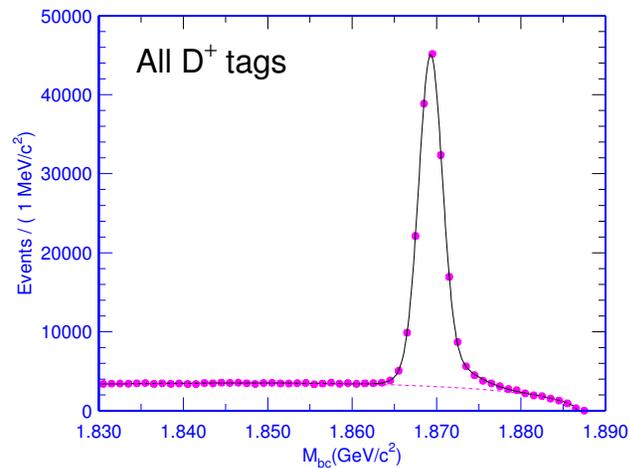
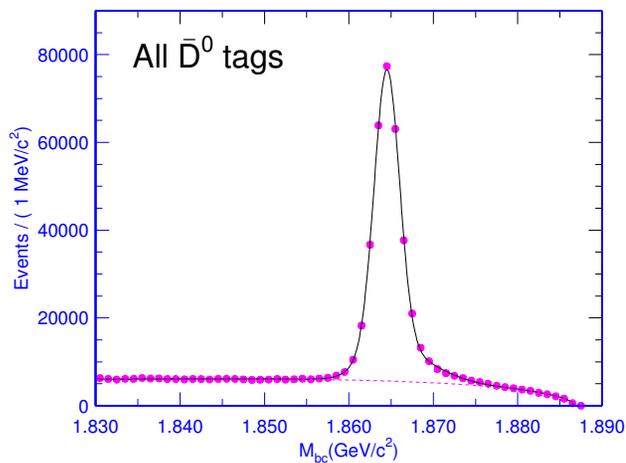
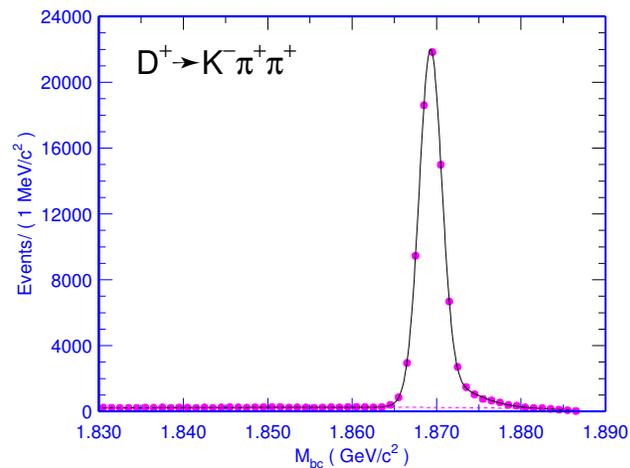
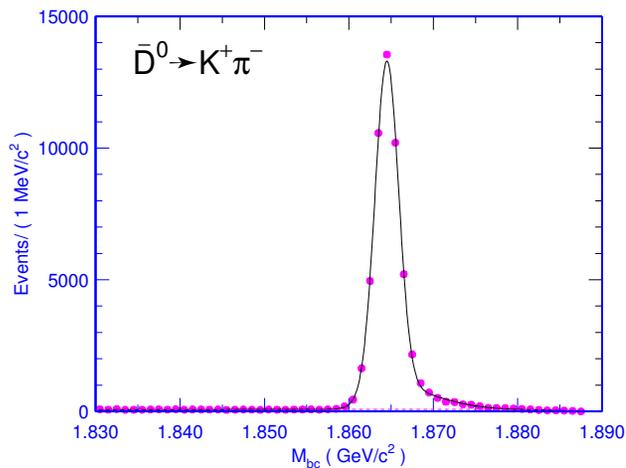
$$\Rightarrow \mathcal{B} = \frac{N_{sig}/\epsilon_{sig}}{N_{tag}/\epsilon_{tag}} = \frac{N_{sig}}{N_{tag}\epsilon_{sig}/\epsilon_{tag}}$$

2. Without  $D$  Tagging: neutrino reconstruction  $\vec{p}_\nu = \vec{p}_{evt} - (\vec{p}_{chrg} + \vec{p}_{neu})$

$$\triangleright D \text{ reconstructed by } \begin{cases} \Delta E = E_{had} + E_e + |\vec{p}_\nu| - E_{beam} \\ M_{bc} = \sqrt{E_{beam}^2 - (\vec{p}_{had} + \vec{p}_e + \vec{p}_\nu)^2} \end{cases}$$

$$\triangleright \mathcal{B} = \frac{N_D}{2N_{D\bar{D}}\epsilon}$$

# Single $D$ Tagging



•  $\sim 308\text{K } D^0$  tag

$\sim 163\text{K } D^+$  tag fully reconstructed

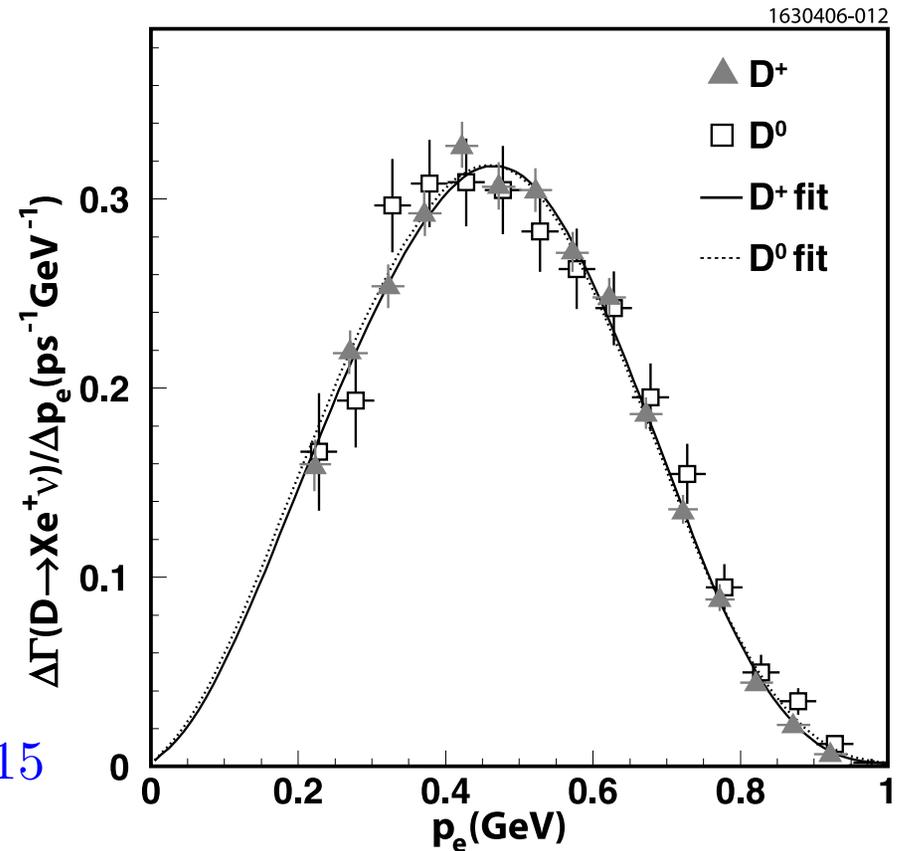
# Inclusive $D$ Semileptonic Decays

mode	branching fraction
$D^0 \rightarrow Xe^+\nu$	$(6.46 \pm 0.17 \pm 0.13)\%$
$\sum_{excl.} \mathcal{B}(D^0 \rightarrow Xe^+\nu)$	$(6.1 \pm 0.2 \pm 0.2)\%$
$D^+ \rightarrow Xe^+\nu$	$(16.13 \pm 0.20 \pm 0.33)\%$
$\sum_{excl.} \mathcal{B}(D^+ \rightarrow Xe^+\nu)$	$(15.1 \pm 0.5 \pm 0.5)\%$

- consistent with the known exclusive modes saturating the inclusive BR's

$$\frac{\Gamma_{D^+}^{SL}}{\Gamma_{D^0}^{SL}} = \frac{\mathcal{B}_{D^+}^{SL}}{\mathcal{B}_{D^0}^{SL}} \times \frac{\tau_{D^0}}{\tau_{D^+}} = 0.985 \pm 0.028 \pm 0.015$$

- consistent with isospin symmetry
- hep-ex/0604044, submitted to PRL.



