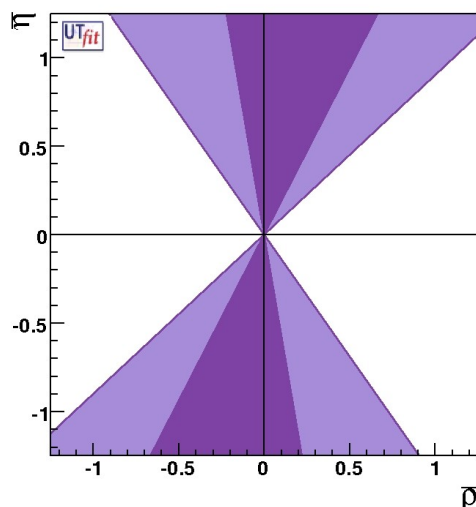


Measurement of the UT angle γ at BaBar

Virginia Azzolini

IFIC – Universitat de Valencia – CSIC
(on behalf of the BaBar Collaboration)



Outline:

Measurements of γ using $B^\pm \rightarrow D^{(*)}K^{(*)\pm}$

GLW Method

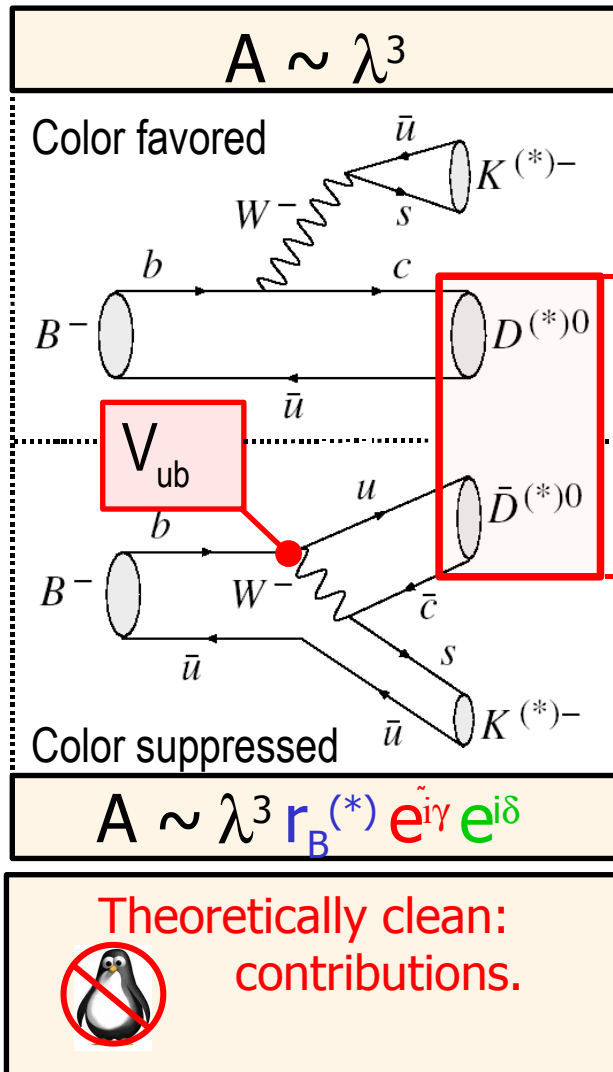
ADS Method

D^0 Dalitz Method (GGSZ)



Methods overview

Access γ via interference between $b \rightarrow c \bar{u} s$ and $b \rightarrow u \bar{c} s$ decay processes
 Reconstruct D in final states f accessible to both to D^0 and \bar{D}^0



Three methods		
GLW D^0 CP-modes $K^+K^-, \pi^+\pi^-$ [CP+] $K_S\pi^0, K_S\omega, K_S\phi$ [CP-]	ADS DCSD mode $K^+\pi^-$ $\bar{D}^0 \rightarrow K^+\pi^-$ suppr. $D^0 \rightarrow K^+\pi^-$ fav.	GGSZ Dalitz $K_S\pi^+\pi^-$

δ = relative (unknown) strong phase

γ = weak phase

$r_B^{(*)}$ = (critical) ratio of suppr./fav. amplitudes:

$$r_B^{(*)} = \frac{|A(B^- \rightarrow \bar{D}^{(*)0} K^-)|}{|A(B^- \rightarrow D^{(*)0} K^-)|} \sim 0.1 - 0.2$$

Larger r_B

→ Larger interference

→ better γ experimental precision

PL B265, 172 (1991)
 PL B557, 198 (2003)

Gronau-London-Wyler method

Phys. Lett. B253, 483; Phys. Lett. B265, 172 (1991)

- Reconstruct D meson in CP-eigenstates (accessible to D^0 and \bar{D}^0)
even (CP = +1 $\pi^+\pi^-$, K^+K^-) & odd (CP = -1 $K_S^0\pi^0$, $K_S^0\phi$, $K_S^0\omega$)
- Measure 4 observables $R_{CP\pm}$, $A_{CP\pm}$ (formulae for D^0K):

$$R_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{2\Gamma(B^- \rightarrow D^0 K^-)} = 1 \pm 2r_B \cos \gamma \cos \delta_B + r_B^2$$


$$A_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)} = \pm 2r_B \sin \gamma \sin \delta_B / R_{CP\pm}$$

Theoretically clean
but
8-fold ambiguity



$$D_{CP\pm}^0 \equiv (D^0 \pm \bar{D}^0) / \sqrt{2}$$

$B \rightarrow D^0 K$

PRD 73, 051105 - 232 *10⁶ BB pairs 

$$R_{CP+} = 0.90 \pm 0.12(stat.) \pm 0.04(syst.) \quad R_{CP-} = 0.86 \pm 0.10(stat.) \pm 0.05(syst.)$$

$$A_{CP+} = 0.35 \pm 0.13(stat.) \pm 0.04(syst.) \quad A_{CP-} = -0.06 \pm 0.13(stat.) \pm 0.04(syst.)$$

$$x_+ = -0.082 \pm 0.053 \pm 0.018, \quad x_- = 0.102 \pm 0.062 \pm 0.022, \quad r_B^2 = -0.12 \pm 0.08 \pm 0.03$$

$B \rightarrow D^0 K^*$

PRD 73, 071103 - 232 *10⁶ BB pairs

$$R_{CP+} = 1.96 \pm 0.40(stat.) \pm 0.11(syst.) \quad R_{CP-} = 0.65 \pm 0.26(stat.) \pm 0.08(syst.)$$

$$A_{CP+} = 0.08 \pm 0.19(stat.) \pm 0.08(syst.) \quad A_{CP-} = 0.26 \pm 0.40(stat.) \pm 0.12(syst.)$$

$$x_+ = 0.32 \pm 0.18 \pm 0.07, \quad x_- = 0.33 \pm 0.16 \pm 0.06, \quad r_B^2 = 0.30 \pm 0.25$$

$B \rightarrow D^{*0} K$

PRD 71, 031102 - 123 *10⁶ BB pairs

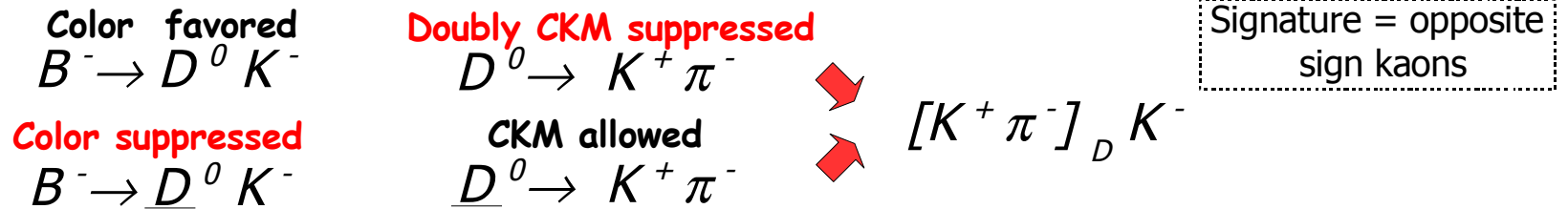
$$R_{CP+} = 1.06 \pm 0.26(stat.) \pm 0.10(syst.) \quad CP \text{ not reconstructed}$$

$$A_{CP+} = 0.10 \pm 0.23(stat.) \pm 0.04(syst.)$$

Atwood-Dunietz-Sony method

Phys. Rev. Lett. 78, 3257 (1997)

Classic two body: Decays into non-CP state, where the color-favoured mode decays via **D**oubly-**C**abibbo **S**uppressed (DCS) channels



Small BF ($\sim 10^{-7}$), but amplitudes are similar \rightarrow expected large CP symmetries
Observables R_{ADS} and A_{ADS} (based on opposite sign and same sign kaon decays):

$$R_{ADS} = \frac{Br([K^+ \pi^-]K^-) + Br([K^- \pi^+]K^+)}{Br([K^- \pi^+]K^-) + Br([K^+ \pi^-]K^+)} = r_D^2 + r_B^2 + 2r_B r_D \cos(\delta_D + \delta_B) \cos \gamma$$

$$A_{ADS} = \frac{Br([K^+ \pi^-]K^-) - Br([K^- \pi^+]K^+)}{Br([K^+ \pi^-]K^-) + Br([K^- \pi^+]K^+)} = 2r_B r_D \sin(\delta_D + \delta_B) \sin \gamma / R_{ADS}$$

with unknown parameters: r_B , δ and γ

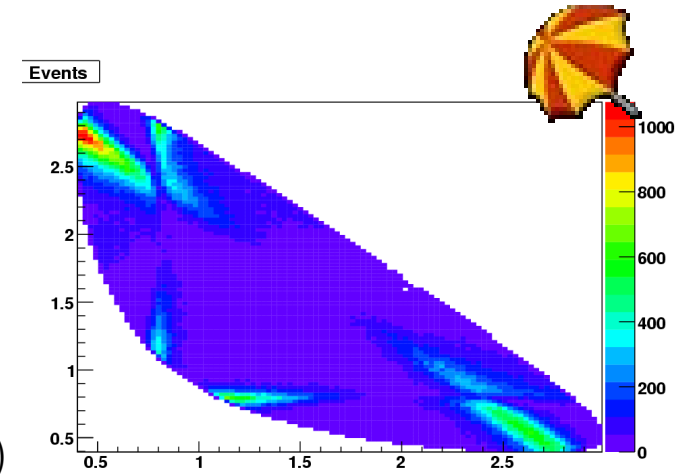
input : $r_D = \left| \frac{A(D^0 \rightarrow K^+ \pi^-)}{A(D^0 \rightarrow K^- \pi^+)} \right| = 0.060 \pm 0.003$ ($D^{*+} \rightarrow D^0 (K\pi) \pi^+$ decays - - PRL91,171801(2003))



D(*)⁰K: PRD 72, 032004 - 232 *10⁶ BB pairs
D⁰K*: PRD 72, 071104 - 232 *10⁶ BB pairs 3

ADS $B \rightarrow D^0 [K^+ \pi^- \pi^0] K$

Multi-body: similar to previous analysis with $f = K^+ \pi^- \pi^0$.
 Complication for γ extraction from $|A_D|$, δ_D variation across the D^0 Dalitz plane:



$$R_{ADS} = \frac{\Gamma(B^+ \rightarrow [K^- \pi^+ \pi^0]_{D^0} K^+) + \Gamma(B^+ \rightarrow [K^- \pi^+ \pi^0]_{\bar{D}^0} K^+) + \Gamma(B^- \rightarrow [K^+ \pi^- \pi^0]_{D^0} K^-) + \Gamma(B^- \rightarrow [K^+ \pi^- \pi^0]_{\bar{D}^0} K^-)}{\Gamma(B^+ \rightarrow [K^+ \pi^- \pi^0]_{D^0} K^+) + \Gamma(B^+ \rightarrow [K^+ \pi^- \pi^0]_{\bar{D}^0} K^+) + \Gamma(B^- \rightarrow [K^- \pi^+ \pi^0]_{D^0} K^-) + \Gamma(B^- \rightarrow [K^- \pi^+ \pi^0]_{\bar{D}^0} K^-)}$$

we can express R_{ADS} as

$$R_{ADS} = \int \left| r_B e^{i(\delta_B + \gamma)} + r_D e^{i\delta_D} \right|^2 dm_{K\pi} dm_{K\pi^0} = r_B^2 + r_D^2 + 2 r_B r_D C \cos \gamma$$

$$r_B^{(*)} = \frac{|A(B^- \rightarrow \underline{D}^{(*)0} K^-)|}{|A(B^- \rightarrow D^{(*)0} K^-)|} \sim 0.1 - 0.2$$

$$r_D^2 \equiv \Gamma(D^0 \rightarrow K^+ \pi^- \pi^0) / \Gamma(D^0 \rightarrow K^- \pi^+ \pi^0) = (0.214 \pm 0.011)\% \quad (\text{BaBar, preliminary})$$

$$C = \frac{1}{r_D BR(D^0 \rightarrow K^- \pi^+ \pi^0)} \int A(D^0 \rightarrow K^- \pi^+ \pi^0) A(D^0 \rightarrow K^+ \pi^- \pi^0) \cos \Delta dm_{12} dm_{13}$$

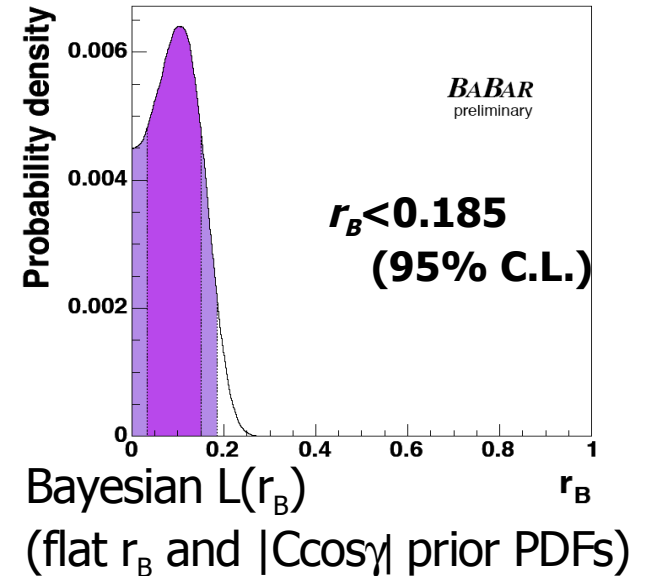
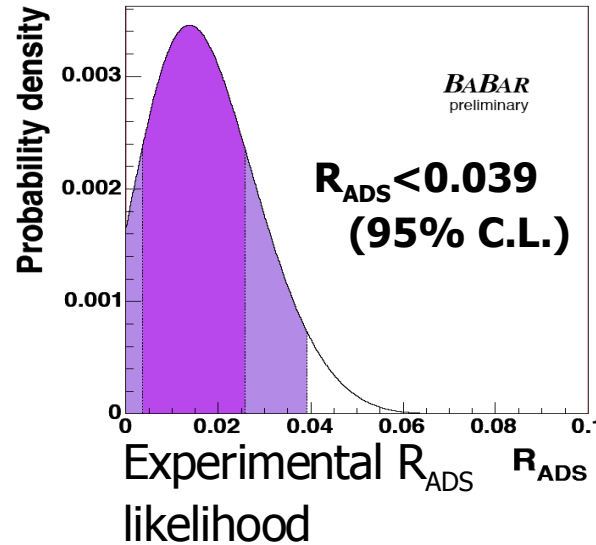
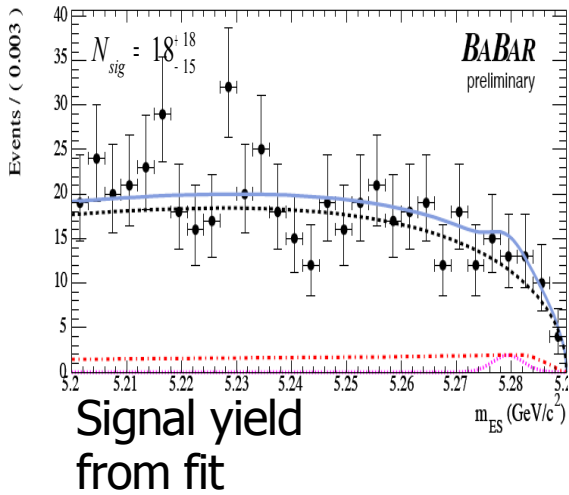


R_{ADS} and r_B distribution extraction

A priori probability is Gaussian consistent with $r_D^2 = (0.214 \pm 0.011)\%$ (BaBar, prel.)

$$R_{ADS} = r_B^2 + r_D^2 + 2 r_B r_D C \cos \gamma$$

Distributed flat in $[-1,1]$ and $[0,1]$



wrt $f=K^+\pi^-$:
more background
but smaller r_D

→ $R_{ADS} < 0.039$ using $|C \cos \gamma| \leq 1$
 $r_B < 0.185$ 95% C.L.

