

# Heavy Quark-Diquark Symmetry and $\chi$ PT for Doubly Heavy Baryons

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DPF 2006, 10/30/2006, Honolulu, Hawaii

- S. Fleming & T.M., PRD 73, 034502 (2006)
- J. Hu & T.M., PRD 73, 054003 (2006)
- T.M. & B. Tiburzi, PRD 74, 054505 (2006)

# Outline

- Motivation

Experiment: SELEX  $\Xi_{cc}^+, \Xi_{cc}^{++}$  candidates

Theory: Heavy Quark-Diquark Symmetry  $\bar{Q}\bar{Q}\bar{q} \leftrightarrow Q\bar{q}$

Savage, Wise

- Diquark Effective actions from vNRQCD

S. Fleming, T.M., PRD 73, 034502 (2006)

$Q\bar{Q}, QQ$  bound states characterized by several scales:

$$m_Q, \quad p \sim m_Q v, \quad E \sim m_Q v^2, \quad \Lambda_{\text{QCD}}$$

HQET: expansion in  $\Lambda_{\text{QCD}}/m_Q$   $m_Q v, m_Q v^2$  missing

Heavy  $Q\bar{Q}, QQ$  systems require NonRelativistic QCD

- Chiral Lagrangians with Quark-Diquark Symmetry

J. Hu, T.M., PRD 73, 054003 (2006)

NEW symmetry predictions for  $\Xi_{cc}^* \rightarrow \Xi_{cc} + \gamma$

em, strong decays of excited doubly heavy baryons

- Quenched and Partially Quenched Theories

T.M., B. Tiburzi, PRD 74, 054505 (2006)

nonanalytic chiral corrections for lattice simulations

doubly heavy masses, hyperfine splittings

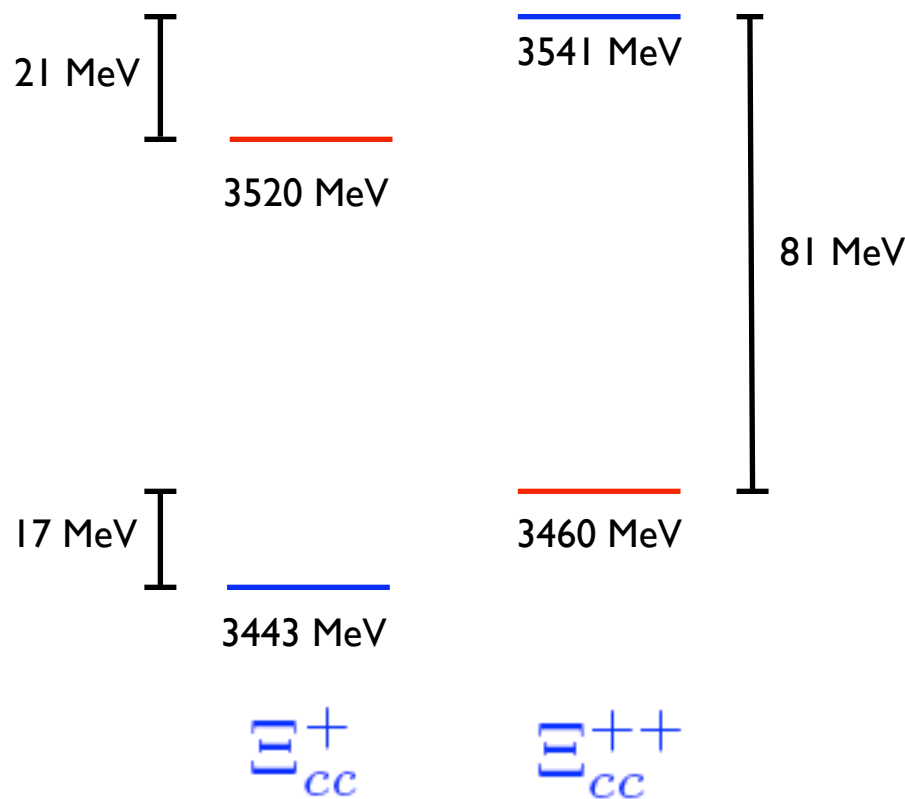
Q-DQ hyperfine prediction: small corrections!