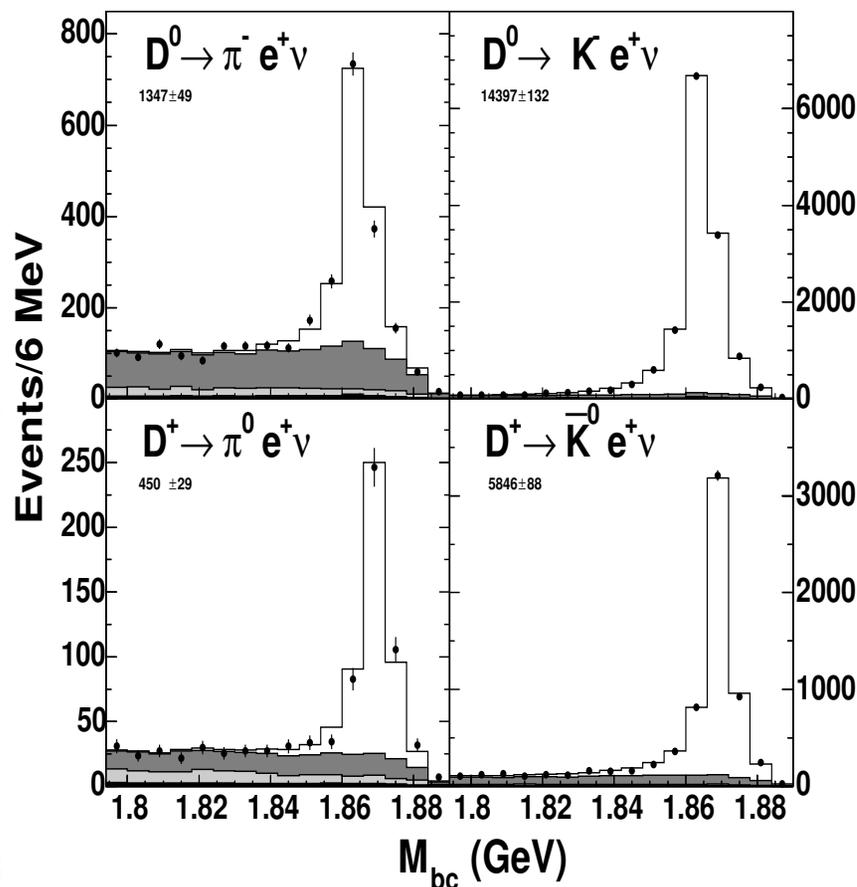
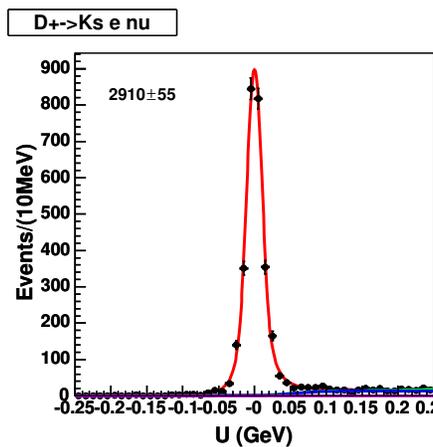
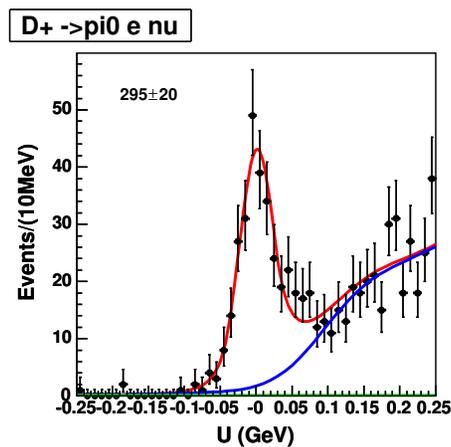
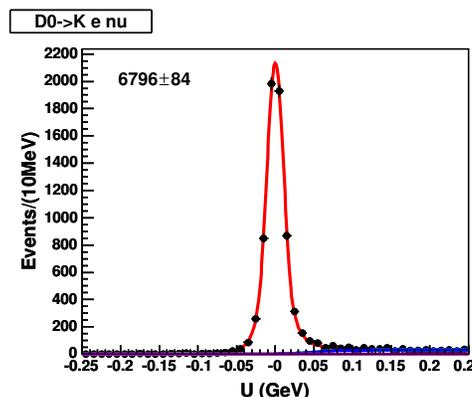
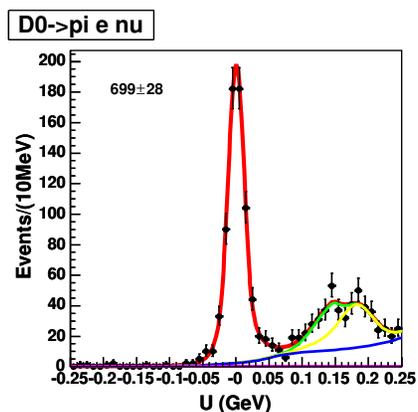
Extrapolated below  $p_e < 0.2$  GeV/c.

# $D \rightarrow K/\pi e^+ \nu$ : Tagged and Untagged

Tagged

40% common samples!