ADS averages

$D^{*0}K$: PRD 72, 032004 - $232 \cdot 10^6$ BB pairs
 D^0K^* : PRD 72, 071104 - $232 \cdot 10^6$ BB pairs
 hep-ex/0607065 - $226 \cdot 10^6$ BB pairs

Comparison with other analyses

R_{ADS} Averages



Classical ADS

Dalitz ADS

$B \rightarrow DK$

$R_{ADS} < 0.029$ 90% C.L.
 $r_B < 0.23$ 90% C.L.

$B \rightarrow [D\pi]_{D^*} K$

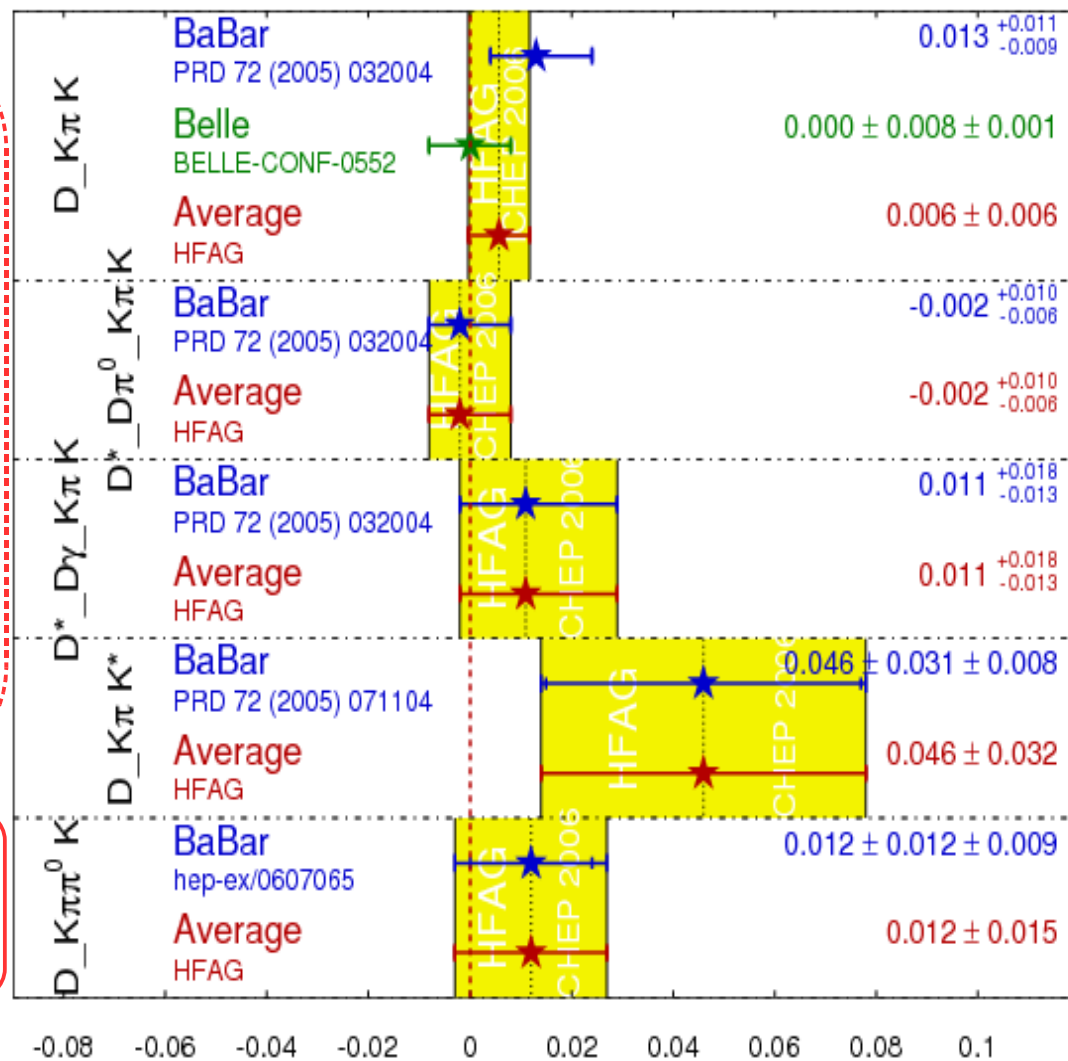
$R_{ADS} < 0.023$ ($D^{*0} \rightarrow D^0 \pi^0$)
 < 0.045 ($D^{*0} \rightarrow D^0 \gamma$) 90% C.L.
 $r_B < 0.16$ 90% C.L.

$B \rightarrow [K^+\pi^-]_D K^{*-}$

$R_{ADS} = 0.046 \pm 0.032$ 1σ
 $r_B = 0.20 \pm 0.14$ 1σ

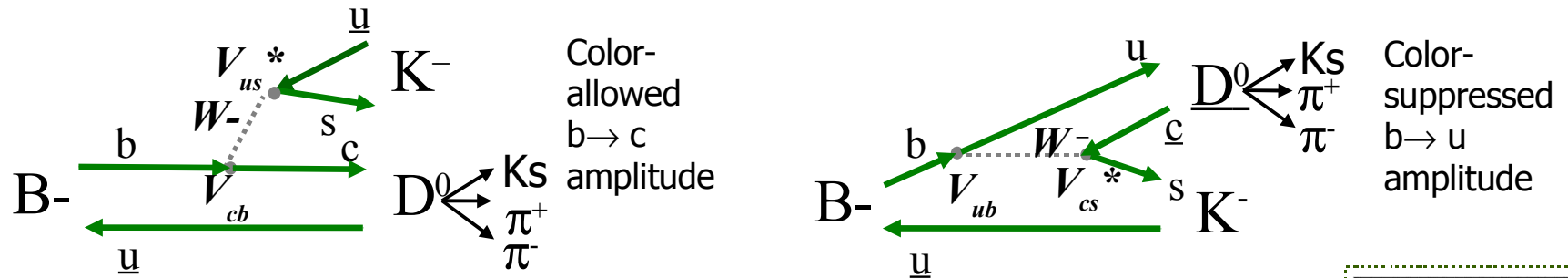
$B \rightarrow [K+\pi-\pi^0] DK^-$

$R_{ADS} < 0.039$ 95% C.L.
 $r_B < 0.185$ 95% C.L.



Giri-Grossman-Soffer-Zupan (Dalitz) method

D^0, \underline{D}^0 decay to 3 body final state $K_S \pi^+ \pi^-$



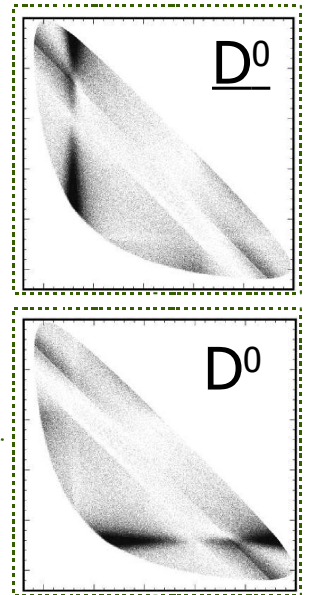
The interference is a function of the Dalitz plot point :

$$B^- : M_-(m_-^2, m_+^2) = \left| A(B^- \rightarrow D^0 K^-) \left[f(m_-^2, m_+^2) + r_B e^{i\delta_B} e^{-i\gamma} f(m_+^2, m_-^2) \right] \right|$$

$$B^+ : M_+(m_-^2, m_+^2) = \left| A(B^+ \rightarrow \bar{D}^0 K^+) \left[f(m_+^2, m_-^2) + r_B e^{i\delta_B} e^{+i\gamma} f(m_-^2, m_+^2) \right] \right|$$

$$m_-^2 = m(K_S^0 \pi^-)^2$$

$$m_+^2 = m(K_S^0 \pi^+)^2$$



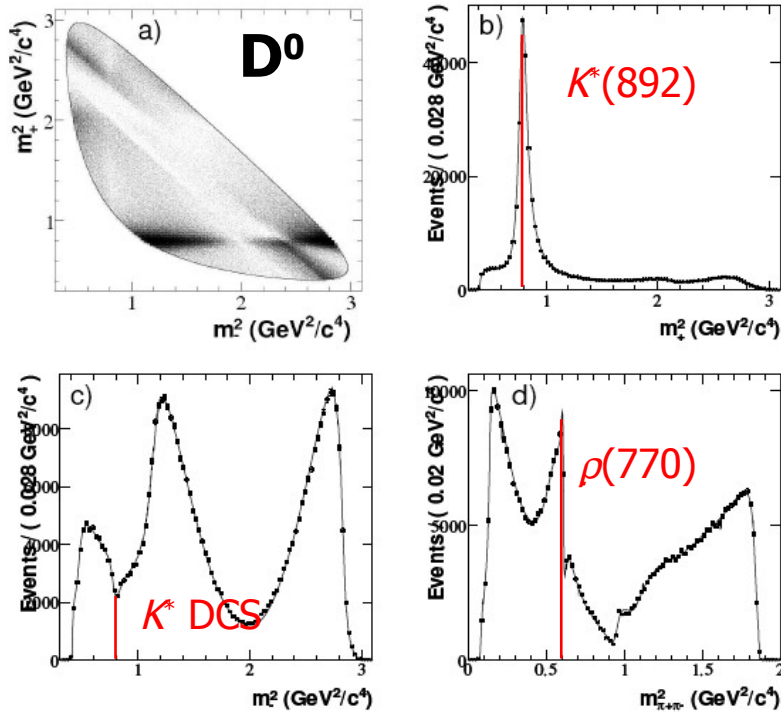
pros: Only Two-fold ambiguity $(\delta_B, \gamma) \rightarrow (\delta_B + \pi, \gamma + \pi)$

significantly larger statistical power $\text{Br}(D^0 \rightarrow K_S \pi^+ \pi^-) \sim 10 * \text{Br}(D^0 \rightarrow f_{CP})$



GGSZ $D^0 \rightarrow K_S \pi\pi$ method

$f(m_-^2, m_+^2)$ extracted from unbinned maximum likelihood fit to tagged D^0
 (from $D^{(*)+} \rightarrow D^0 \pi^+$ decays, $\sim 390k$ evts @97.7% purity).



Isobar model (\equiv coherent Σ of **Breit-Wigner (BW)** amplitudes)
 . 3-body D^0 decays proceed mostly via 2 -body decays
 .. $A_D = 16$ distinct resonances + 1 NR term
 ... Not so good for $\pi\pi$ S-wave
 $\sigma(500) / \sigma'(1000)$ added to describe reasonably well the data

Component	$Re\{a_r e^{i\phi_r}\}$	$Im\{a_r e^{i\phi_r}\}$	Fit fraction (%)
$K^*(892)^-$	-1.223 ± 0.011	1.3461 ± 0.0096	58.1
$K_0^*(1430)^-$	-1.698 ± 0.022	-0.576 ± 0.024	6.7
$K_2^*(1430)^-$	-0.834 ± 0.021	0.931 ± 0.022	3.6
$K^*(1410)^-$	-0.248 ± 0.038	-0.108 ± 0.031	0.1
$K^*(1680)^-$	-1.285 ± 0.014	0.205 ± 0.013	0.6
$K^*(892)^+$	0.0997 ± 0.0036	-0.1271 ± 0.0034	0.5
$K_0^*(1430)^+$	-0.027 ± 0.016	-0.076 ± 0.017	0.0
$K_2^*(1430)^+$	0.019 ± 0.017	0.177 ± 0.018	0.1
$\rho(770)$	1	0	21.6
$\omega(782)$	-0.02194 ± 0.00099	0.03942 ± 0.00066	0.7
$f_2(1270)$	-0.699 ± 0.018	0.387 ± 0.018	2.1
$\rho(1450)$	0.253 ± 0.038	0.036 ± 0.055	0.1
Non-resonant	-0.99 ± 0.19	3.82 ± 0.13	8.5
$f_0(980)$	0.4465 ± 0.0057	0.2572 ± 0.0081	6.4
$f_0(1370)$	0.95 ± 0.11	-1.619 ± 0.011	2.0
σ	1.28 ± 0.02	0.273 ± 0.024	7.6
σ'	0.290 ± 0.010	-0.0655 ± 0.0098	0.9

K-matrix Model *

- . include $\pi\pi$ S-wave terms
- .. unitarity
- ... χ^2 / dof similar to BW model



GGSZ $D^0 \rightarrow K_S \pi\pi$ method

Dalitz model systematic uncertainties:

- . introduce 8 alternative models
- .. generate high statistics toy MC (x100 data statistics) experiments according nominal (BW) model
- ... fit with both nominal & alternative model
- take the maximum of the absolute value of the differences

$\pi\pi$ S-wave: Use K-matrix $\pi\pi$ S-wave model instead of the nominal BW model

$\pi\pi$ P-wave: Change $\rho(770)$ parameters according to PDG
 Replace Gounaris-Sakurai by regular BW
 Remove $\rho(1450)$

$\pi\pi$ D-wave: Zemach Tensor as the Spin Factor

$K\pi$ S-wave: Allow $K^*_0(1430)$ mass and width to be determined from the fit
 Use LASS parameterization with LASS parameters

$K\pi$ P-wave: Use $B \rightarrow J/\psi K_S \pi^+$ as control sample for $K^*(892)$ parameters
 Allow $K^*(892)$ mass and width to be determined from the fit

$K\pi$ D-wave: Zemach Tensor as the Spin Factor

Blatt-Weiskopf penetration factors

No running width

Dalitz plot normalization



GGSZ $D^0 \rightarrow K_S \pi\pi$ method

Cartesian Coordinates:

From previous studies, parameters (r_B, γ, δ) badly behave statistically

No sensitivity to γ for $r_B < 0.1$ (+underestimated errors on γ and δ)

→ Fit 4 cartesian coordinates (x_{\pm}, y_{\pm})

$$x_{\pm} = \text{Re} (r_B e^{i(\delta \pm \gamma)}) \quad y_{\pm} = \text{Im} (r_B e^{i(\delta \pm \gamma)})$$