em decays, including  $1/m_Q$  corrections

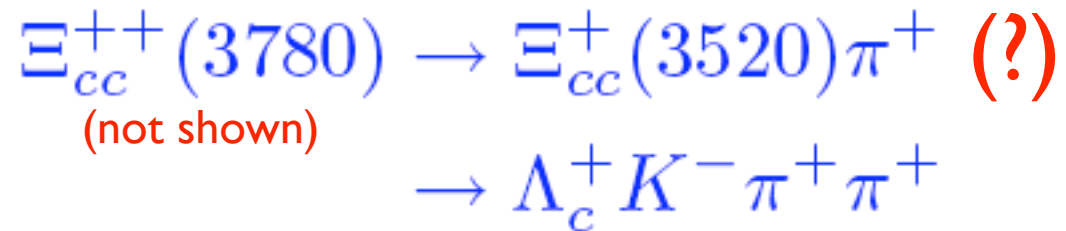
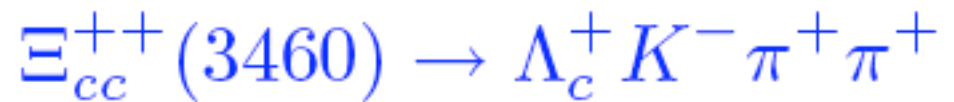
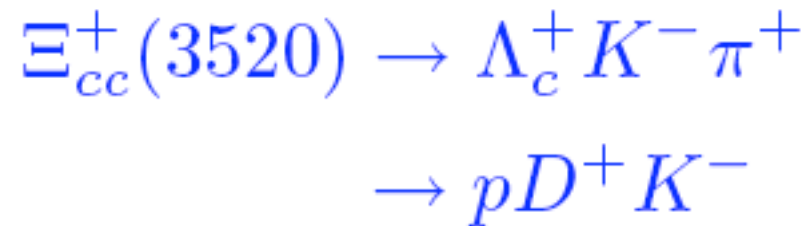
- Outlook

# SELEX Doubly Charm Baryons?

PRL 89, 112001(2002), PLB 628,18 (2004)



## Observed decays



- $\Xi_{cc}^+(3443), \Xi_{cc}^{++}(3541)$  unpublished [www-selex.fnal.gov/Welcome.html](http://www-selex.fnal.gov/Welcome.html)

- high statistical significance, few events ( $\sim 10-30$ )

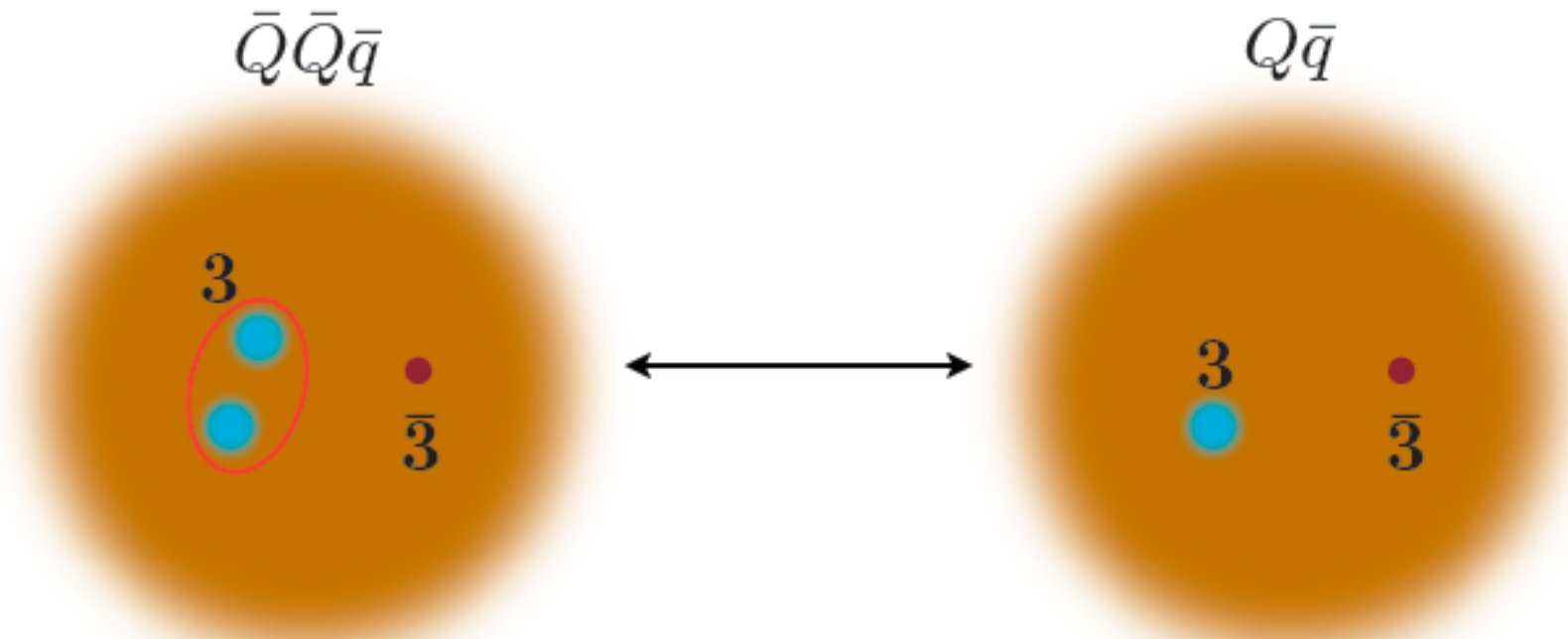
- search by BELLE fails to confirm  $\Xi_{cc}^+(3520)$  (hep-ex/0606051)