Untagged



## Results of $D$ Semileptonic Decays

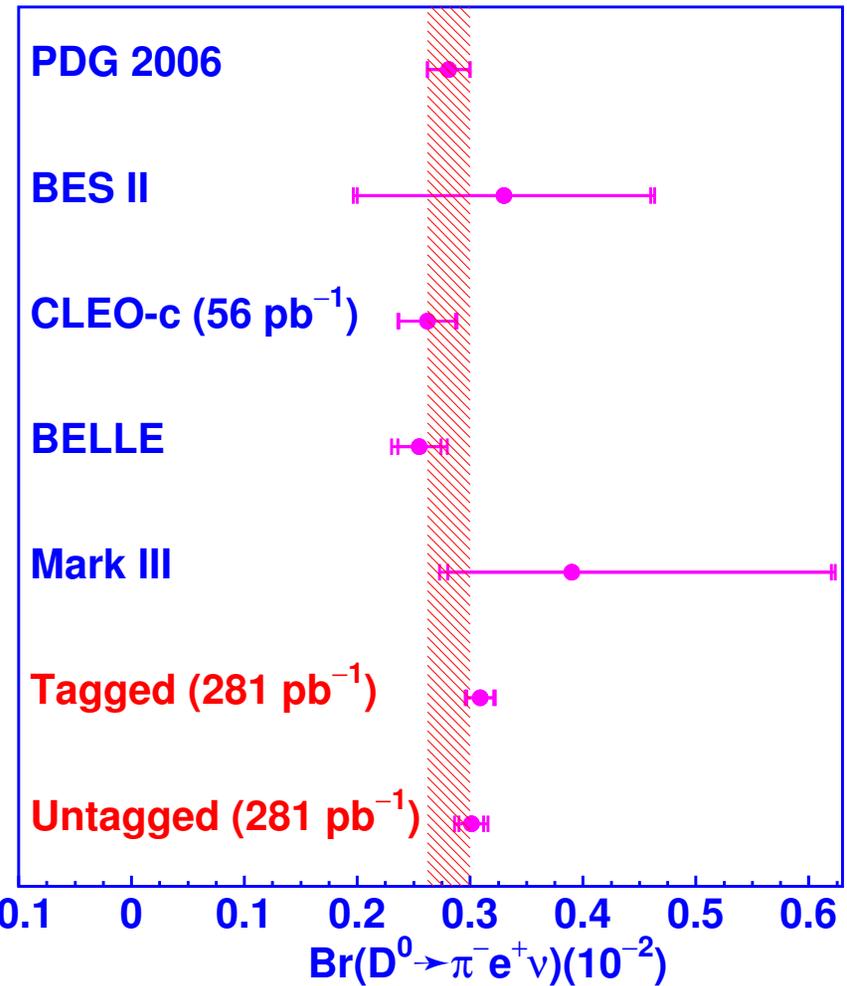
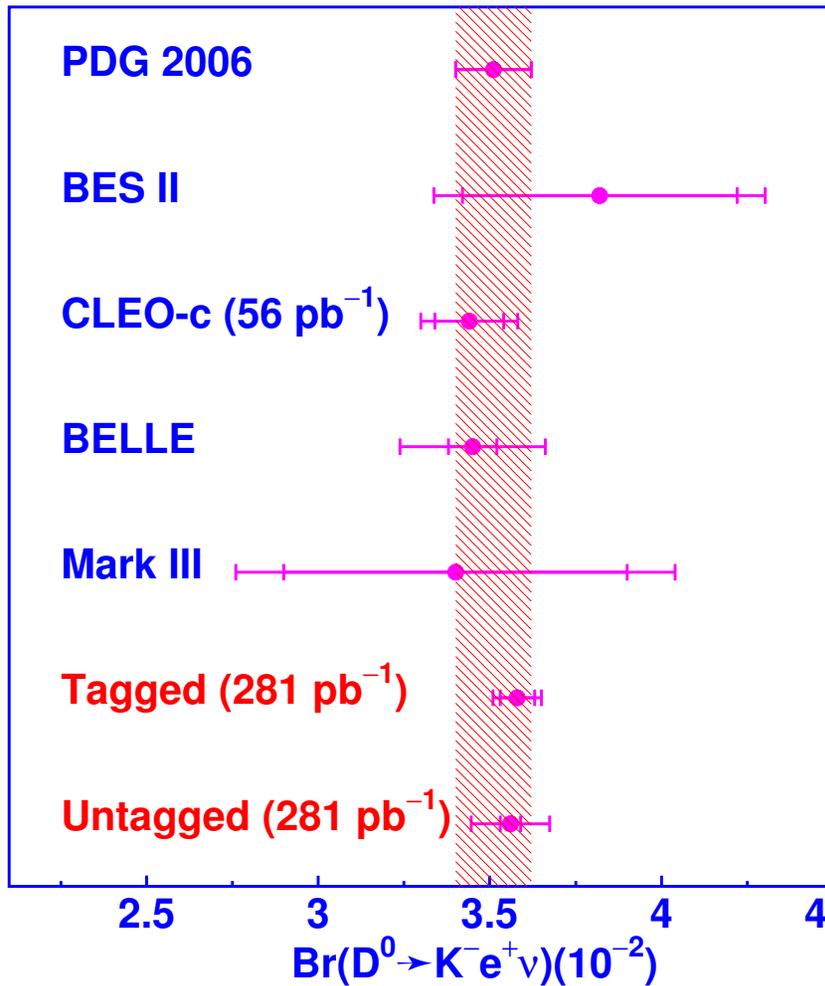
- $D$  Semileptonic BR's

Mode	Tag (%)	Untag (%)	PDG'06 (%)
$D^0 \rightarrow K^- e^+ \nu$	$3.58 \pm 0.05 \pm 0.05$	$3.56 \pm 0.03 \pm 0.11$	$3.51 \pm 0.11$
$D^0 \rightarrow \pi^- e^+ \nu$	$0.309 \pm 0.012 \pm 0.006$	$0.301 \pm 0.011 \pm 0.010$	$0.281 \pm 0.019$
$D^+ \rightarrow \bar{K}^0 e^+ \nu$	$8.86 \pm 0.17 \pm 0.20$	$8.75 \pm 0.13 \pm 0.30$	$8.6 \pm 0.5$
$D^+ \rightarrow \pi^0 e^+ \nu$	$0.397 \pm 0.027 \pm 0.028$	$0.383 \pm 0.025 \pm 0.016$	$0.44 \pm 0.07$

Ratio	$\frac{\Gamma(D^0 \rightarrow \pi^- e^+ \nu)}{\Gamma(D^0 \rightarrow K^- e^+ \nu)}$	$\frac{\Gamma(D^0 \rightarrow \pi^- e^+ \nu)}{\Gamma(D^+ \rightarrow \pi^0 e^+ \nu)}$	$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu)}{\Gamma(D^+ \rightarrow K^0 e^+ \nu)}$
CLEO-c	$(8.5 \pm 0.3 \pm 0.1)\%$	$1.95 \pm 0.15 \pm 0.14$	$1.02 \pm 0.02 \pm 0.02$
		$1.99 \pm 0.15 \pm 0.10$	$1.03 \pm 0.02 \pm 0.04$
PDG'06	$8.0 \pm 0.6$		

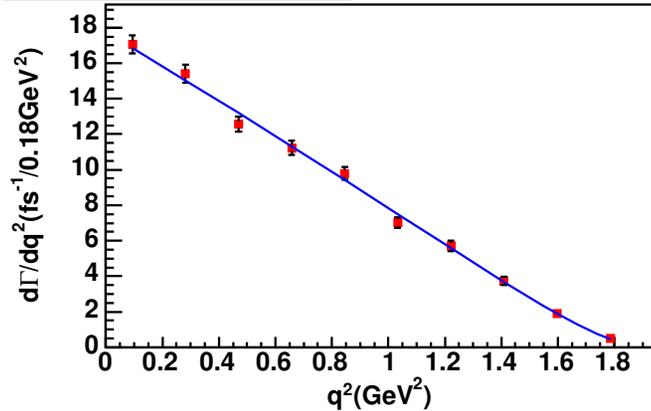
- More precise results
- Ratios of  $\frac{\Gamma_{D^0}}{\Gamma_{D^+}}$  consistent with isospin symmetry
- PDG'06 dominated by CLEO-c results from  $56 \text{ pb}^{-1}$

# Comparison with Other Results

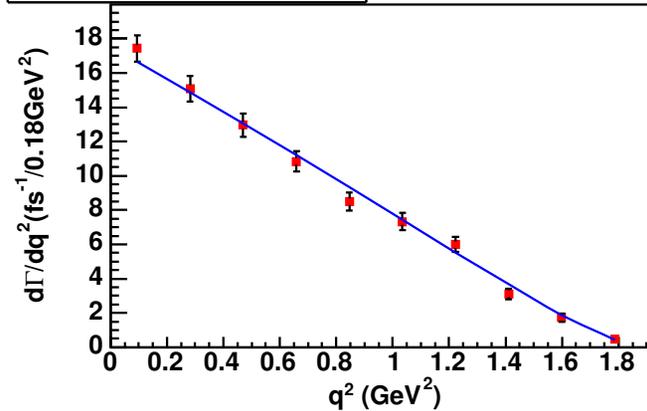


# Form Factor Fits (Tagged)

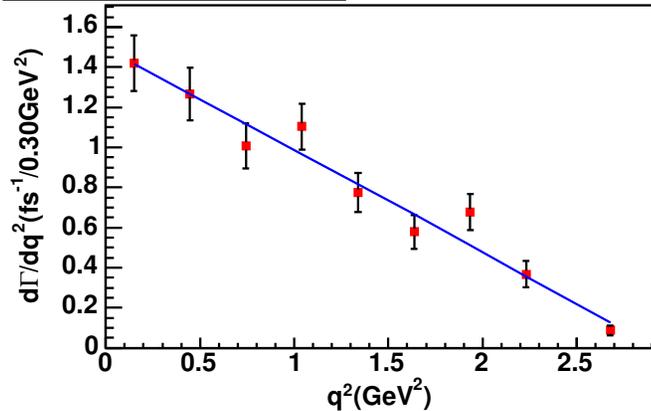
Decay Rate for  $D^0 \rightarrow K e \nu$