- . Gaussian Errors on x, y (no unphysical zone)
- .. (x^+, y^+) , (x^-, y^-) uncorrelated
- ... Unbiased results $\forall r_B$
- Easier to combine different results

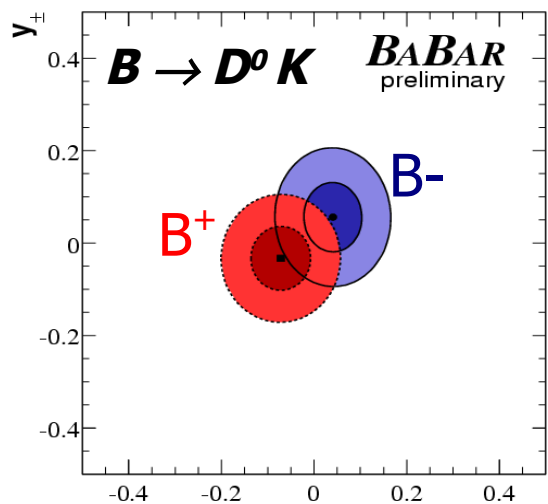
Note: GLW results also sensitive to x_{\pm} and through the relations

$$x_{\pm} = \frac{R_{CP^+}(1 \mp A_{CP^+}) - R_{CP^-}(1 \mp A_{CP^-})}{4}$$

$$r_B^2 = \frac{R_{CP^+} + R_{CP^-} - 2}{2}$$



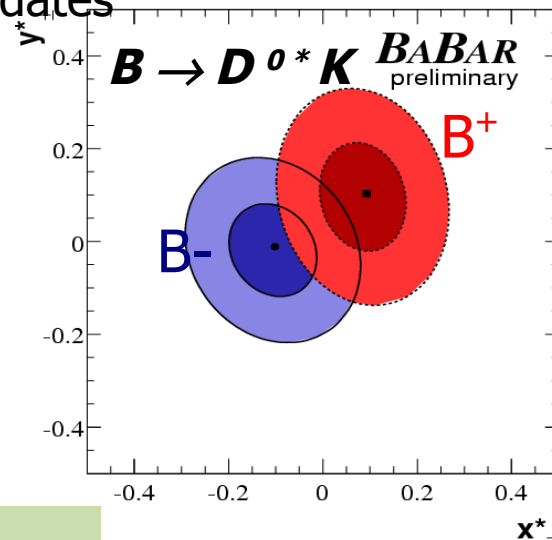
GGSZ $D^0 \rightarrow K_S \pi \pi$ method



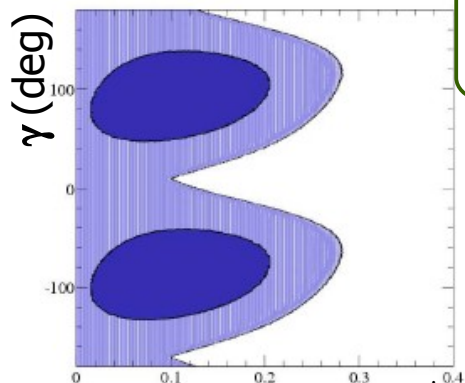
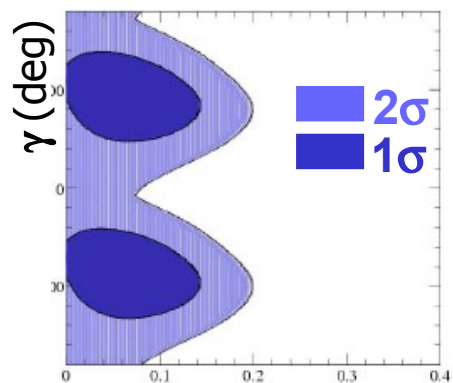
• Dalitz distribution of selected B[±] candidates

•• Fitted values of $x_{\pm}^{(*)}, y_{\pm}^{(*)}$

x_-	$0.041 \pm 0.059 \pm 0.018 \pm 0.011$
y_-	$0.056 \pm 0.071 \pm 0.007 \pm 0.023$
x_+	$-0.072 \pm 0.056 \pm 0.014 \pm 0.029$
y_+	$-0.033 \pm 0.066 \pm 0.007 \pm 0.018$
x_-^*	$-0.106 \pm 0.091 \pm 0.020 \pm 0.009$
y_-^*	$-0.019 \pm 0.096 \pm 0.022 \pm 0.016$
x_+^*	$0.084 \pm 0.088 \pm 0.015 \pm 0.018$
y_+^*	$0.096 \pm 0.111 \pm 0.032 \pm 0.017$



x_{\pm} frequentist [Neyman] approach
 used to build 5D confidence level on $(\gamma, r_B, \delta_B, r_B^*, \delta_B^*)$
 1 σ and 2 σ projection contours on $r_B^{(*)}, \gamma$



$$\gamma \text{ mod } 180^\circ = (92 \pm 41 \pm 11 \pm 12)^\circ$$

Stat Syst Dalitz

$$r_B < 0.142 \quad (r_B < 0.198)$$

$$0.016 < r_B^* < 0.206 \quad (r_B^* < 0.142)$$

1 σ

(2 σ)

Virginia Azzolini r_B

r_B^*

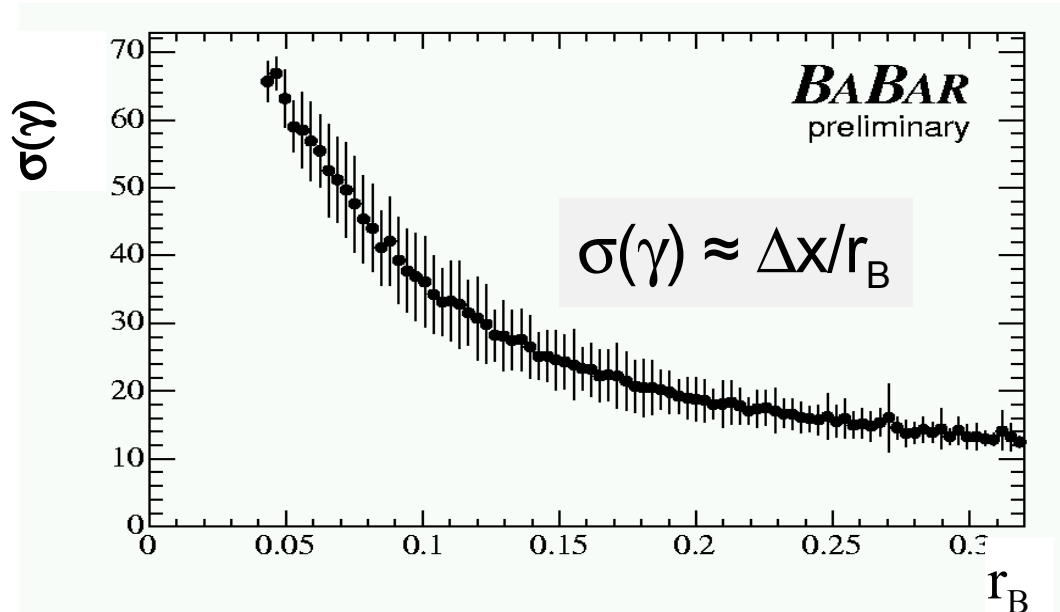
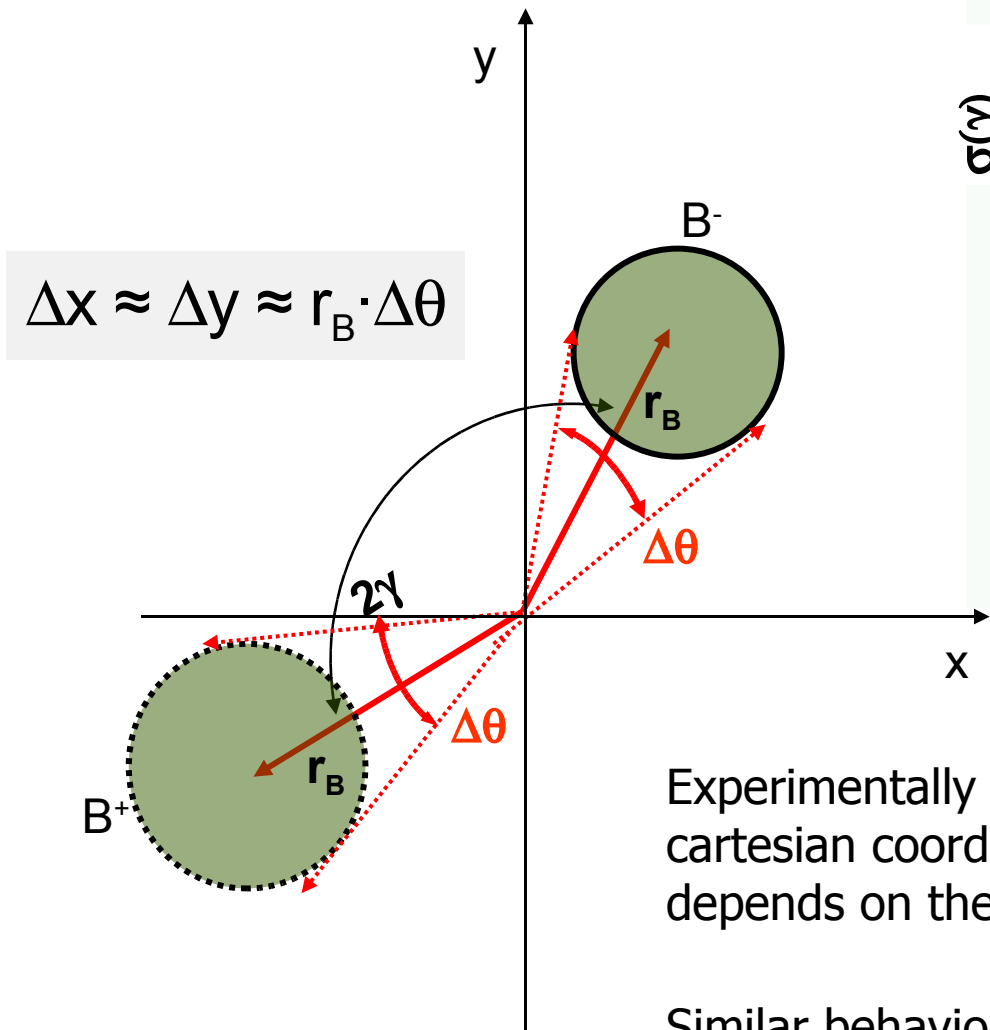


GGSZ $D^0 \rightarrow K_S \pi \pi$ method

Comments on the results:

Better precision on x,y wrt to Belle,

σ_γ worse due to smaller measured central value of $r_B^{(*)}$



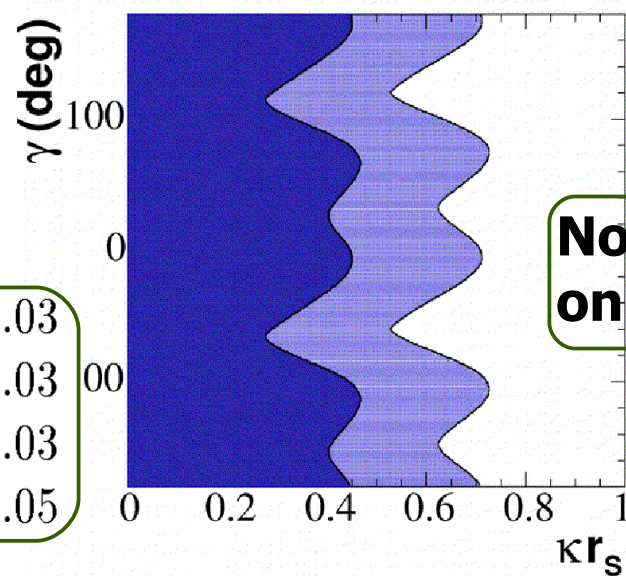
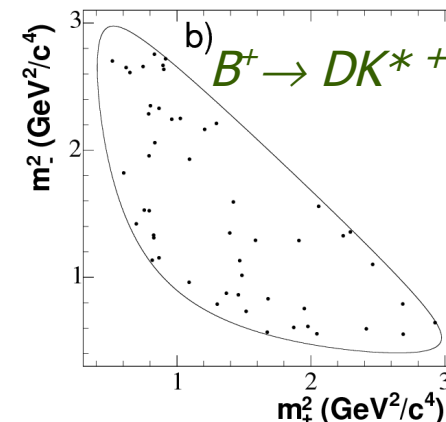
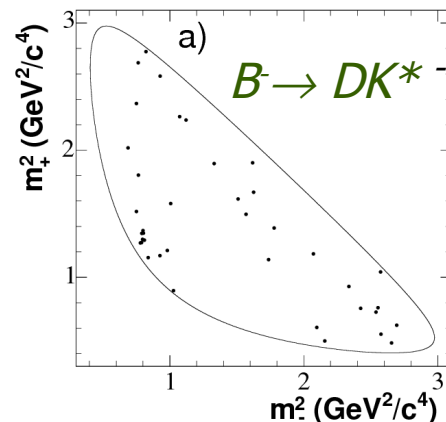
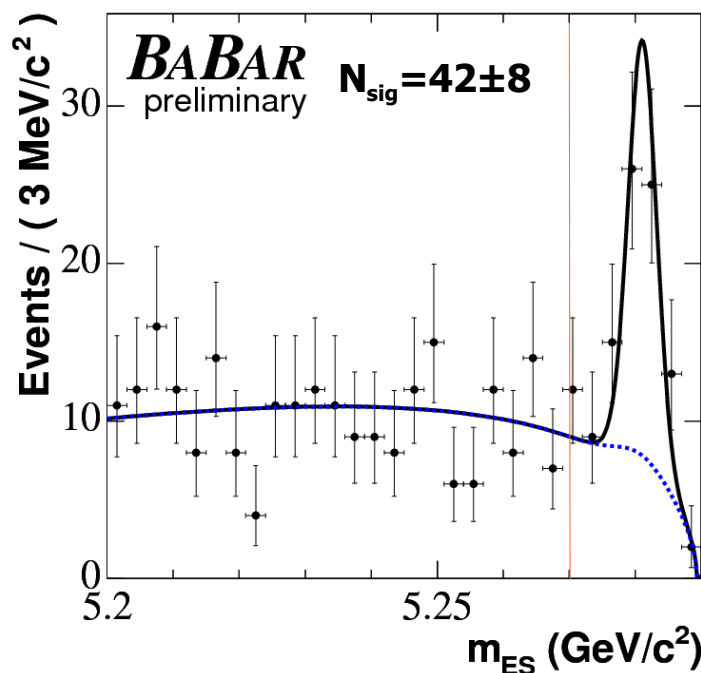
Experimentally we can improve the measurement of the CP cartesian coordinates **but** the improvement on error of γ depends on the true value of the r_B parameter.

Similar behavior for statistical and systematic error.

GGSZ $B \rightarrow D^0 K^* (K^* \rightarrow K_S \pi), D^0 \rightarrow K_S \pi \pi$ method



Analogous to previous analysis, one additional fit parameter k to take into account non- resonant $B \rightarrow D^0 K_S \pi$ background and r_B, δ_B variation across B Dalitz plot.