- Masses, hyperfine consistent with quark model, lattice  
hyperfine splitting  $\sim 80$  MeV      Lewis, Mathur, Woloshyn; Flynn, Mescia, Tariq

## Puzzling Aspects of SELEX Observation

- Isospin splitting  $\sim 20$  MeV ?      larger than expected
- radiative decays should dominate weak decay  
 $\Xi_{cc}^+(3520)$  excited state?       $\Xi_{cc}^* \rightarrow \Xi_{cc} + \gamma$  ?
- Weak lifetimes      Guberina, et. al. EPJ C9, 213 (1999)  
experiment:  $< 33$  fs      theory (HQET+OPE):  $\sim 100$  fs
- Production cross sections      (Kiselev, Likhoded, hep-ph/0208231)  
significantly larger than expected from LO pQCD  
forward production  $\langle x_F \rangle \sim 0.3$       seen in  $p, \Sigma$  not  $\pi$  beams  
nonperturbative mechanisms (e.g. intrinsic charm, leading particle effect) ?

# Heavy Quark-Diquark Symmetry



- HQET-like Lagrangian for Heavy Diquarks (Savage, Wise)

$$\mathcal{L} = h^\dagger iD_0 h + \vec{T}^\dagger \cdot iD_0 \vec{T} + \frac{g_s}{2m_Q} h^\dagger \vec{\sigma} \cdot \vec{B} h + \frac{ig_s}{2m_Q} \vec{T}^\dagger \cdot \vec{B} \times \vec{T} + \dots$$

- At lowest order, U(5) symmetry acting on  $(h, \vec{T})$

Hyperfine splittings:  $m_{\Xi^*} - m_{\Xi} = \frac{3}{4} (m_{H^*} - m_H)$

- Hyperfine splittings in quark model

$$H_{Q\bar{q}} = \dots + \frac{\lambda}{m_Q m_q} \vec{S}_Q \cdot \vec{S}_{\bar{q}}$$

$$H_{\bar{Q}Q\bar{q}} = \dots + \frac{1}{2} \frac{\lambda}{m_Q m_q} \sum_{\bar{Q}} \vec{S}_{\bar{Q}} \cdot \vec{S}_{\bar{q}}$$

- $\frac{1}{2}$  - color SU(3) factor:  $\bar{Q}\bar{q}$  in  $\bar{3}$  vs.  $Q\bar{q}$  in 1
- Prediction for doubly charm baryons

$$m_{\Xi_{cc}^*} - m_{\Xi_{cc}} \approx \frac{3}{4} (m_{D^*} - m_D) = 106 \text{ MeV}$$

- Error?  $O\left(\frac{\Lambda_{\text{QCD}}}{m_c}\right) \sim \frac{1}{3}$       106 MeV vs. 80 MeV ??

# Heavy $Q\bar{Q}$ , $\bar{Q}\bar{Q}$ Systems: NonRelativistic QCD (NRQCD)

- **vNRQCD**: separate  $k$  into  $O(m_Q v)$  and  $O(m_Q v^2)$  parts

$$\vec{k} = \vec{p} + \vec{k}' \quad h_v = \sum_{\vec{p}} e^{-i\vec{p}\cdot\vec{x}} \psi_{\vec{p}} \quad D_\mu \psi_{\vec{p}} = O(m_Q v^2) \psi_{\vec{p}}$$

- **vNRQCD Lagrangian** (Luke, Manohar, Rothstein)

$$\mathcal{L} = \sum_{\mathbf{p}} \chi_{\mathbf{p}}^\dagger \left( iD^0 - \frac{(\mathbf{p} - i\mathbf{D})^2}{2m_Q} + \frac{g}{2m_Q} \boldsymbol{\sigma} \cdot \mathbf{B} \right) \chi_{\mathbf{p}} - \frac{1}{2} \sum_{\mathbf{p}, \mathbf{q}} \frac{g_s^2}{(\mathbf{p} - \mathbf{q})^2} \chi_{\mathbf{q}}^\dagger \bar{T}^A \chi_{\mathbf{p}} \chi_{-\mathbf{q}}^\dagger \bar{T}^A \chi_{-\mathbf{p}} + \dots$$

- **Power counting**:  $\vec{p} \sim m_Q v$   $\psi_{\vec{p}}, \chi_{\vec{p}} \sim (m_Q v)^{3/2}$

$$D_0, \vec{D} \sim m_Q v^2 \quad (\text{soft gluons}) \quad A^\mu \sim m_Q v^2 \quad (\text{soft}) \quad A_{\vec{p}}^\mu \sim m_Q v$$