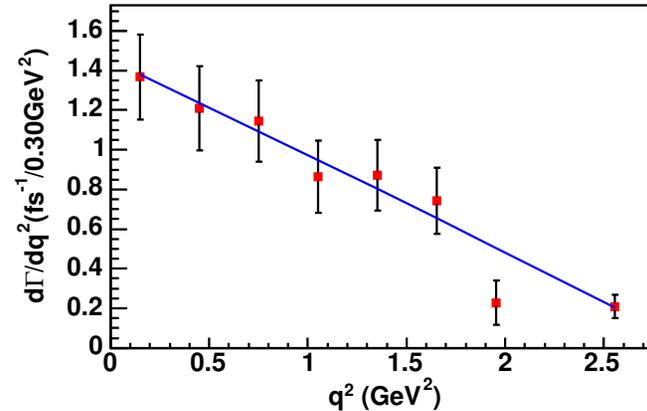
Decay Rate for  $D^+ \rightarrow K_s e \nu$



Decay Rate for  $D^0 \rightarrow \pi e \nu$

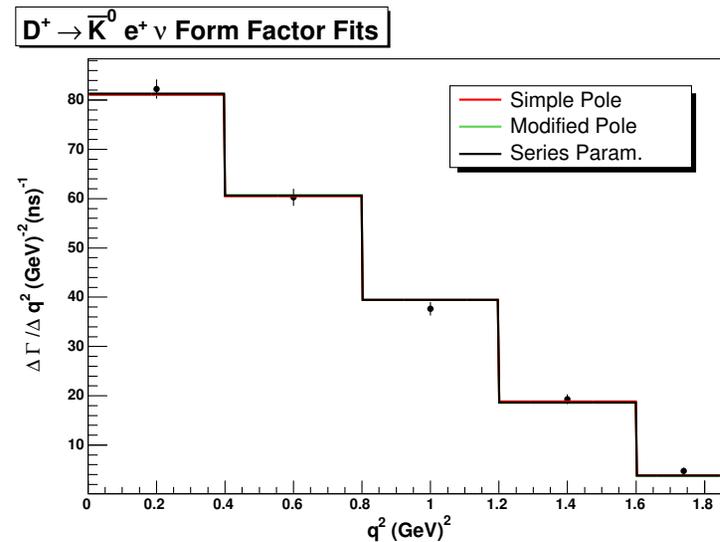
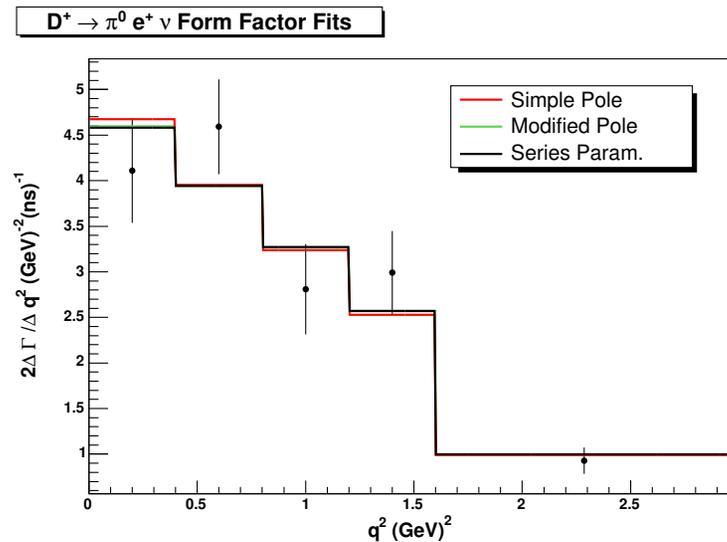
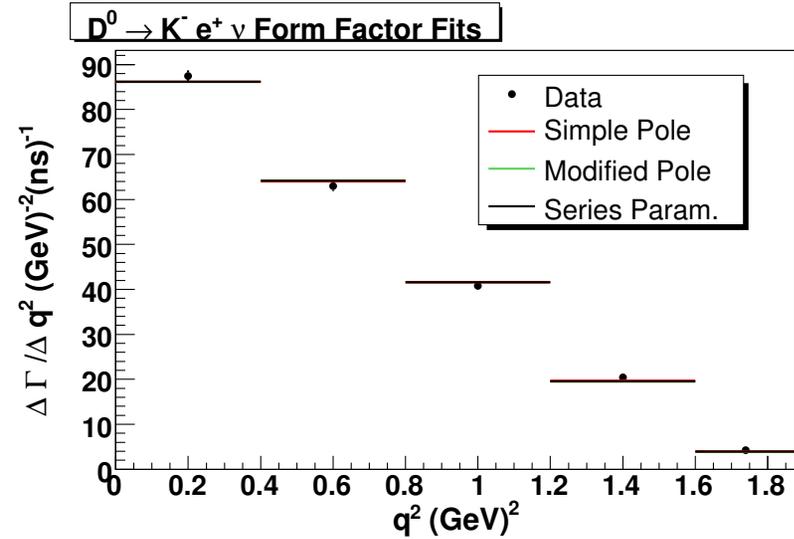
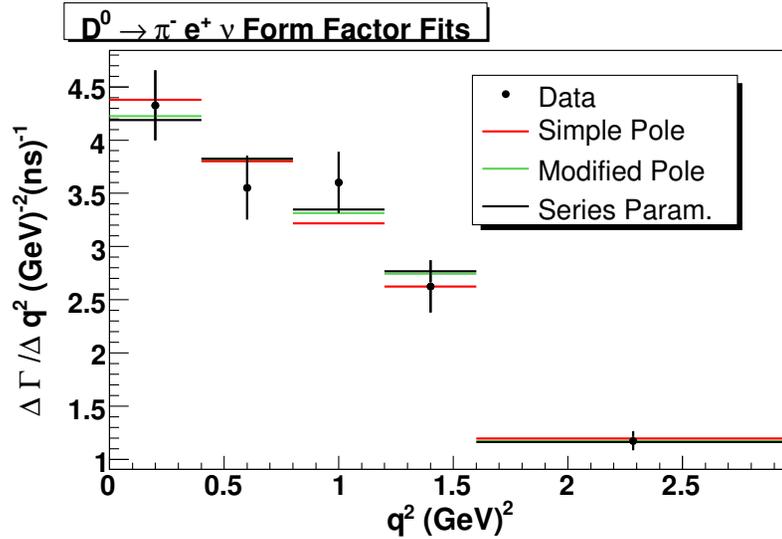


Decay Rate for  $D^+ \rightarrow \pi^0 e \nu$



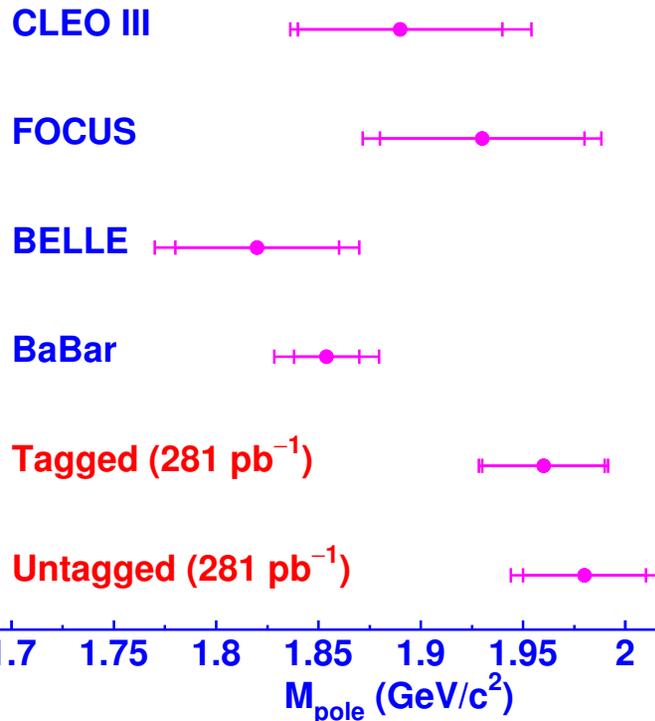
- Modified pole  $f_+(q^2) = \frac{f_+(0)}{(1-q^2/M_{pole}^2)(1-\alpha q^2/M_{pole}^2)} \Rightarrow$  simple pole ( $\alpha = 0$ ).
- Hill series expansion (Phys. Lett. **B633**, 61 (2006)).