$x_{s-} \equiv \kappa r_s \cos(\delta_s - \gamma)$	$-0.20 \pm 0.20 \pm 0.11 \pm 0.03$
$y_{s-} \equiv \kappa r_s \sin(\delta_s - \gamma)$	$0.26 \pm 0.30 \pm 0.16 \pm 0.03$
$x_{s+} \equiv \kappa r_s \cos(\delta_s + \gamma)$	$-0.07 \pm 0.23 \pm 0.13 \pm 0.03$
$y_{s+} \equiv \kappa r_s \sin(\delta_s + \gamma)$	$-0.01 \pm 0.32 \pm 0.18 \pm 0.05$

GLW+ADS+GGSZ + $\sin(2\beta+\gamma)$: present and prospect

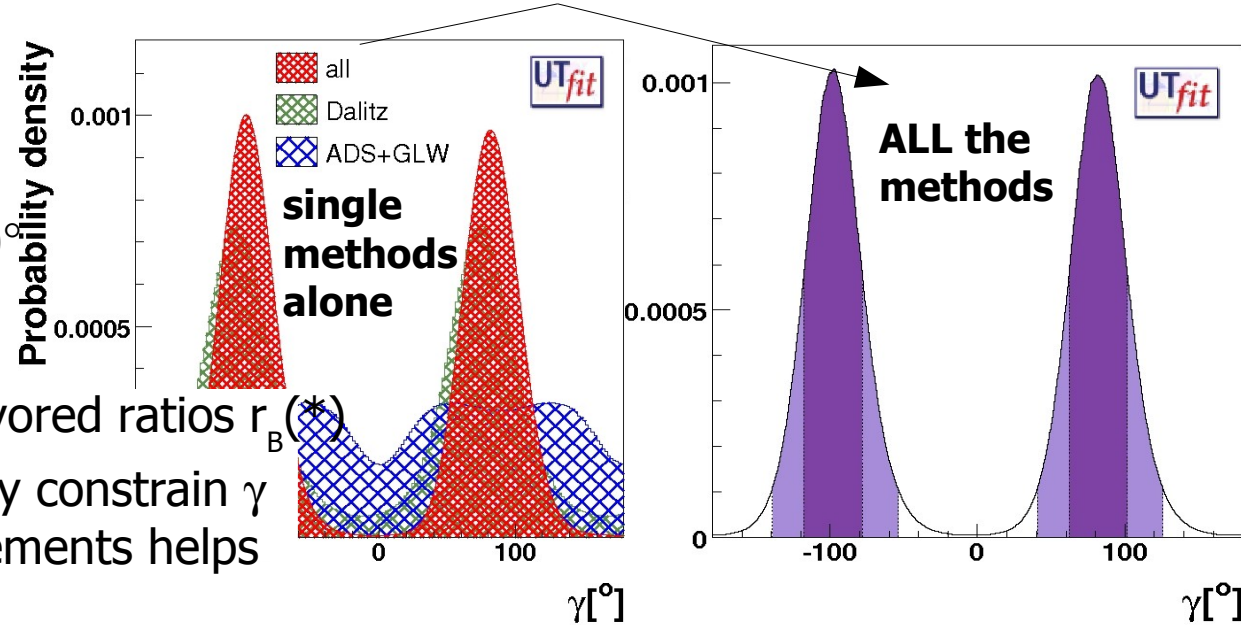
GGSZ method:

- . powerful tool:
- .. the golden mode for γ

$$\gamma \bmod 180^\circ = (92 \pm 41 \pm 11 \pm 12)^\circ$$

GLW & ADS methods:

- . limits on the suppressed-to-favored ratios r_B (*)
- .. more statistic needed to really constrain γ
- ... combining different measurements helps



combination of all the measured modes:

$$\gamma_{\text{GLW,ADS,GGSZ}} = 82 \pm 20 \text{ ([41,126] @ 95\% Prob.) [UTfit]}$$

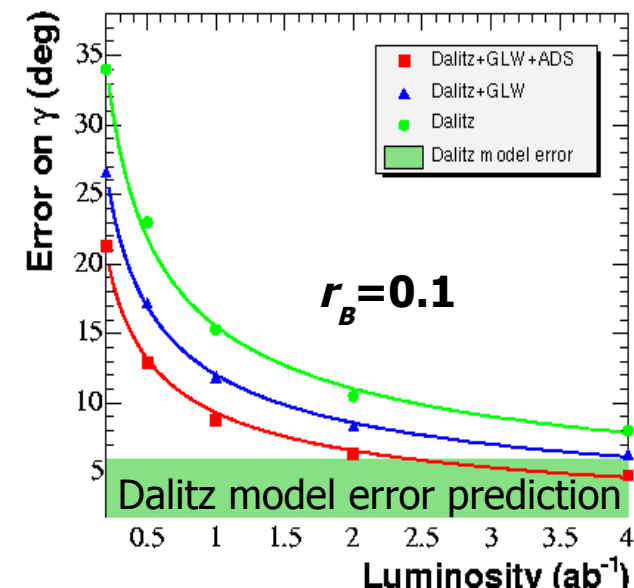
$$\gamma_{\text{GLW,ADS,GGSZ}} = -98 \pm 20 \text{ ([-139,-33] @ 95\% Prob.) [UTfit]}$$

still crucial is **combining** methods & decay modes along with **more statistics**



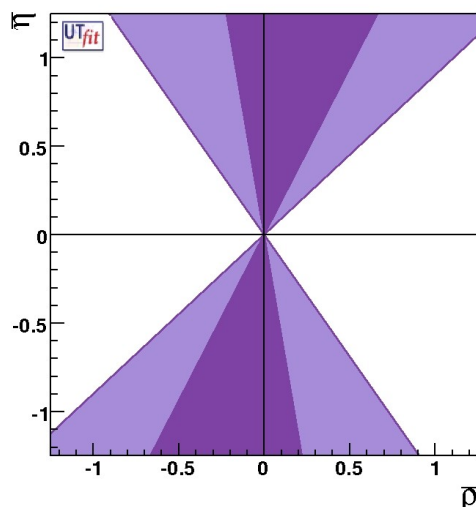
If $r_B \geq 0.1$ at 1 ab^{-1} γ will be know with a

precision close to 10°



Measurement of the UT angle γ at BaBar

Virginia Azzolini



Outline:

Measurements of γ using $B^\pm \rightarrow D^{(*)}K^{(*)\pm}$

GLW Method

ADS Method

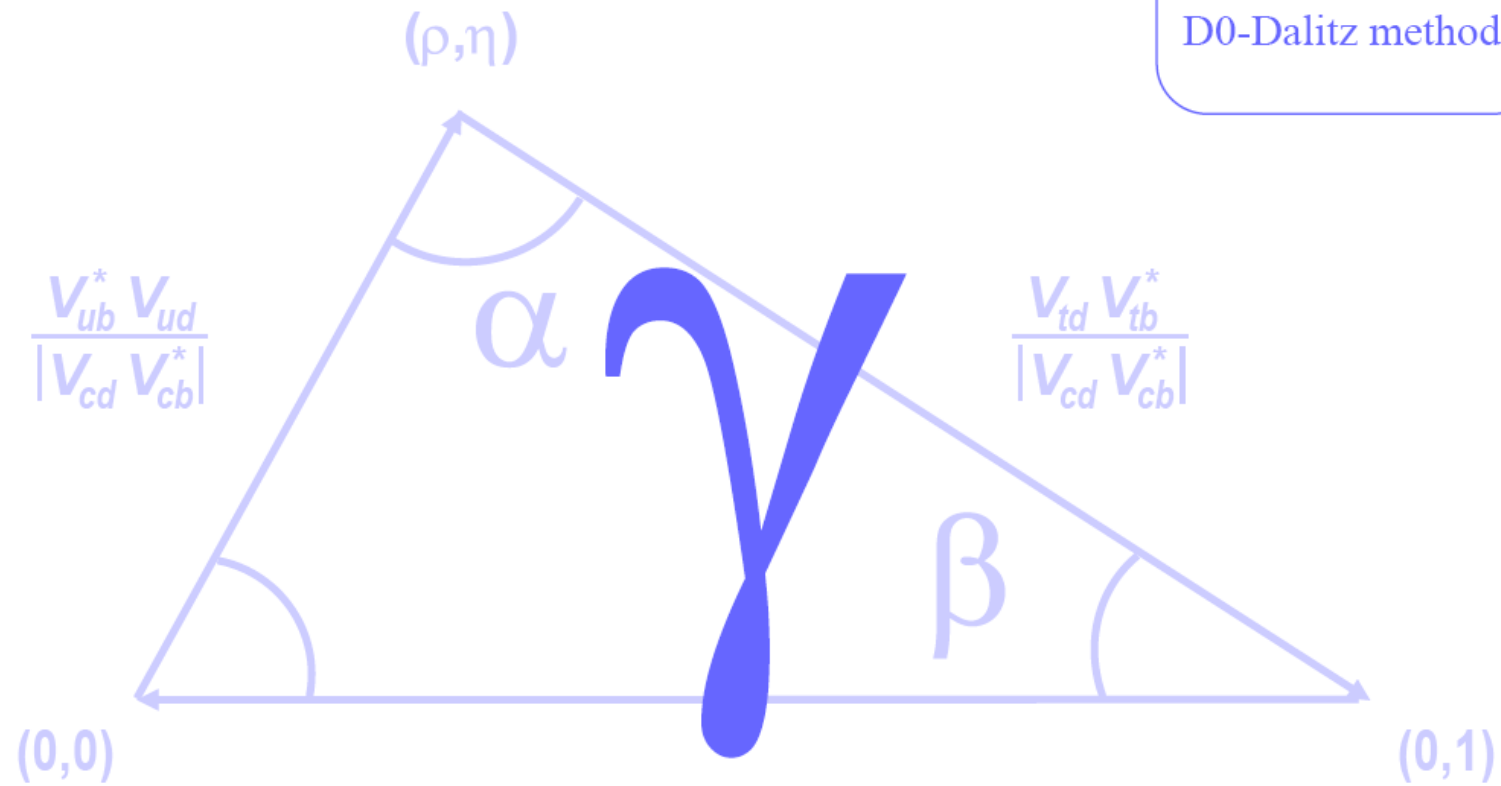
D^0 Dalitz Method (GGSZ)



backup

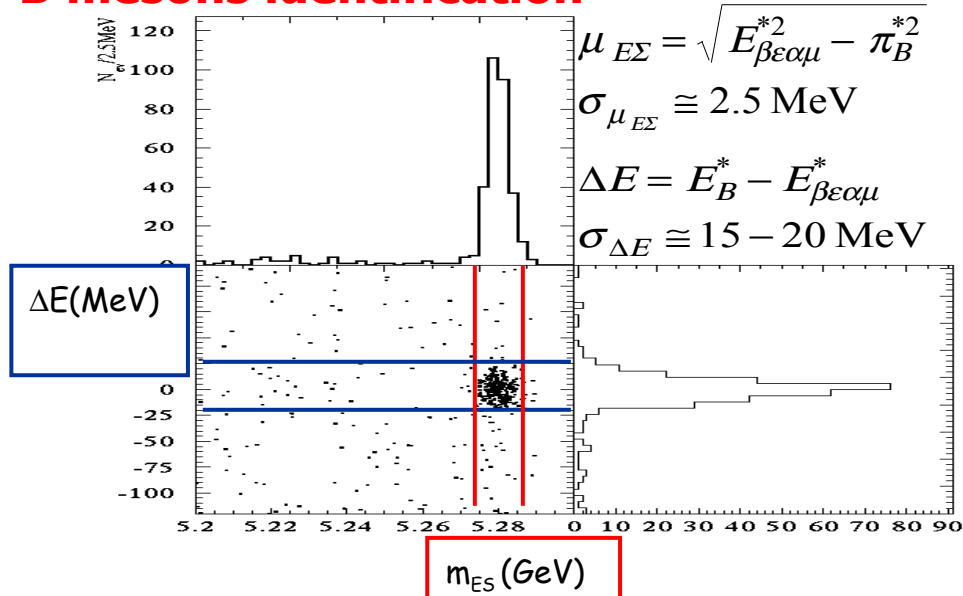
$$B^\pm \rightarrow D^{(*)}K^{(*)}$$

GLW, ADS and
D0-Dalitz methods

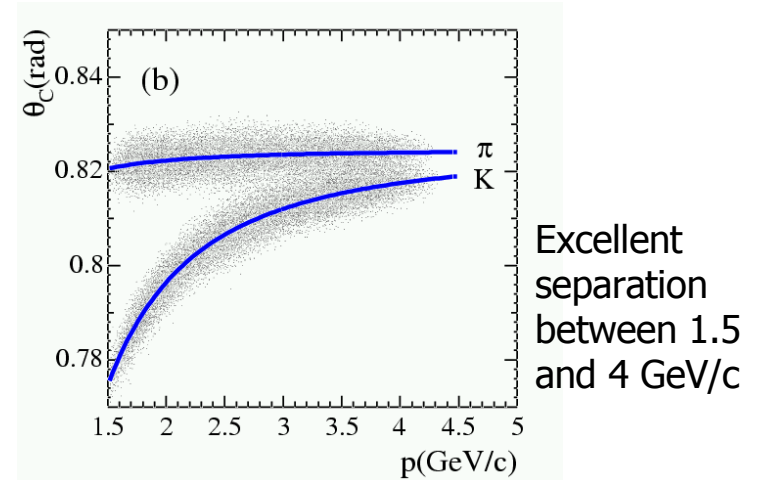


Selection of signal events

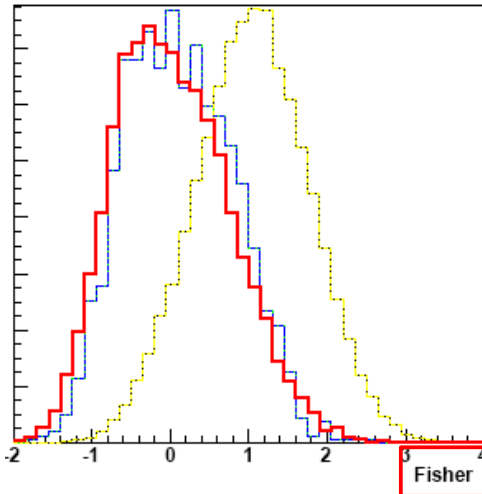
B mesons identification



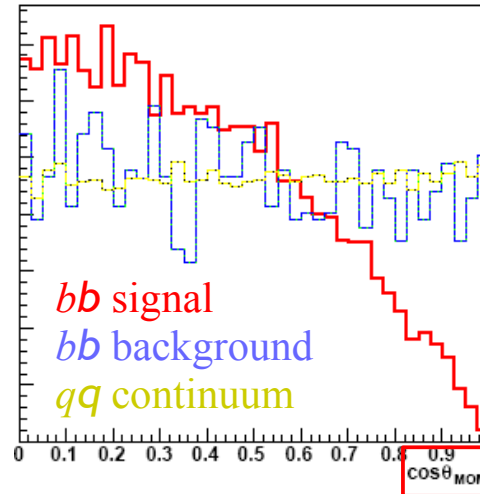
K/ π : Cherenkov angle



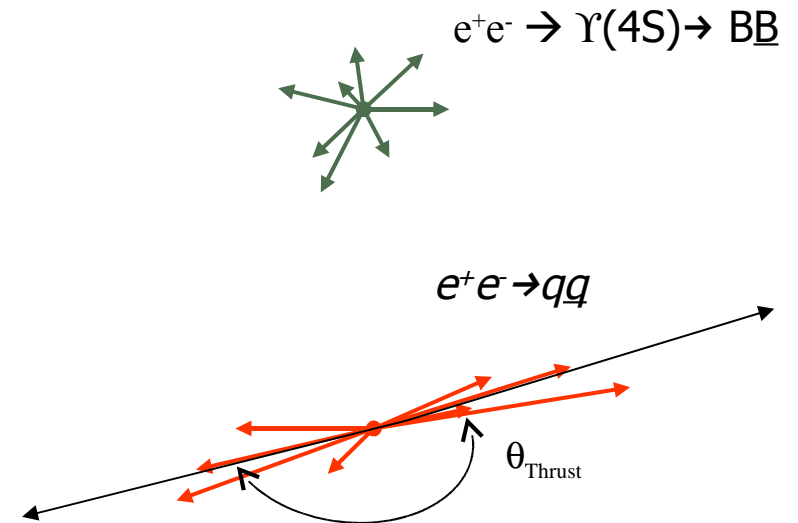
Variables that distinguish spherical B events from jet-like continuum.