- **HQET +  $\bar{Q}\bar{Q}\bar{Q}\bar{Q}$  Operators**, **different power counting**



- **Effective Action for Heavy Diquarks**

S. Fleming, T.M., PRD 73, 034502 (2006)

- **composite diquark field**  $\mathbf{T}_r^i = \sum_{\mathbf{p}} e^{i\mathbf{p}\cdot\mathbf{r}} \frac{1}{2} \epsilon^{ijk} (\chi_{-\mathbf{p}})_j \epsilon^\sigma (\chi_{\mathbf{p}})_k$

- **Hubbard-Stratonovich trans., integrate out  $\chi_p$**

$$\begin{aligned} \mathcal{L}_{\mathbf{T}} &= \int d^3\mathbf{r} \mathbf{T}_r^\dagger \left( iD_0 + \frac{\nabla_{\mathbf{r}}^2}{m_Q} - V^{(3)}(r) \right) \mathbf{T}_r + \frac{g}{2m_Q} \int d^3\mathbf{r} i \mathbf{T}_r^\dagger \cdot \mathbf{B} \times \mathbf{T}_r \\ &= \sum_n \mathbf{T}_n^\dagger (iD_0 + \delta_n) \mathbf{T}_n + \frac{g}{2m_Q} i \sum_n \mathbf{T}_n^\dagger \cdot \mathbf{B} \times \mathbf{T}_n \end{aligned}$$

$$\mathbf{T}_r^i = \sum_n \mathbf{T}_n^i \phi_n(\mathbf{r}) \quad \left( -\frac{\nabla_{\mathbf{r}}^2}{m_Q} + V^{(3)}(r) \right) \phi_n(\mathbf{r}) = -\delta_n \phi_n(\mathbf{r})$$

- **Savage-Wise Lagrangian obtained after integrating out all excited diquark fields**

# Chiral Lagrangian with Heavy Quark-Diquark

**Symmetry** J. Hu, T.M., PRD 73, 054003 (2006)

- **Heavy Hadron Chiral Perturbation Theory**

(Wise; Burdman, Donoghue, Yan, et. al.)

- **Heavy Meson Fields** combine  $0^-$  and  $1^-$  heavy mesons in single field

$$H_a = (Q\bar{q}_a) = \left( \frac{1 + \not{v}}{2} \right) (P_a^{*\mu} \gamma_\mu - \gamma_5 P_a)$$

- **Goldstone Bosons**  $(\pi, K, \eta)$   $SU(3)_L \times SU(3)_R \rightarrow SU_{L+R}(3)$

$$\xi = e^{i\Pi/f} \quad \Sigma = \xi^2$$

$$D_{ab}^\mu = \delta_{ab} \partial^\mu - V_{ab}^\mu \quad V_{ab}^\mu = \frac{1}{2} (\xi^\dagger \partial^\mu \xi + \xi \partial^\mu \xi^\dagger) \quad A_{ab}^\mu = \frac{i}{2} (\xi^\dagger \partial^\mu \xi - \xi \partial^\mu \xi^\dagger)$$

- $$\mathcal{L} = \frac{f^2}{8} \text{Tr} \partial^\mu \Sigma \partial_\mu \Sigma^\dagger + \frac{f^2 B_0}{4} \text{Tr} (m_q \Sigma + m_q \Sigma^\dagger)$$

$$- \text{Tr} \bar{H}_a i v \cdot D_{ba} H_b + g \text{Tr} \bar{H}_a H_b \gamma_\mu \gamma_5 A_{ba}^\mu + \dots$$

- In rest frame,  $v = (1, \vec{0})$   $H_v = \begin{pmatrix} 0 & -\vec{P}_v \cdot \vec{\sigma} - P_v \\ 0 & 0 \end{pmatrix}$

For processes where four velocity is conserved we can work in heavy meson rest frame and  $H_v$  can be represented by  $2 \times 2$  field

$$H_a = \vec{P}_a \cdot \vec{\sigma} + P_a$$

$$\mathcal{L} = \text{Tr}[H_a^\dagger (iD_0)_{ba} H_b] - g \text{Tr}[H_a^\dagger H_b \vec{\sigma} \cdot \vec{A}_{ba}] + \frac{\Delta_H}{4} \text{Tr}[H_a^\dagger \sigma^i H_a \sigma^i]$$

- Including Doubly Heavy Baryons  $2 \times 2$  field  $\rightarrow 5 \times 2$  field

$$H_{a,\alpha\beta} \rightarrow \mathcal{H}_{a,\mu\beta} = H_{a,\alpha\beta} + T_{a,i\beta}$$

$$T_{a,i\beta} = \sqrt{2} \left( \Xi_{a,i\beta}^* + \frac{1}{\sqrt{3}} \Xi_{a,\gamma} \sigma_{\gamma\beta}^i \right) \quad \Xi_{a,i\beta}^* \sigma_{\beta\gamma}^i = 0.$$