# Form Factor Fits (Untagged)

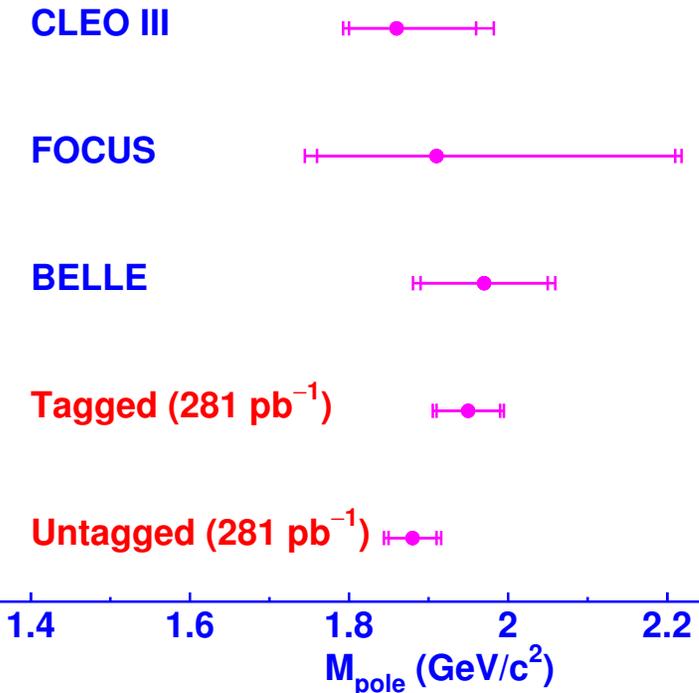


# Form Factor Fits (Tagged/Untagged)

## $D \rightarrow K e^+ \nu$

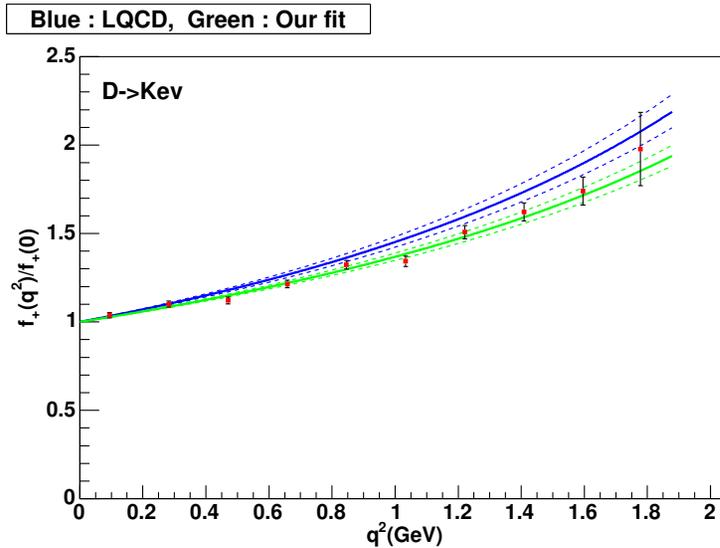
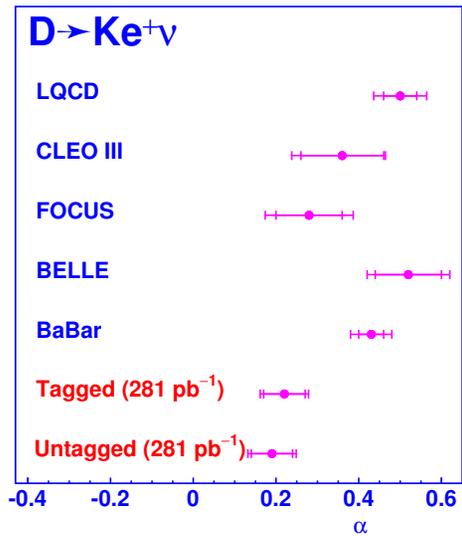
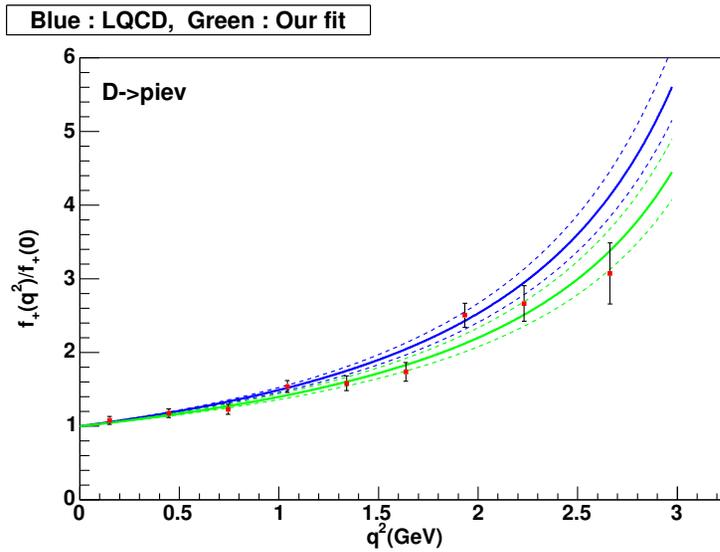
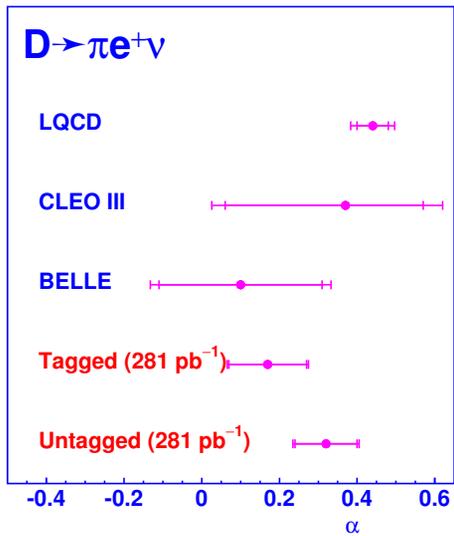


## $D \rightarrow \pi e^+ \nu$



Mode	$M_{pole}$ (Tagged)	$M_{pole}$ (Untagged)
$D \rightarrow K e \nu$	$1.96 \pm 0.03 \pm 0.01$	$1.98 \pm 0.03 \pm 0.02$
$D \rightarrow \pi e \nu$	$1.95 \pm 0.04 \pm 0.02$	$1.88 \pm 0.03 \pm 0.02$

# Form Factors and Tests of LQCD

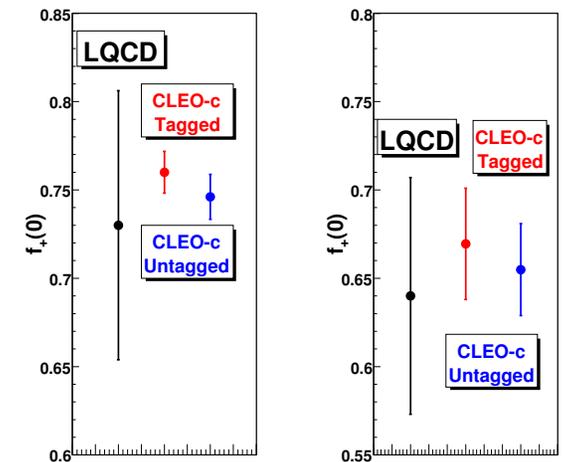


## $V_{cs}$ and $V_{cd}$ Results

With  $f_+(0)$  from unquenched LQCD (PRL 94, 011601 (2005)) and  $V_{cx} f_+(0)$  values from fits  $\rightarrow V_{cs}$  and  $V_{cd}$