Variables that distinguish $\Upsilon(4S) \rightarrow bb$ from $e^+e^- \rightarrow qq$



Thrust angle defines the jet-like event



Combinatorial $e^+e^- \rightarrow qq$ bkg suppression

Gronau-London-Wyler method

Phys. Lett. B253, 483; Phys. Lett. B265, 172 (1991)

D⁰K : PRD 73, 051105 - 232 *10⁶ BB pairs
 D⁰K* : PRD 73, 071103 - 232 *10⁶ BB pairs
 D*⁰K : PRD 71, 031102 - 123 *10⁶ BB pairs



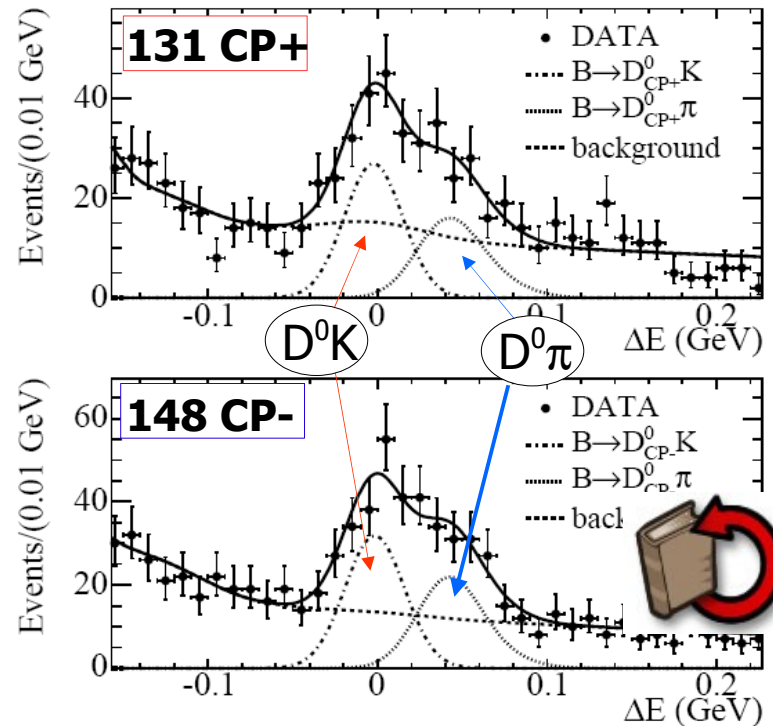
- Reconstruct D meson in CP-eigenstates (accessible to D⁰ and \underline{D}^0)
 even (CP = +1 $\pi^+\pi^-, K^+K^-$) & odd (CP = -1 $K_s^0\pi^0, K_s^0\phi, K_s^0\omega$)
- Measure 4 observables $R_{CP\pm}, A_{CP\pm}$ (formulae for D⁰K):

$$R_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{2\Gamma(B^- \rightarrow D^0 K^-)} = 1 \pm 2r_B \cos \gamma \cos \delta_B + r_B^2$$

$$A_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)} = \pm 2r_B \sin \gamma \sin \delta_B / R_{CP\pm}$$

Theoretically clean
 but
 8-fold ambiguity

$$D_{CP\pm}^0 \equiv (D^0 \pm \bar{D}^0) / \sqrt{2}$$



3 ind. observables
 3 unknowns:

γ
 δ = strong phase diff.
 $A(B^- \rightarrow \underline{D}^0 K^-)$ &
 $A(B^- \rightarrow D^0 K^-)$

$$r_B = \frac{|A(B^- \rightarrow \underline{D}^0 K^-)|}{|A(B^- \rightarrow D^0 K^-)|}$$



GLW : results



$B \rightarrow D^0 K$

PRD 73, 051105 232*10⁶ BB

$$R_{CP^+} = 0.90 \pm 0.12(\text{stat.}) \pm 0.04(\text{syst.}) \quad R_{CP^-} = 0.86 \pm 0.10(\text{stat.}) \pm 0.05(\text{syst.})$$

$$A_{CP^+} = 0.35 \pm 0.13(\text{stat.}) \pm 0.04(\text{syst.}) \quad A_{CP^-} = -0.06 \pm 0.13(\text{stat.}) \pm 0.04(\text{syst.})$$

$B \rightarrow D^0 K^*$

PRD 73, 071103 232*10⁶ BB

$$R_{CP^+} = 1.96 \pm 0.40(\text{stat.}) \pm 0.11(\text{syst.}) \quad R_{CP^-} = 0.65 \pm 0.26(\text{stat.}) \pm 0.08(\text{syst.})$$

$$A_{CP^+} = 0.08 \pm 0.19(\text{stat.}) \pm 0.08(\text{syst.}) \quad A_{CP^-} = 0.26 \pm 0.40(\text{stat.}) \pm 0.12(\text{syst.})$$

$B \rightarrow D^{*0} K$

PRD 71, 031102 123*10⁶ BB

$$R_{CP^+} = 1.06 \pm 0.26(\text{stat.}) \pm 0.10(\text{syst.}) \quad CP \text{ not reconstructed}$$

$$A_{CP^+} = \tilde{0}.10 \pm 0.23(\text{stat.}) \pm 0.04(\text{syst.})$$



- . With current statistics, these **DO NOT** constrain (alone) γ/ϕ_3 nor $r_B^{(*)}$
- .. however, they provide competitive measurements of the cartesian coordinates x_{\pm} ,

used by Dalitz, through the relations

$$x_{\pm} = \frac{R_{CP^+}(1 \mp A_{CP^+}) - R_{CP^-}(1 \mp A_{CP^-})}{4} \quad r_B^2 = \frac{R_{CP^+} + R_{CP^-} - 2}{2}$$

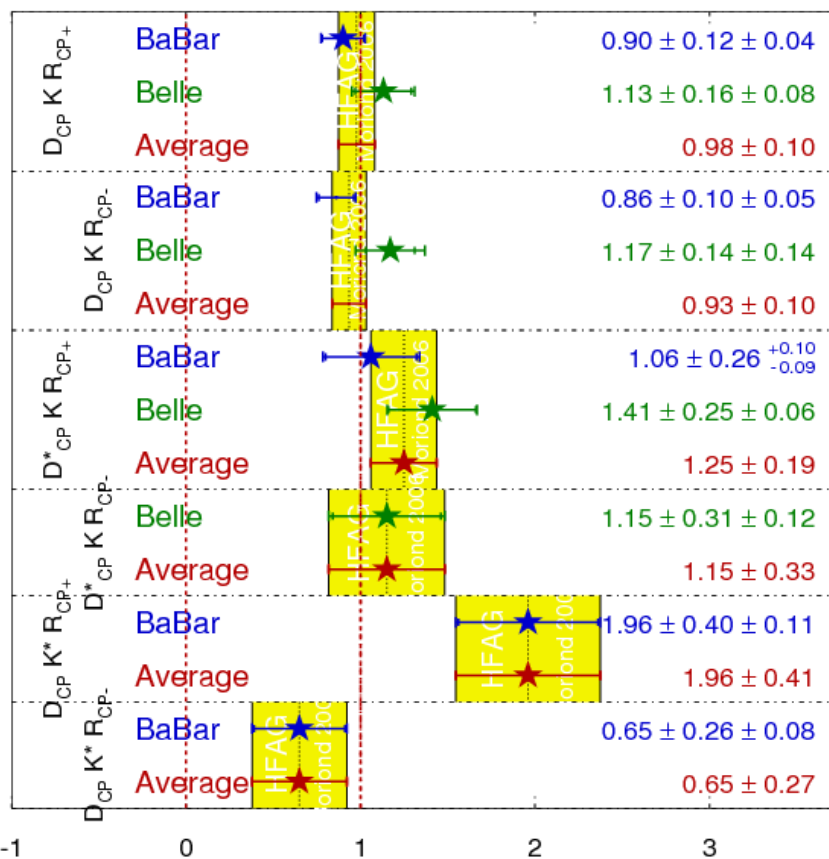
$$x_+ = -0.082 \pm 0.053 \pm 0.018, \quad x_- = 0.102 \pm 0.062 \pm 0.022, \quad r_B^2 = -0.12 \pm 0.08 \pm 0.03 \quad B \rightarrow D^0 K$$

$$x_+ = 0.32 \pm 0.18 \pm 0.07, \quad x_- = 0.33 \pm 0.16 \pm 0.06, \quad r_B^2 = 0.30 \pm 0.25 \quad B \rightarrow D^0 K^*$$

GLW averages

R_{CP} Averages

HFAG
Moriond 2006
PRELIMINARY



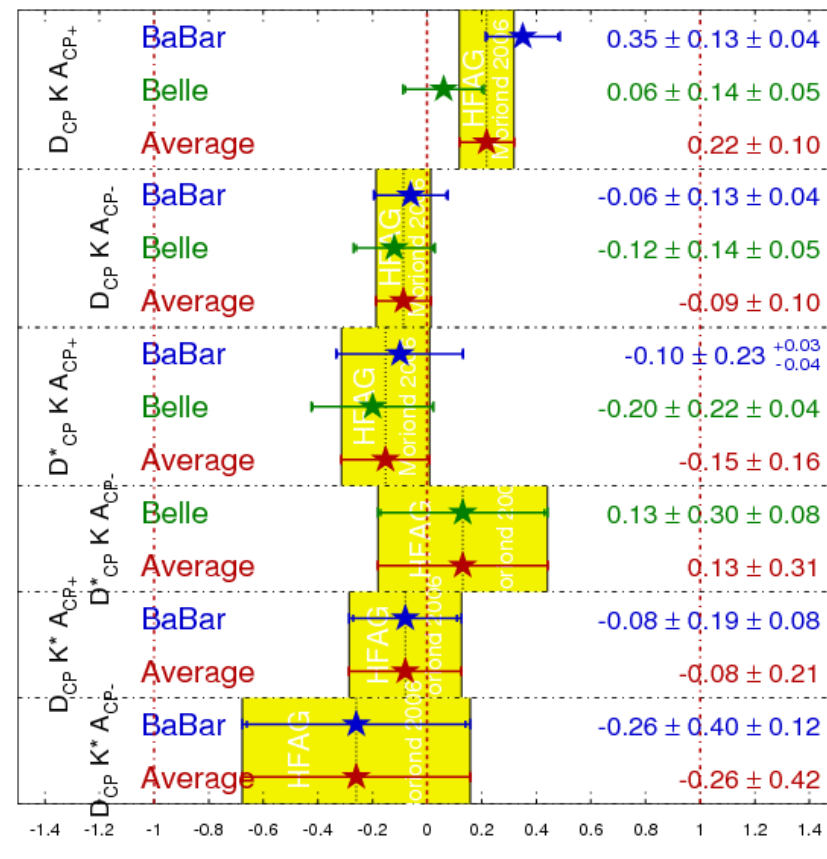
$D_{CP} K$

$D_{CP}^* K$

$D_{CP} K^*$

A_{CP} Averages

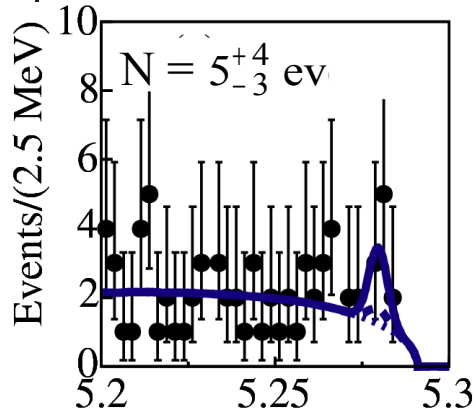
HFAG
Moriond 2006
PRELIMINARY



Implications for r_B and γ see body of the talk

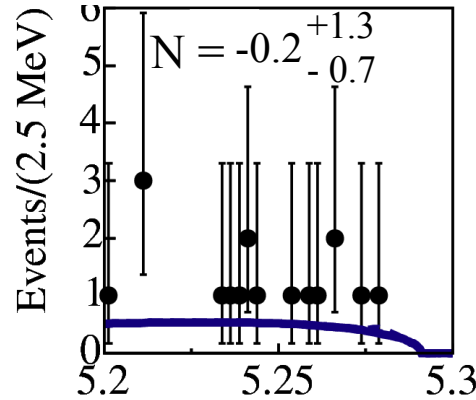
ADS results

$D^{(*)0}K$: PRD 72, 032004 - 232 *10⁶ BB pairs
 D^0K : PRD 72, 071104 - 232 *10⁶ BB pairs



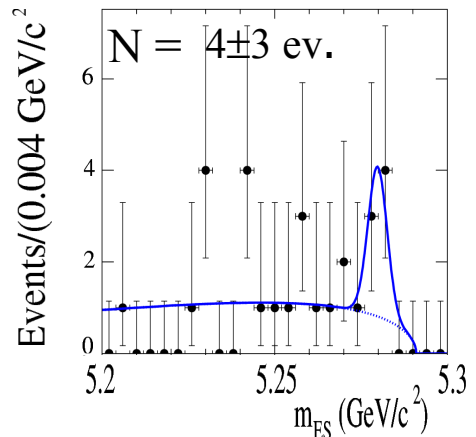
$B \rightarrow DK$

$R_{ADS} < 0.029$ 90% C.L.