- **Transformations**

rotations  $\mathcal{H}'_a = \mathcal{R}\mathcal{H}_a U^\dagger$

$$\mathcal{R} = \begin{pmatrix} U & 0 \\ 0 & R \end{pmatrix} \quad \begin{array}{l} U - 2 \times 2 \\ R - 3 \times 3 \end{array}$$

heavy quark spin  $\mathcal{H}'_a = S\mathcal{H}_a$

parity  $\mathcal{H}'_a = -\mathcal{H}_a$

$$S \subset U(5) \quad V \subset SU(3)$$

SU(3) chiral  $\mathcal{H}'_a = \mathcal{H}_b V_{ba}^\dagger$

- **Chiral Lagrangian**

$$\mathcal{L} = \text{Tr}[\mathcal{H}_a^\dagger (iD_0)_{ba} \mathcal{H}_b] - g \text{Tr}[\mathcal{H}_a^\dagger \mathcal{H}_b \vec{\sigma} \cdot \vec{A}_{ba}] + \frac{\Delta_H}{4} \text{Tr}[\mathcal{H}_a^\dagger \Sigma^i \mathcal{H}_a \sigma^i]$$

$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{T} \end{pmatrix} \quad (\mathcal{T}^i)_{jk} = -i\epsilon_{ijk}$$

- **hyperfine splitting**

$$m_{\Xi^*} - m_{\Xi} = \frac{3}{4}(m_{P^*} - m_P)$$

- Including electromagnetic interactions

$$\frac{e\beta}{2} \text{Tr}[\mathcal{H}_a^\dagger \mathcal{H}_b \vec{\sigma} \cdot \vec{B} Q_{ab}] + \frac{e}{2m_Q} Q' \text{Tr}[\mathcal{H}_a^\dagger \vec{\Sigma}' \cdot \vec{B} \mathcal{H}_b] \quad \vec{\Sigma}' = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & -2\vec{T} \end{pmatrix}$$

- Radiative Decay Rates  $\beta = \frac{1}{m_q}$  in quark model

$$\Gamma[P_a^* \rightarrow P_a \gamma] = \frac{\alpha}{3} \left( \beta Q_{aa} + \frac{Q'}{m_Q} \right)^2 \frac{m_P}{m_{P^*}} E_\gamma^3$$

$$\Gamma[\Xi_a^* \rightarrow \Xi_a \gamma] = \frac{4\alpha}{9} \left( \beta Q_{aa} - \frac{Q'}{m_Q} \right)^2 \frac{m_\Xi}{m_{\Xi^*}} E_\gamma^3$$

- Include  $O(\sqrt{m_q})$  chiral corrections (Amundsen, et. al.)

$$\beta Q_{11} \rightarrow \frac{2}{3}\beta - \frac{g^2 m_K}{4\pi f_K^2} - \frac{g^2 m_\pi}{4\pi f_\pi^2}$$

$$\beta Q_{22} \rightarrow -\frac{1}{3}\beta + \frac{g^2 m_\pi}{4\pi f_\pi^2} \quad \beta Q_{33} \rightarrow -\frac{1}{3}\beta + \frac{g^2 m_K}{4\pi f_K^2}$$

Fit	$\beta^{-1}(\text{MeV})$	$m_c(\text{MeV})$	$\Gamma[\Xi_{cc}^{*++}] (\text{keV})$	$\Gamma[\Xi_{cc}^{*+}] (\text{keV})$
QM 1	379	1863	$3.3 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$	$2.6 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$
QM 2	356	1500	$3.4 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$	$3.2 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$
$\chi$ PT 1	272	1432	$2.3 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$	$3.5 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$
$\chi$ PT 2	276	1500	$2.3 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$	$3.3 \left( \frac{E_\gamma}{80 \text{ MeV}} \right)^3$

● QM: no chiral correction      1 - fit  $m_c$    2- fix  $m_c = 1500 \text{ MeV}$

●  $\chi$ PT:  $f_\pi = 130 \text{ MeV}$     $f_K = 159 \text{ MeV}$

●  $\Gamma[\Xi^*] \sim 3 \text{ keV}$       QM :  $\Gamma[\Xi^{*++}] \approx \Gamma[\Xi^{*+}]$

$\chi$ PT :  $\Gamma[\Xi^{*++}] < \Gamma[\Xi^{*+}]$

# Quenched and Partially Quenched Theories

- Existing calculations of bbq, ccq baryons are quenched

Lewis, Mathur, Woloshyn; Flynn, Mescia, Tariq

- Lattice can potentially answer important questions:

how heavy quarks have to be for Quark-Diquark symmetry to work?

predict masses, hyperfine splittings

matrix elements for em, weak decays

- Simulations w/ dynamical sea quarks needed  
(and are being planned)