Mode	$V_{cx} \pm (stat.) \pm (sys.) \pm (theory)$	PDG'06
$D \rightarrow \pi e \nu$ (tagged)	$0.234 \pm 0.010 \pm 0.004 \pm 0.024$	$0.230 \pm 0.011$
$D \rightarrow \pi e \nu$ (untagged)	$0.229 \pm 0.007 \pm 0.005 \pm 0.024$	$0.230 \pm 0.011$
$D \rightarrow K e \nu$ (tagged)	$0.996 \pm 0.008 \pm 0.015 \pm 0.104$	$0.957 \pm 0.095$
$D \rightarrow K e \nu$ (untagged)	$1.014 \pm 0.013 \pm 0.009 \pm 0.106$	$0.957 \pm 0.095$

- Expt. uncertainty  $V_{cs} < 2\%$ ,  $V_{cd} < 4\%$ , LQCD  $\sim 10\%$ .
- Alternatively,  $V_{cs}$  ( $W \rightarrow cs$ ) and  $V_{cd} = -V_{us}$  from other experiments, we determine  $f_+(0)$  ( $< 2\%$  for  $f_+(0)^K$ ,  $< 4\%$  for  $f_+(0)^\pi$ ) to test LQCD ( $\sim 10\%$ ).
- Tagged/Untagged: 40% overlap, DO NOT AVERAGE
- Results from untagged method are about to be submitted to PRL and PRD

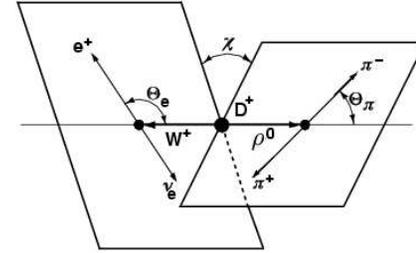


$$D \rightarrow \rho e^+ \nu$$

- Five variables:  $q^2$ ,  $\cos \theta_\ell$ ,  $\cos \theta_V$ ,  $\chi$  and  $M_V$

$$d\Omega \equiv dq^2 d \cos \theta_\pi d \cos \theta_e d\chi dm(\pi\pi)$$

4-D ( $q^2$ ,  $\cos \theta_\ell$ ,  $\cos \theta_V$ ,  $\chi$ ) fit to data



$$\begin{aligned} \frac{d\Gamma}{d\Omega} = & \mathcal{B}(\rho \rightarrow \pi\pi) \frac{3G_F^2 |V_{cd}|^2}{8(4\pi)^4} p_{\rho^0} q^2 BW(m(\pi\pi)) \times \left\{ (1 + \cos \theta_e)^2 \sin^2 \theta_\pi |H_+(q^2, m(\pi\pi))|^2 \right. \\ & + (1 - \cos \theta_e)^2 \sin^2 \theta_\pi |H_-(q^2, m(\pi\pi))|^2 + 4 \sin^2 \theta_e \cos^2 \theta_\pi |H_0(q^2, m(\pi\pi))|^2 \\ & + 4 \sin \theta_e (1 + \cos \theta_e) \sin \theta_\pi \cos \theta_\pi \cos \chi H_+(q^2, m(\pi\pi)) H_0(q^2, m(\pi\pi)) \\ & - 4 \sin \theta_e (1 - \cos \theta_e) \sin \theta_\pi \cos \theta_\pi \cos \chi H_-(q^2, m(\pi\pi)) H_0(q^2, m(\pi\pi)) \\ & \left. - 2 \sin^2 \theta_e \sin^2 \theta_\pi \cos 2\chi H_+(q^2, m(\pi\pi)) H_-(q^2, m(\pi\pi)) \right\} \end{aligned}$$

$$H_\pm(q^2) = (M_D + M_V) A_1(q^2) \mp 2 \frac{M_D p_V}{M_D + M_V} V(q^2),$$

$$H_0(q^2) = \frac{1}{2M_V \sqrt{q^2}} \left[ (M_D^2 - M_V^2 - q^2) (M_D + M_V) A_1(q^2) - 4 \frac{M_D^2 p_V^2}{M_D + M_V} A_2(q^2) \right]$$

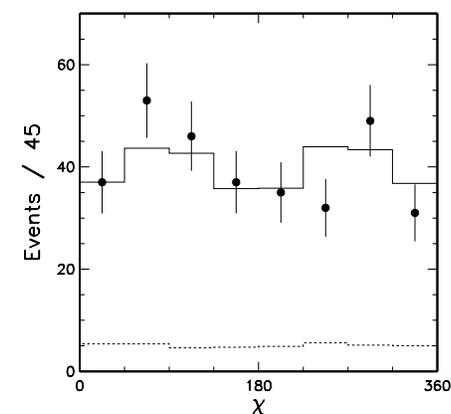
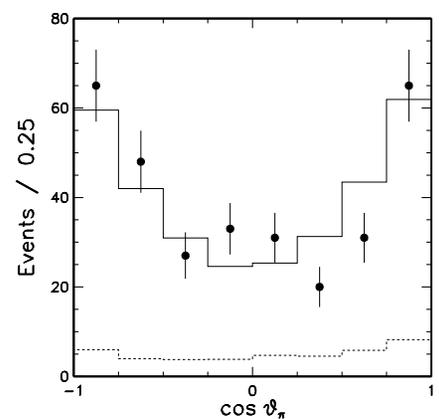
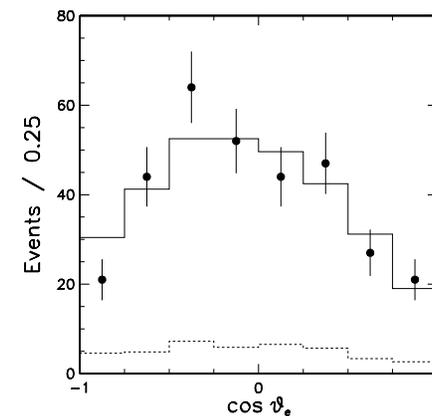
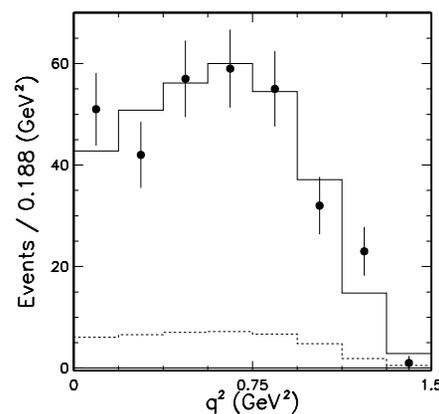
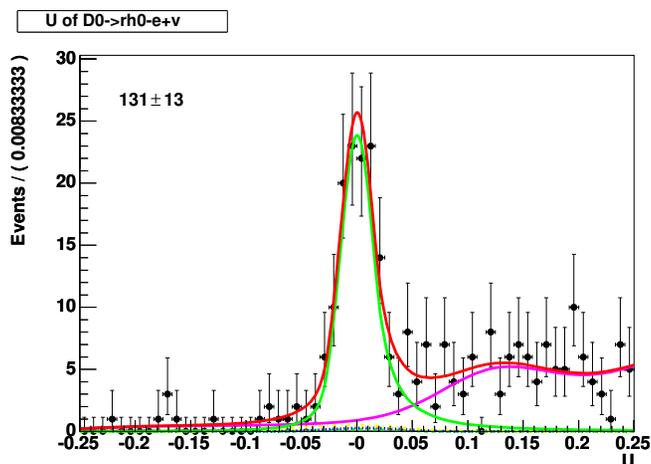
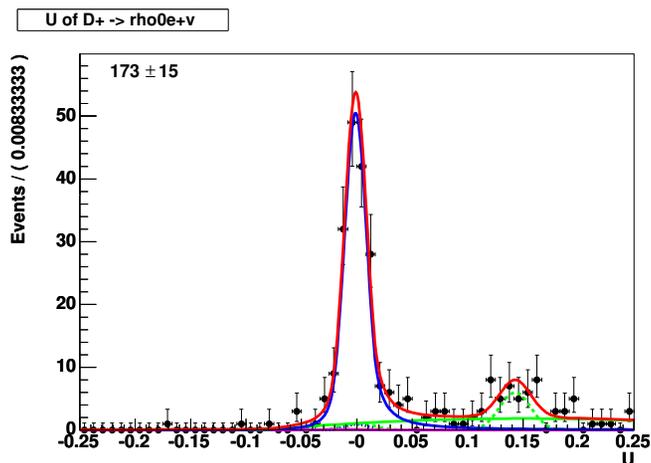
$$A_{1(2)}(q^2) = \frac{A_{1(2)}(0)}{1 - q^2/M_A^2} \quad V(q^2) = \frac{V(0)}{1 - q^2/M_V} \quad R_V \equiv \frac{V(0)}{A_1(0)} \quad R_2 \equiv \frac{A_2(0)}{A_1(0)}$$