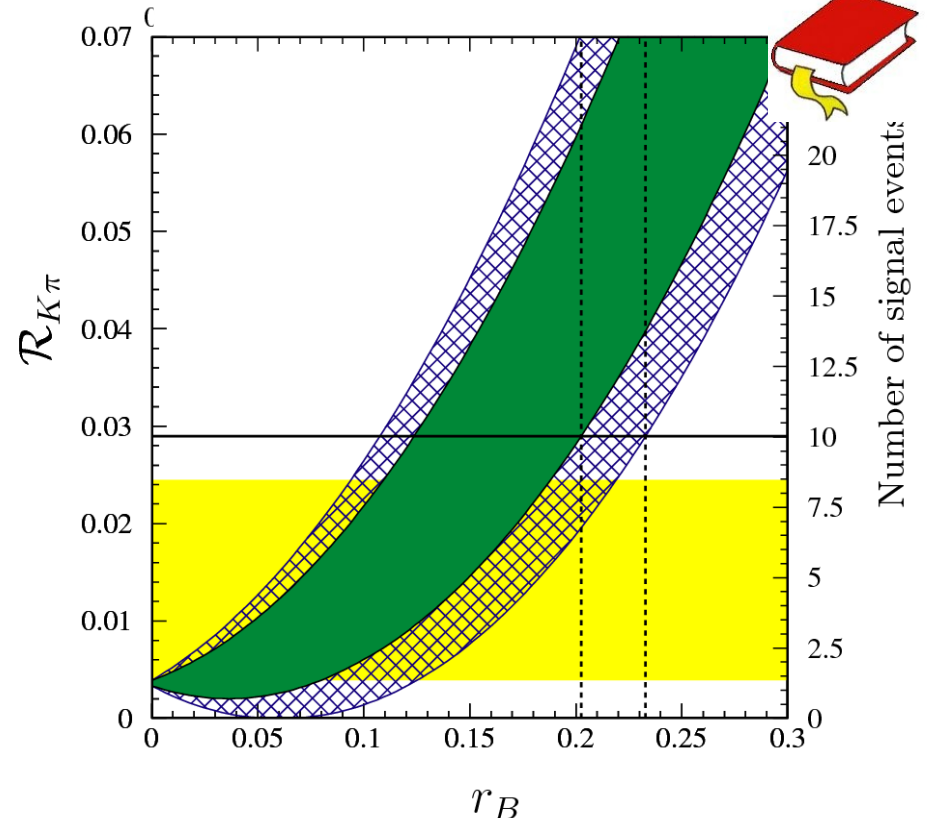
$B \rightarrow [D\pi]_{D^*} K$

$R_{ADS} < 0.023$ ($D^{*0} \rightarrow D^0 \pi^0$)
 < 0.045 ($D^{*0} \rightarrow D^0 \gamma$)
 90% C.L.



$B \rightarrow [K^+\pi^-]_D K^{*-}$

$R_{ADS} = 0.046 \pm 0.032$ 1 σ



DK : $r_B < 0.23$ 90% C.L. at least

D^*K : $r_B < 0.16$ 90% C.L.

DK^* : $r_B = 0.20 \pm 0.14$ 1 σ

No significant signal

$\rightarrow A_{ADS}$ no measured

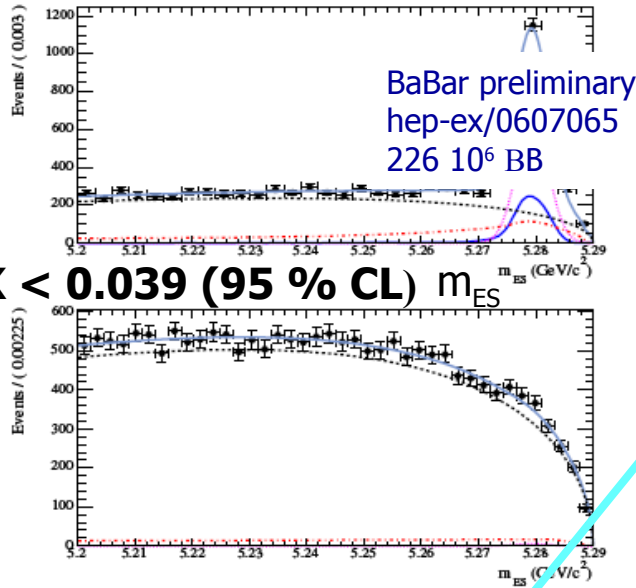
limit on R_{ADS}

limit on r_B using $|\cos(\delta_D + \delta_B)\cos\gamma| < 1_5$

ADS averages

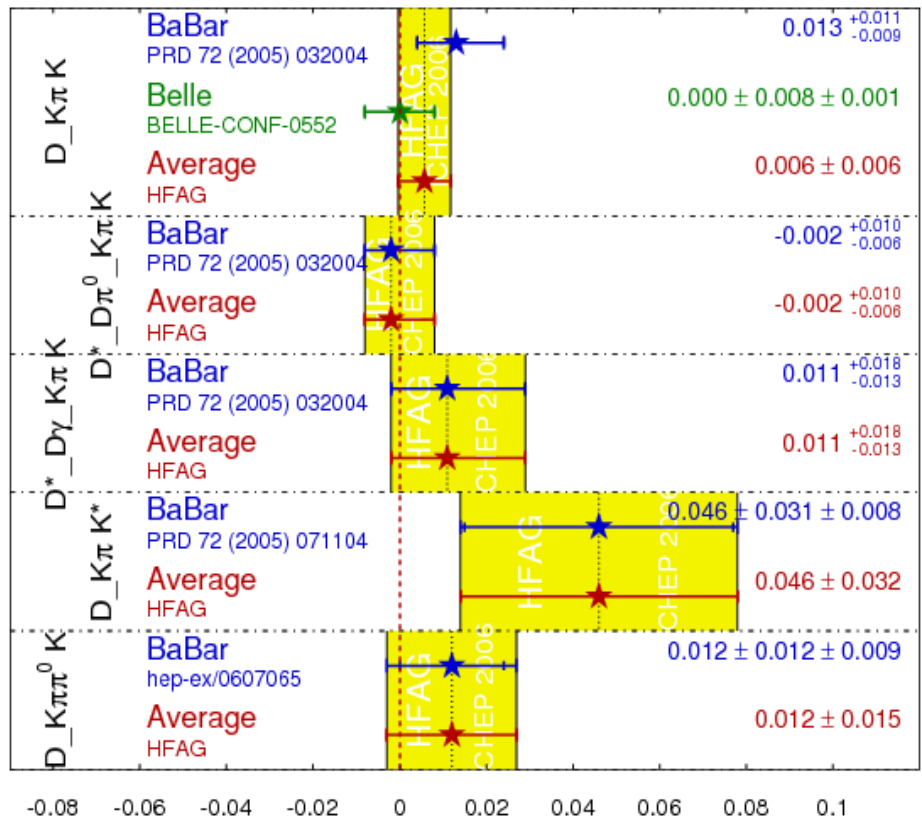
New BaBar result in $[K^+\pi^-\pi^0]_D K^-$

No signal yet in suppressed modes

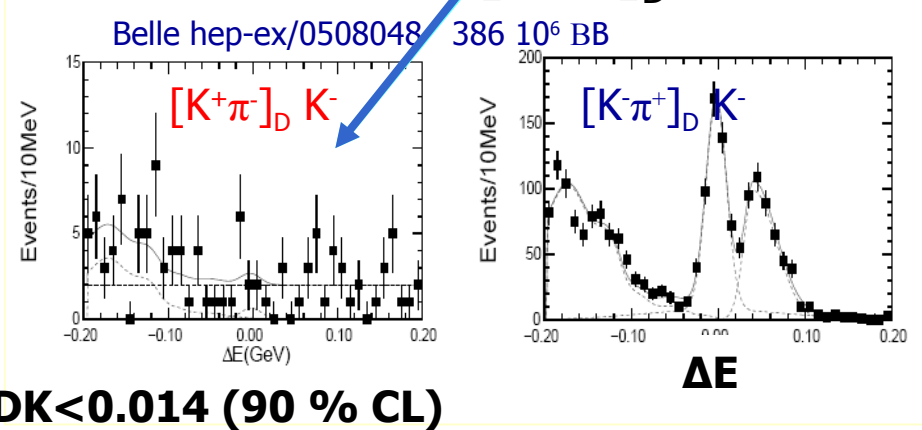


R_{ADS} Averages

HFAG
ICHEP 2006
PRELIMINARY



Belle result in $[K^+\pi^-]_D K^-$





$\forall \gamma$ (and $r_B^{(*)}, \delta_B^{(*)}$) from

UPDATED

known $D^0/\underline{D}^0 \rightarrow K_S \pi^+ \pi^-$ Dalitz model $f_{\pm}(m_+^2, m_-^2)$ $m_{\pm}^2 = m(K_S^0 \pi^{\pm})^2$

– B-/B+ decay rates vs m_+^2, m_-^2

$$\Gamma_{B^{\mp}}(m_-^2, m_+^2) \propto |f_{\mp}|^2 + r_B^{(*)2} |f_{\pm}|^2 + 2\eta \{ x_{\mp}^{(*)} \text{Re}[f_{\pm}^* f_{\mp}] + y_{\mp}^{(*)} \text{Im}[f_{\mp} f_{\pm}^*] \}$$

$$x_{\pm}^{(*)} = r_B^{(*)} \cos(\delta_B^{(*)} \pm \gamma)$$

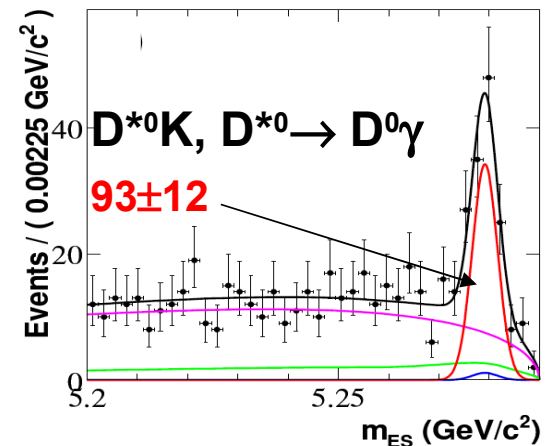
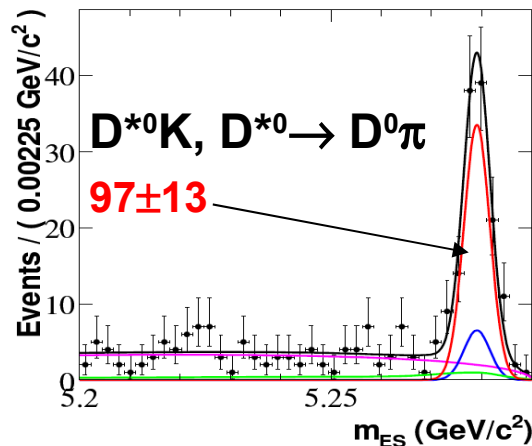
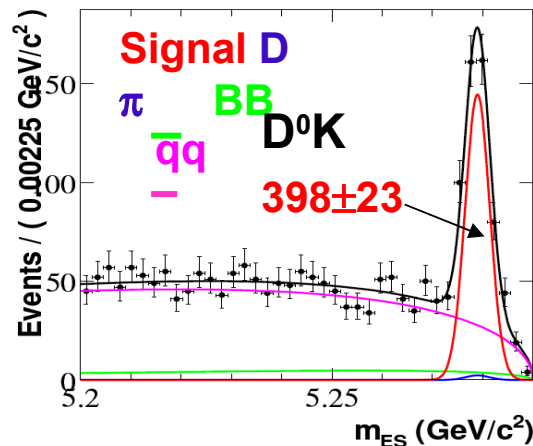
$$y_{\pm}^{(*)} = r_B^{(*)} \sin(\delta_B^{(*)} \pm \gamma)$$

$$r_B^{(*)2} = x_{\pm}^{(*)2} + y_{\pm}^{(*)2}$$

$\eta = +1 (D^0K, D^{*0}[D^0\pi^0]K), -1 (D^{*0}[D^0\gamma]K)$

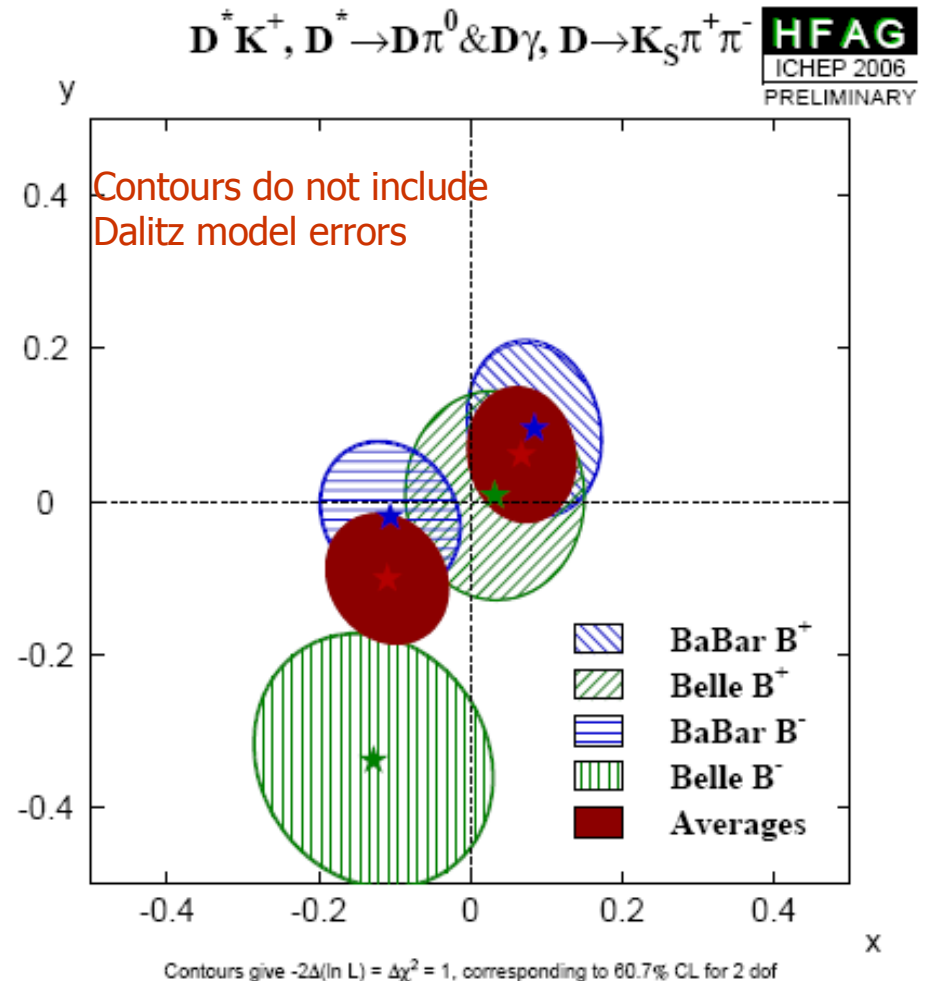
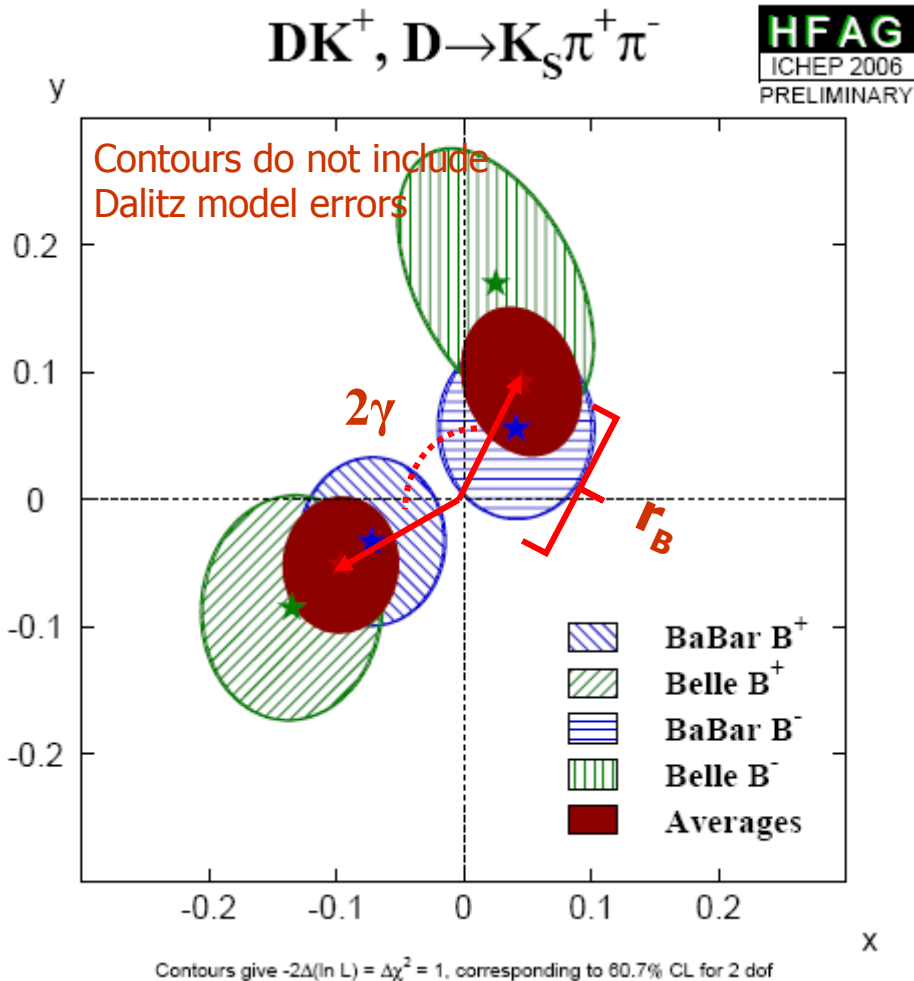
• Update of previous analysis with:

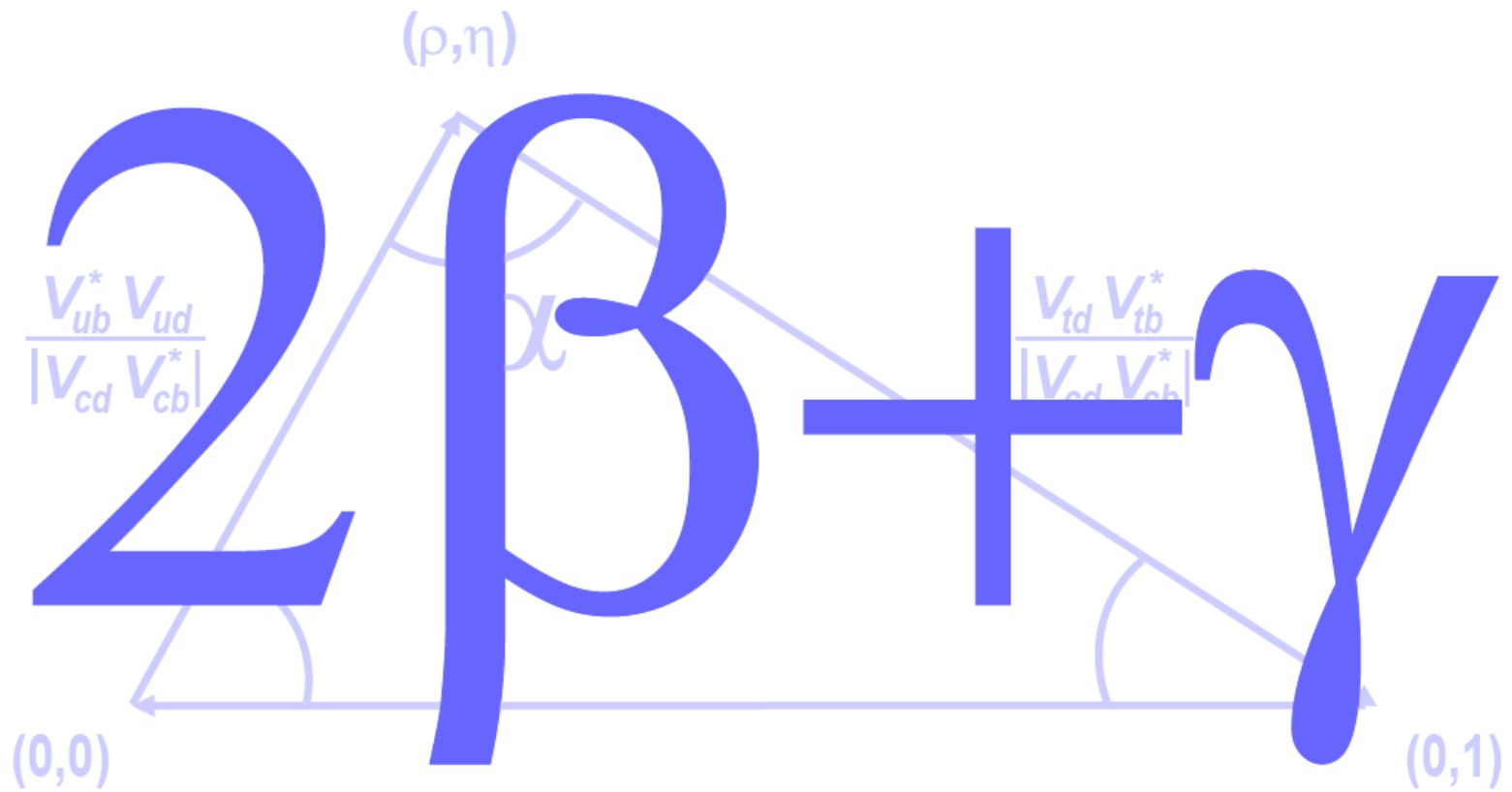
- 1.5x more statistics
- More refined evaluation of systematic uncertainties (esp. Dalitz model one)
- Same Dalitz model (apart from $K^*(1430)$ parameters), larger $D^0/\underline{D}^0 \rightarrow K_S \pi \pi$ sample



Results on γ

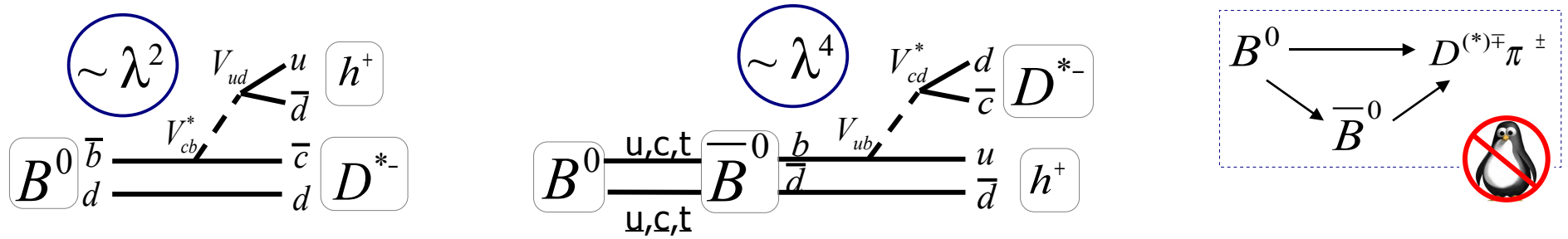
- HFAG averages for $x_{\pm} = r_B \cos(\delta_B \pm \gamma)$, $y_{\pm} = r_B \sin(\delta_B \pm \gamma)$
- UTfit find $\gamma = 78 \pm 30^\circ$ based on $B^- \rightarrow D^{(*)} K^{(*)-}$ decays
- Note: σ_γ depends significantly on the value of r_B





CP violation in neutral B^0 decays \rightarrow time dependant

. Use interference $b \rightarrow c \bar{u} d$ / $b \rightarrow u \bar{c} d$ instead of $b \rightarrow c \bar{u} s$ / $u \bar{c} s$ to extract $2\beta + \gamma$



.. Wrt DK, the favored $b \rightarrow c$ amplitude is $O(\lambda^2)$, the suppressed is $O(\lambda^4)$

- Higher yields

$$- r_{D^{(*)}\pi} \equiv |A(B^0 \rightarrow D^{(*)-}\pi^+) / A(B^0 \rightarrow D^{(*)+}\pi^-)| \approx |V_{ub} V_{cd}| / |V_{cb} V_{ud}|$$

\rightarrow Smaller asymmetries and sensitivity to γ

strong phase between $b \rightarrow u$ and $b \rightarrow c$

... $\sin(2\beta + \gamma)$ is measured from the time evolution:

$$P_\eta(B^0, \Delta t) \propto 1 + \eta \cos(\Delta m_d \Delta t) + (a + \eta b - \eta c) \sin(\Delta m_d \Delta t)$$

$$P_\eta(\bar{B}^0, \Delta t) \propto 1 - \eta \cos(\Delta m_d \Delta t) - (a - \eta b - \eta c) \sin(\Delta m_d \Delta t)$$

$$\eta = + \text{ for } D^{*-}\pi^+, \quad \eta = - \text{ for } D^{*+}\pi^-$$

$$\begin{cases} a = 2r \sin(2\beta + \gamma) \cos \delta \\ c_{lep} = 2r \cos(2\beta + \gamma) \sin \delta \end{cases}$$

Only B's with lepton tag

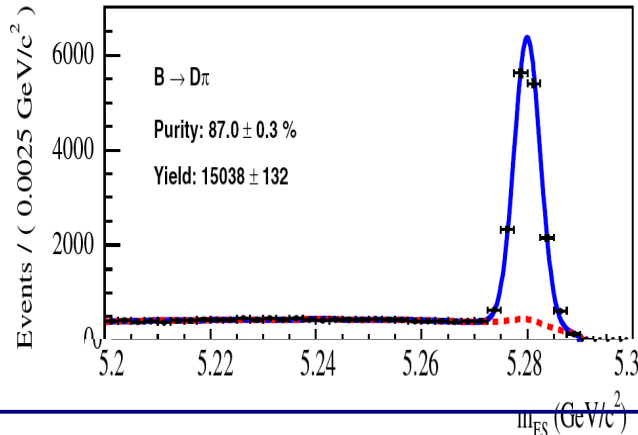
.... In present experiments no hope to fit for r^*

\rightarrow determine elsewhere ($B^0 \rightarrow D_s^{(*)}\pi/\rho$ assuming SU(3), neglecting annihilation)

$\sin(2\beta+\gamma)$ from $B^0 \rightarrow D^{(*)} \pi/\rho$

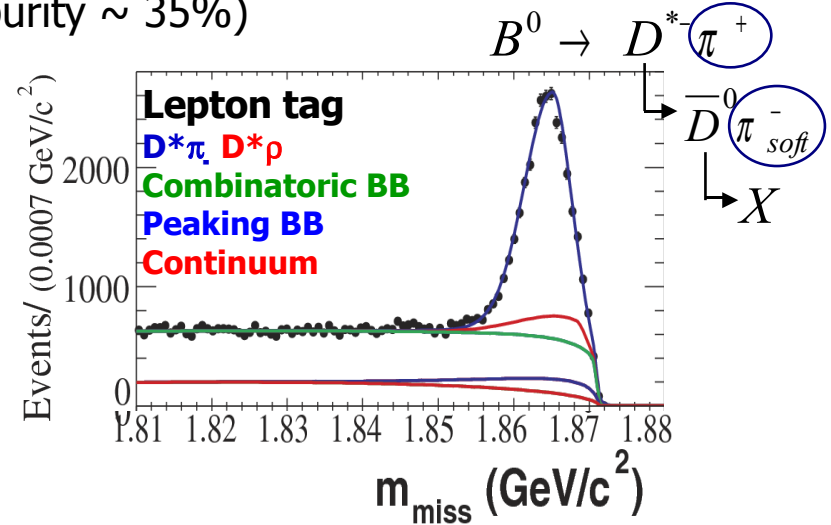


38000 fully reconstructed $D^{(*)}\pi/D\rho$
 (purity $\sim 90\%$)

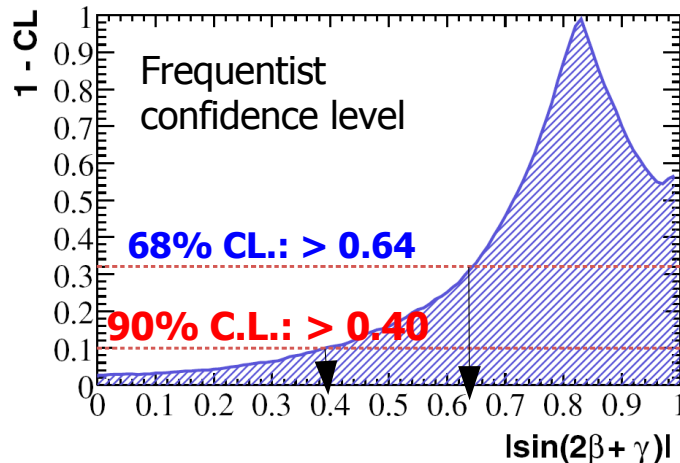


$a^{D\pi} = -0.010 \pm 0.023 \pm 0.007$	$c_{lep.}^{D\pi} = -0.033 \pm 0.042 \pm 0.012$
$a^{D^*\pi} = -0.040 \pm 0.023 \pm 0.010$	$c_{lep.}^{D^*\pi} = 0.049 \pm 0.042 \pm 0.015$
$a^{D\rho} = -0.024 \pm 0.031 \pm 0.009$	$c_{lep.}^{D\rho} = -0.098 \pm 0.055 \pm 0.018$

90000 partially reco'ed $B^0 \rightarrow D^* \pi$ ($D^* \rightarrow D^0 \pi$, $D^0 \rightarrow X$)
 (purity $\sim 35\%$)



$a^{D^*\pi} = -0.034 \pm 0.014 \pm 0.009$
$c_{lep.}^{D^*\pi} = -0.025 \pm 0.020 \pm 0.013$



Using

$r_{D\pi} = 0.019 \pm 0.004$
$r_{D^*\pi} = 0.015 \pm 0.006$
$r_{D\rho} = 0.003 \pm 0.006$

$|\sin(2\beta+\gamma)| > 0.64(0.40) @ 68(90)\% CL$

Observation of $B^0 \rightarrow D_s^{(*)+} \pi^- , D_s^{(*)-} K^+$



$\sin(2\beta+\gamma)$ in $B^0 \rightarrow D^{(*)\mp} \pi^\pm$ needs $r(D^{(*)}\pi) = |A(B^0 \rightarrow D^{(*)+} \pi^-) / A(B^0 \rightarrow D^{(*)-} \pi^+)|$

but

current available data \rightarrow direct BF measurement

$$r(D^{(*)}\pi) \stackrel{\text{SU(3)}}{=} \tan \theta_c \frac{f_{D^{(*)}}}{f_{D_s^{(*)}}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^{(*)+} \pi^-)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \pi^+)}}$$

$\tan \theta_c$: Cabibbo angle
 $f_{D^{(*)}}/f_{D_s^{(*)}}$: ratio of $D^{(*)}$ and $D_s^{(*)}$ decay const

measured BF through D_s^+ reco in

$D_s \rightarrow \phi\pi, K^0 K^+$ and $K^{*0} K^+$ modes :

$$\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (1.3 \pm 0.3 \pm 0.2) * 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow D_s^{*+} \pi^-) = (2.8 \pm 0.6 \pm 0.5) * 10^{-5}$$

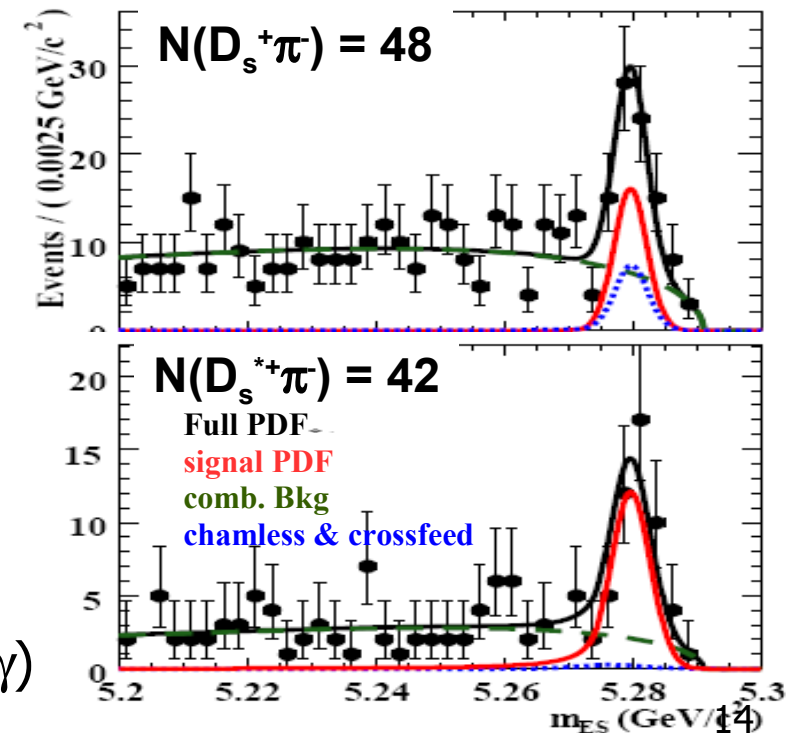
SU(3)

$$r(D \pi) = (1.3 \pm 0.2 \pm 0.1) * 10^{-2} \text{ (30\% smaller)}$$

$$r(D^* \pi) = (1.9 \pm 0.2 \pm 0.2) * 10^{-2} \text{ (25\% larger)}$$

\rightarrow Improved σ_r but smaller $\langle r \rangle$

\rightarrow expect no big improvement on $\sigma(2\beta+\gamma)$



$\text{Sin}(2\beta+\gamma)$ from $B \rightarrow D^{(*)0}K^0$ and $D^{(*)}a_{0(2)}$?