- Motivates construction of quenched and partially quenched versions of Quark-Diquark symmetric  $\chi$ PT

T.M., B. Tiburzi, PRD 74, 054505 (2006)

- One loop mass corrections



- nonanalytic corrections to hyperfine splitting

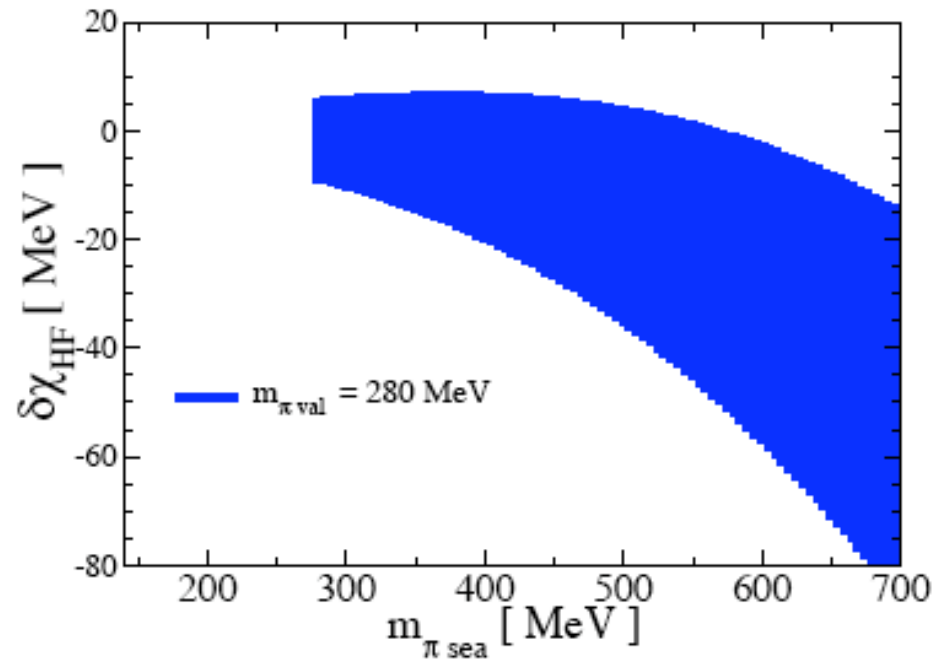
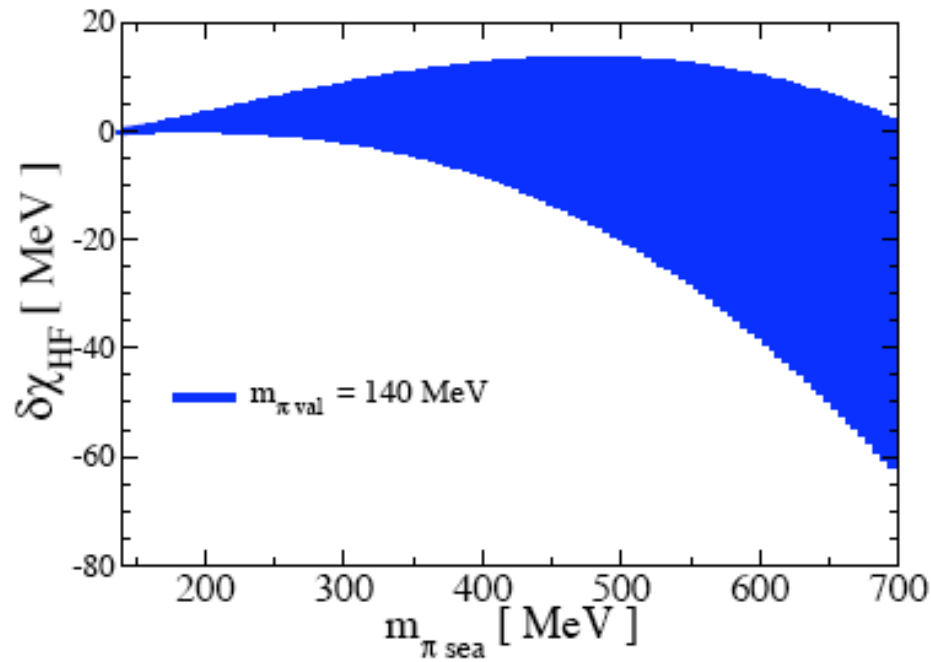
$$\delta m_{\Xi_{cc}^*} - \delta m_{\Xi_{cc}} = \begin{cases} -7.0 \text{ MeV} & \mu = 500 \text{ MeV} \\ 8.1 \text{ MeV} & \mu = 1000 \text{ MeV} \\ 16.9 \text{ MeV} & \mu = 1500 \text{ MeV} \end{cases}$$

$$\delta m_{\Xi_{cc}^*} - \delta m_{\Xi_{cc}} - \frac{3}{4}(\delta m_{D^*} - \delta m_D) = \begin{cases} 3.9 \text{ MeV} & \mu = 500 \text{ MeV} \\ 5.3 \text{ MeV} & \mu = 1000 \text{ MeV} \\ 6.1 \text{ MeV} & \mu = 1500 \text{ MeV} \end{cases}$$