# Form Factors in $D \rightarrow \rho e^+ \nu$

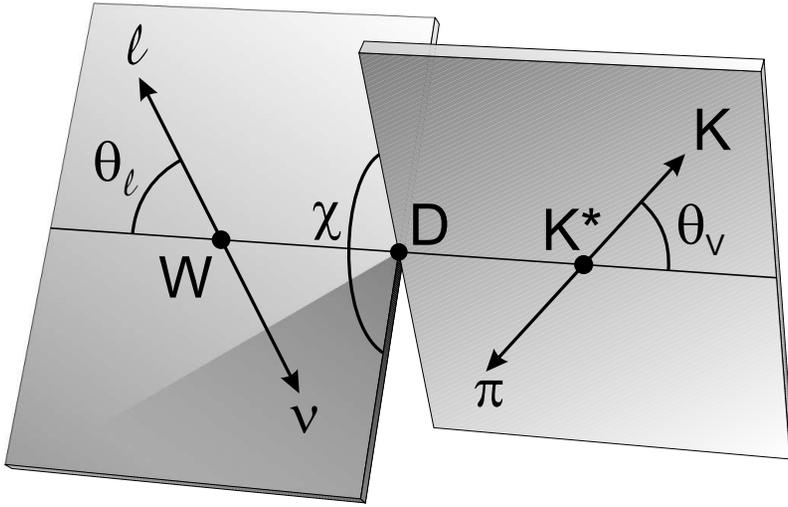
- Improved BR's

$$\mathcal{B}(D^0) = (1.56 \pm 0.16 \pm 0.09) \times 10^{-3}$$

$$\mathcal{B}(D^+) = (2.32 \pm 0.20 \pm 0.12) \times 10^{-3}$$



- $R_V = 1.40 \pm 0.25 \pm 0.03$ ,  
 $R_2 = 0.57 \pm 0.18 \pm 0.06$
- First measurement of FF



- $\frac{d\Gamma}{d \cos \theta_\ell d \cos \theta_V d\chi dq^2 dm_V}$
- $A_{1(2)}(q^2) = \frac{A_{1(2)}(0)}{1 - q^2/M_A^2}$ ,
- $V(q^2) = \frac{V(0)}{1 - q^2/M_V^2}$
- $R_V \equiv \frac{V(0)}{A_1(0)}$ ,  $R_2 \equiv \frac{A_2(0)}{A_1(0)}$

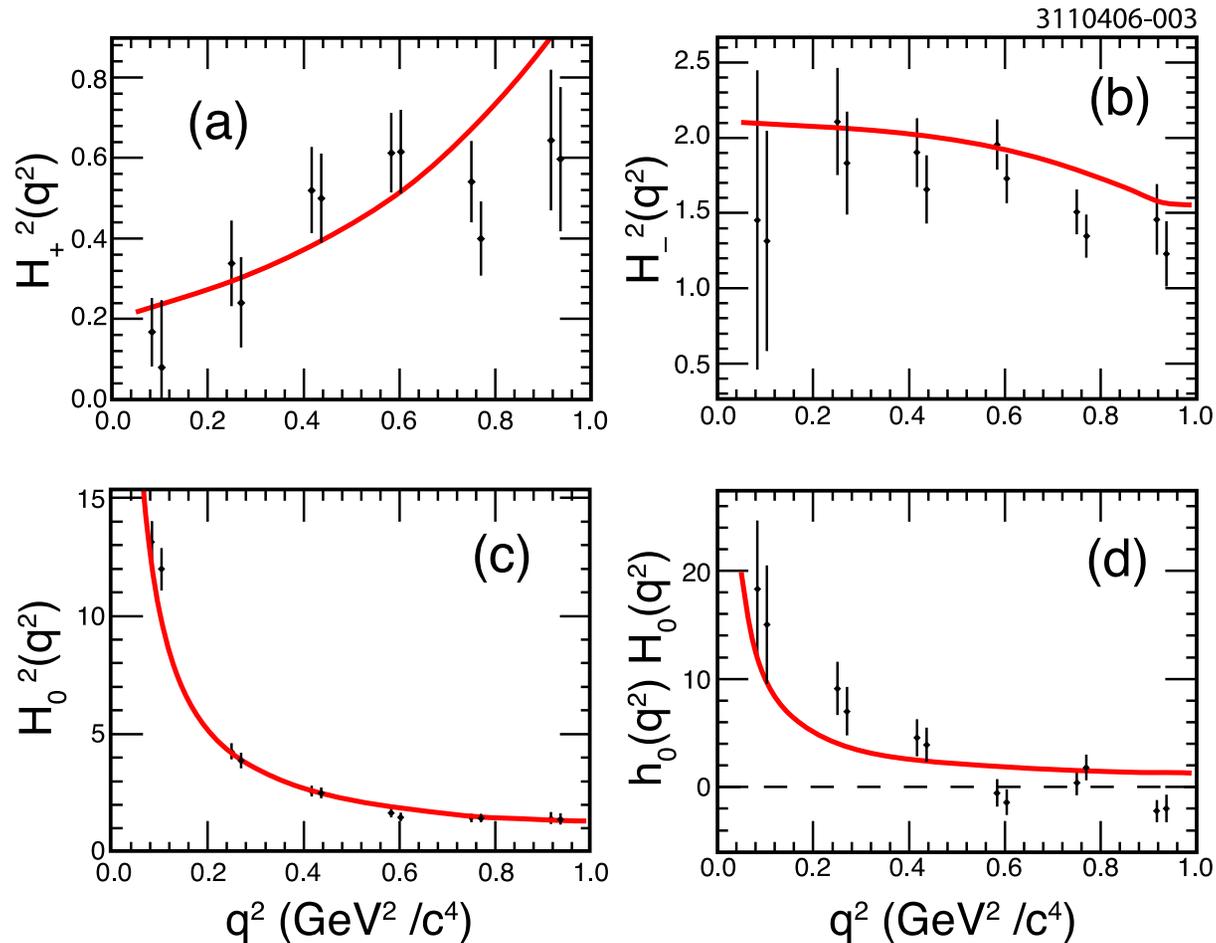
$$\int |A|^2 d\chi \propto \left\{ \begin{array}{l} ((1 + \cos \theta_\ell) \sin \theta_V)^2 |H_+(q^2)|^2 |BW|^2 \\ + ((1 - \cos \theta_\ell) \sin \theta_V)^2 |H_-(q^2)|^2 |BW|^2 \\ + (2 \sin \theta_\ell \cos \theta_V)^2 |H_0(q^2)|^2 |BW|^2 \\ + 8 \sin^2 \theta_\ell \cos \theta_V H_0(q^2) h_0(q^2) \text{Re}\{A e^{-i\delta} BW\} \\ \mathcal{O}(A^2) \end{array} \right\}$$

$$H_\pm(q^2) = (M_D + M_V) A_1(q^2) \mp 2 \frac{M_D p_V}{M_D + M_V} V(q^2),$$

$$H_0(q^2) = \frac{1}{2M_V \sqrt{q^2}} \left[ (M_D^2 - M_V^2 - q^2) (M_D + M_V) A_1(q^2) - 4 \frac{M_D^2 p_V^2}{M_D + M_V} A_2(q^2) \right],$$

(S-wave  $h_0 = H_0$  assumed when present in  $K^*$ )