$f = D^{(*)0}K_s$

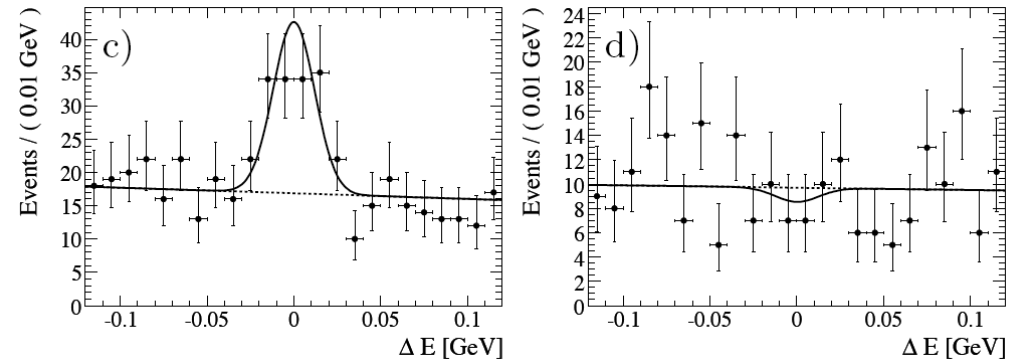
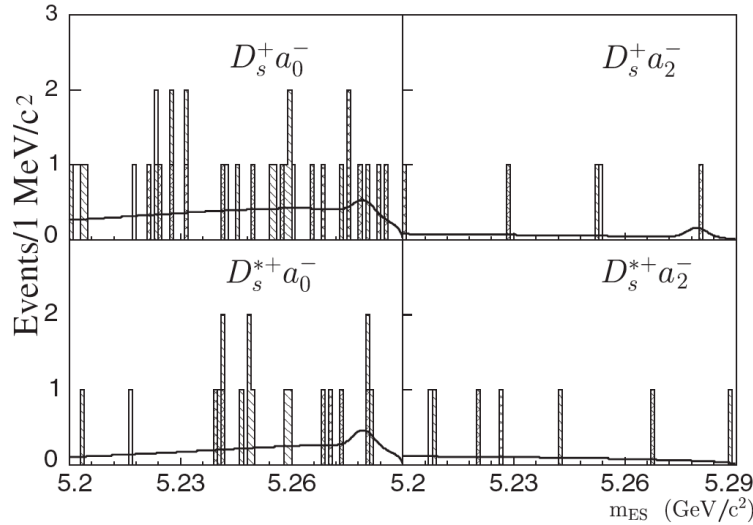
- Both $b \rightarrow c$ and $b \rightarrow u$ amplitudes are color-suppressed
 $\rightarrow \text{BR} \sim 10^{-5}$, $r \approx f * |V_{ub} V_{cs}| / |V_{cb} V_{us}| \approx f * 0.4$

(f: different strong interaction dynamics in $b \rightarrow c, u$)

$f = D^{(*)}a_0(2)$

- .. $D^{(*)0}K^0$ ($K^0 \rightarrow K_s$) BFs and r in the self-tagging final state

$D^0K^{*0}, K^{*0} \rightarrow K\pi$ (assuming that r for DK^{*0} is the same as r for DK^0)



We measure (SU(3)- related) $D^{(*)}a_{0(2)}$ BF upper limits:

$$\begin{aligned} BF(B \rightarrow D_s^+ a_0^-) &< 1.9 \cdot 10^{-5} & BF(B \rightarrow D_s^{*+} a_0^-) &< 3.6 \cdot 10^{-5} \\ BF(B \rightarrow D_s^+ a_2^-) &< 1.9 \cdot 10^{-4} & BF(B \rightarrow D_s^{*+} a_2^-) &< 2.0 \cdot 10^{-4} \end{aligned}$$

$BF(D^{(*)}a_{0(2)}) < \approx 10^{-6}$.

Since $\epsilon < \approx 10\%$ and secondary BFs $\sim 10\%$,
 channel is not usable to measure $\text{sin}(2\beta+\gamma)$ at BaBar

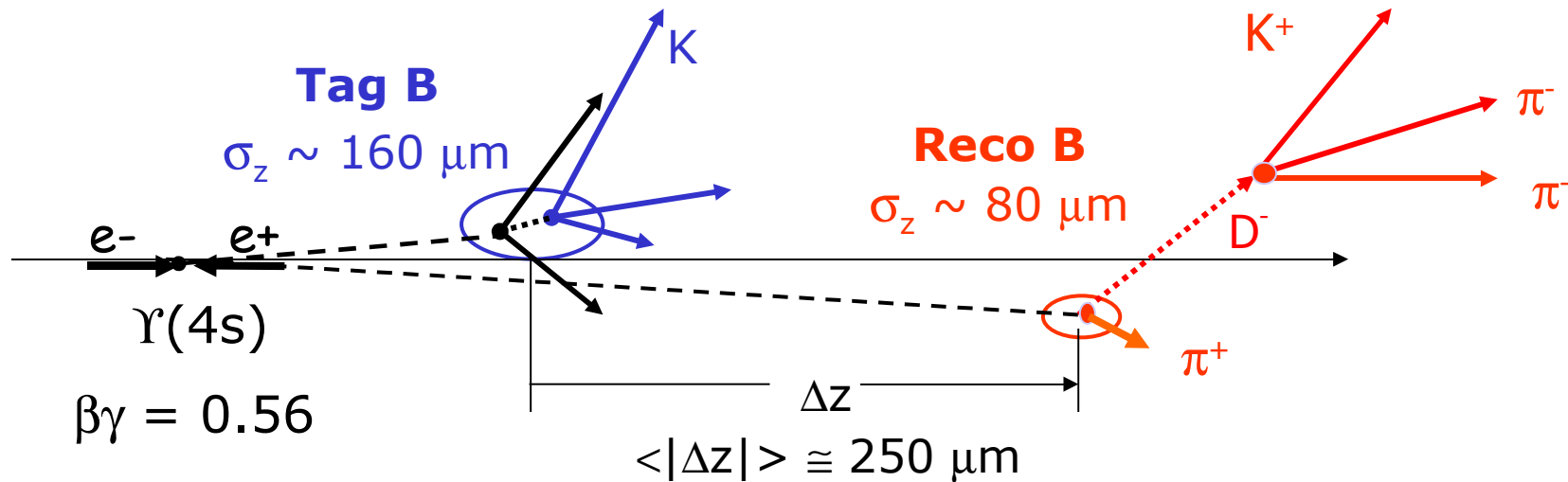
$$\begin{aligned} \mathcal{B}(\tilde{B}^0 \rightarrow D^0 \tilde{K}^0) &= (5.3 \pm 0.7 \pm 0.3) \times 10^{-5} \\ \mathcal{B}(\tilde{B}^0 \rightarrow D^{*0} \tilde{K}^0) &= (3.6 \pm 1.2 \pm 0.3) \times 10^{-5} \\ \mathcal{B}(\bar{B}^0 \rightarrow D^0 \bar{K}^{*0}) &= (4.0 \pm 0.7 \pm 0.3) \times 10^{-5} \\ \mathcal{B}(\bar{B}^0 \rightarrow \bar{D}^0 \bar{K}^{*0}) &= (0.0 \pm 0.5 \pm 0.3) \times 10^{-5} \end{aligned}$$

$r(D^0K^{*0}) < 0.4$ @ 90% C.L.:

r_B smaller than theo. expected

not useful to measure γ value yet

Experimental technique



3. Reconstruct inclusively the vertex of the "other" B meson (B_{TAG})

4. Determine the flavor of B_{TAG}

1. Reconstruct one B meson (B_{REC}) in a final state of interest (e.g. $D^-\pi^+$)

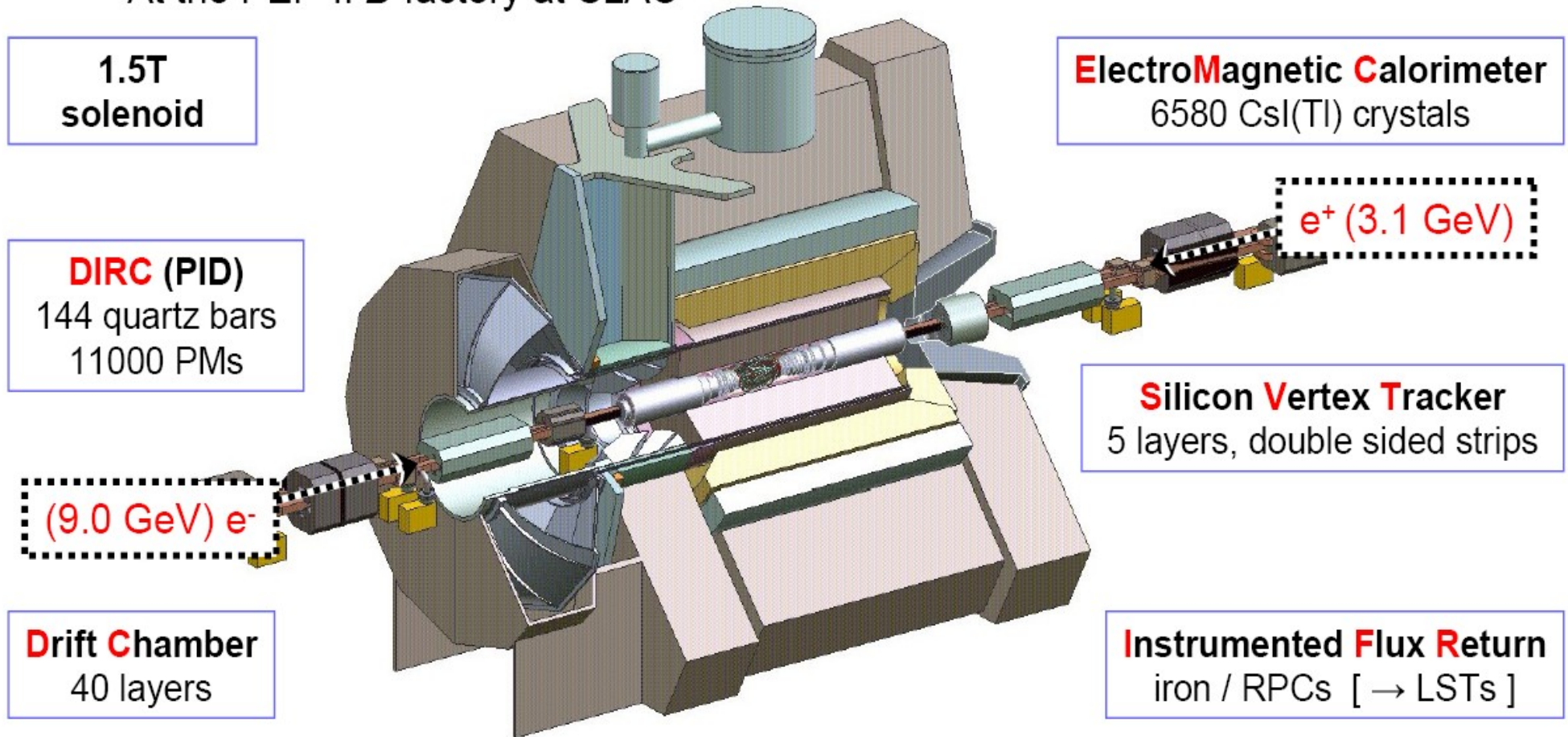
2. Reconstruct the vertex position

5. Compute the proper time difference $\Delta t \cong \Delta z / \gamma\beta c$ (RMS ~ 1.1 ps)

6. Fit the Δt spectra

B_AB_AR : where? what? who?

- At the PEP-II *B*-factory at SLAC



- *BABAR* collaboration consists 11 countries and ~590 physicists !



References

γ :

$r_B^{(*)}$, theoretical expectation value: [Phys. Lett B265, 172 \(1991\)](#), [PL B557, 198 \(2003\)](#)

Gronau-London-Wyler method: [Phys. Lett. B253, 483](#); [Phys. Lett. B265, 172 \(1991\)](#)

. $D^0 K$: [PRD 73, 051105 – 232 *10⁶ BB](#)

. $D^0 K^*$: [PRD 73, 071103 – 232 *10⁶ BB](#)

. $D^{*0} K$: [PRD 71, 031102 – 123 *10⁶ BB](#)

Atwood-Dunietz-Sony method : [Phys. Rev. Lett. 78, 3257 \(1997\)](#)

. $D^{(*)0} K$: [PRD 72, 032004 – 232 *10⁶ BB](#)

. $D^{0*} K$: [PRD 72, 071104 – 232 *10⁶ BB](#)

. $D^0 [K^+ p^- p^0] K$: [hep-ex/0607065 – 226 *10⁶ BB](#)

Giri-Grossman-Soffer-Zupan (Dalitz) method: [Phys. Rev. D68, 054018 \(2003\)](#)

. $D^{(*)0} K$: [hep-ex/0607104 – 347 *10⁶ BB](#)

. DK^* : [hep-ex/0507101 – 227 *10⁶ BB](#)

$2\beta + \gamma$:

. $B^0 \rightarrow D^{(*)} \pi / \rho$: [PRD73 :111101 - 232 *10⁶ BB](#) , [PRD71:112003- 232 *10⁶ BB](#)

. $B^0 \rightarrow D_s^{(*)+} \pi^- , D_s^{(*)-} K^+$: [hep-ex/0604012 - 230 *10⁶ BB](#)