- $\mu$  dependence cancelled by counterterms (not included)
- nonanalytic chiral corrections small



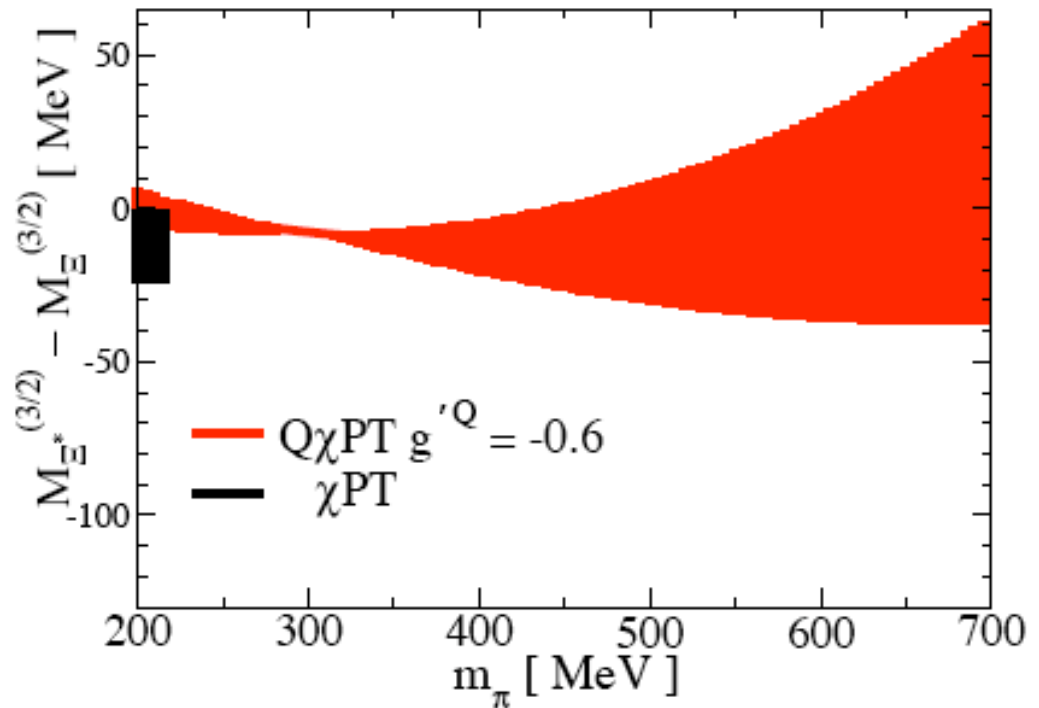
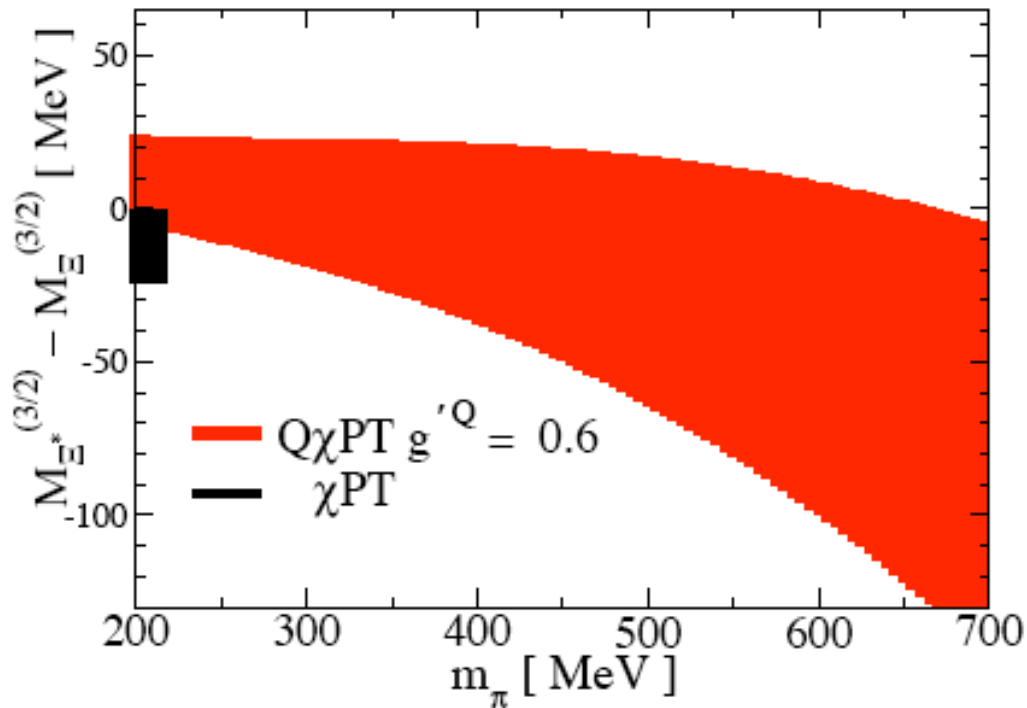
- PQQ $\chi$ PT nonanalytic corrections to hyperfine splittings