## Form Factors in $D^+ \rightarrow K^- \pi^+ e^+ \nu$

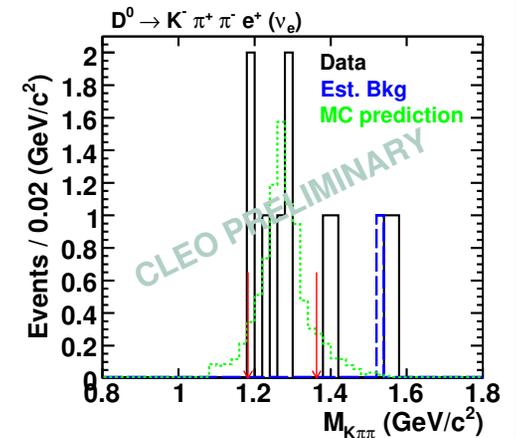
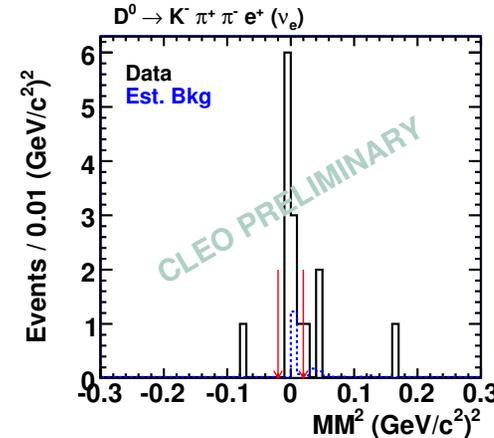
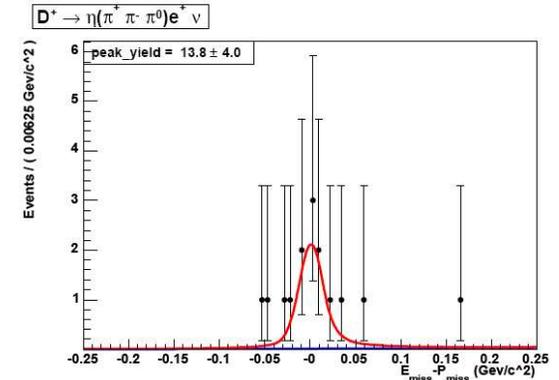
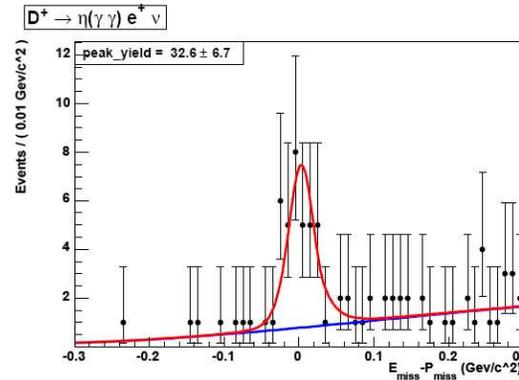


- significant S-wave amp. confirmed ( $h_0 \neq 0$ ), no evidence for d- or f-wave (PRD **74** 052001 (2006), two sets of event selection )

# Rare $D$ Semileptonic Decays

- $L=281 \text{ pb}^{-1}$ , all results are preliminary

Mode	$\mathcal{B}(\times 10^{-4})$
$\eta e^+ \nu$	$12.9 \pm 1.9 \pm 0.7$
$K^- \pi^+ \pi^- e^+ \nu$	$2.9^{+1.5}_{-1.1} \pm 0.5$
$K_1(1270) e^+ \nu$	$2.2^{+1.4}_{-1.1} \pm 0.2$
$\omega e^+ \nu$	$14.9 \pm 2.7 \pm 0.5$
$\eta' e^+ \nu$	$< 3$ (@ CL=90%)
$\phi e^+ \nu$	$< 2$ (@ CL=90%)

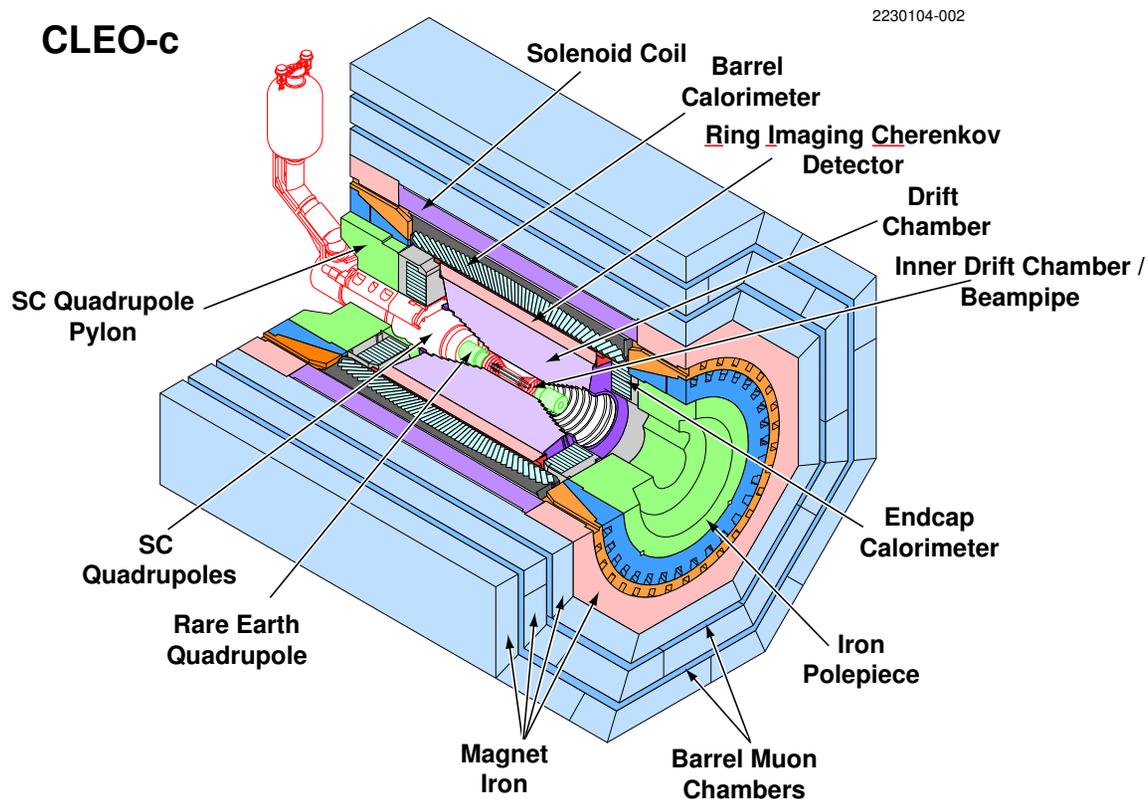


- **first** observation of  $\eta e^+ \nu$  and  $K^- \pi^+ \pi^- (K_1) e^+ \nu$
- improved  $\mathcal{B}(\omega e^+ \nu)$  and ULs for  $\eta' e^+ \nu$  and  $\phi e^+ \nu$ .

## Summary

- Precise inclusive lepton spectra
- Precise  $D$  semileptonic BR's  $\rightarrow V_{cs}$  and  $V_{cd}$
- Precise results on  $D \rightarrow Pe^+\nu$  form factors to test LQCD
- First study of FF in  $D \rightarrow \rho e^+\nu$  and confirmed significant S-wave amplitude in  $D^+ \rightarrow K^{*0}e^+\nu$ .
- Search for new mode, first observation of  $\eta e^+\nu$  and  $K^-\pi^+\pi^-e^+\nu$
- We expect further improvement with more data (750 pb<sup>-1</sup> planned).

# CLEO-c Detector



- CLEO-c:

- ◇  $B=1$  T;
- ◇ tracking (93% of  $4\pi$ )
  - ▷ 16 axial, 31 stereo lay.
  - ▷  $\sigma_p/p \sim 0.6\%$
- ◇ CsI (95% of  $4\pi$ )
  - ▷  $\sigma_E/E \sim 5\%$  @ 0.1 GeV
  - ▷  $\sim 2.2\%$  @ 1 GeV
- ◇ Hadron ID
  - ▷ RICH (80% of  $4\pi$ )+dE/dx
  - ▷  $\epsilon_K > 90\%$  w/ few% fakes
- ◇ Electron ID
  - ▷ RICH+dE/dx + CsI