$$\delta\chi_{HF} = \left( M_{\Xi^*}^{(3/2)} - M_{\Xi}^{(3/2)} \right)_{\text{PQQ}\chi\text{PT}} - \left( M_{\Xi^*}^{(3/2)} - M_{\Xi}^{(3/2)} \right)_{\chi\text{PT}}$$

- nonanalytic corrections large: +15 MeV, -60 MeV

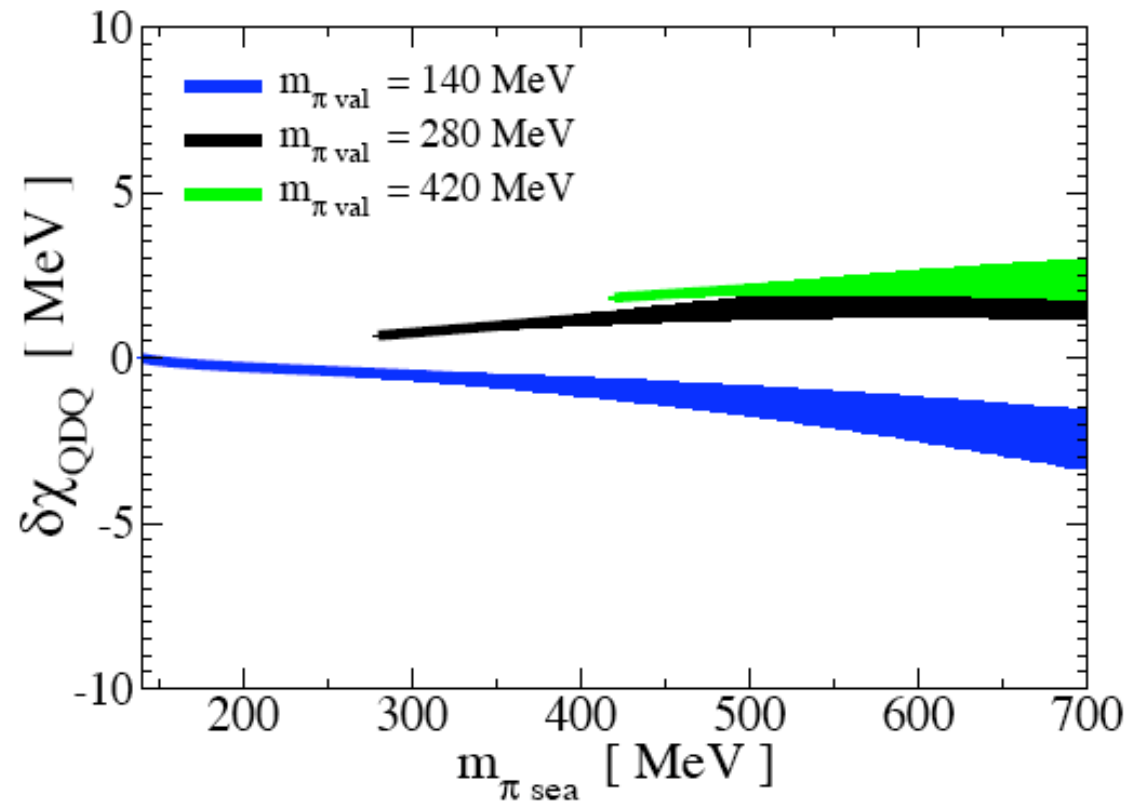
- qualitatively similar results in quenched theory



- $$\mathcal{L}^Q = \left( \mathcal{H}^\dagger (\mathcal{H} i \overleftrightarrow{D}_0) \right) - g^Q (\mathcal{H}^\dagger \mathcal{H} \mathbf{A} \cdot \boldsymbol{\sigma}) - g'^Q (\mathcal{H}^\dagger \mathcal{H} \boldsymbol{\sigma}) \cdot \text{str}(\mathbf{A})$$

$$+ \frac{\Delta_H^Q}{4} (\mathcal{H}^\dagger \boldsymbol{\Sigma} \cdot \mathcal{H} \boldsymbol{\sigma}) + \sigma^Q (\mathcal{H}^\dagger \mathcal{H} \mathcal{M}) + \sigma'^Q (\mathcal{H}^\dagger \mathcal{H}) \text{str}(\mathcal{M})$$

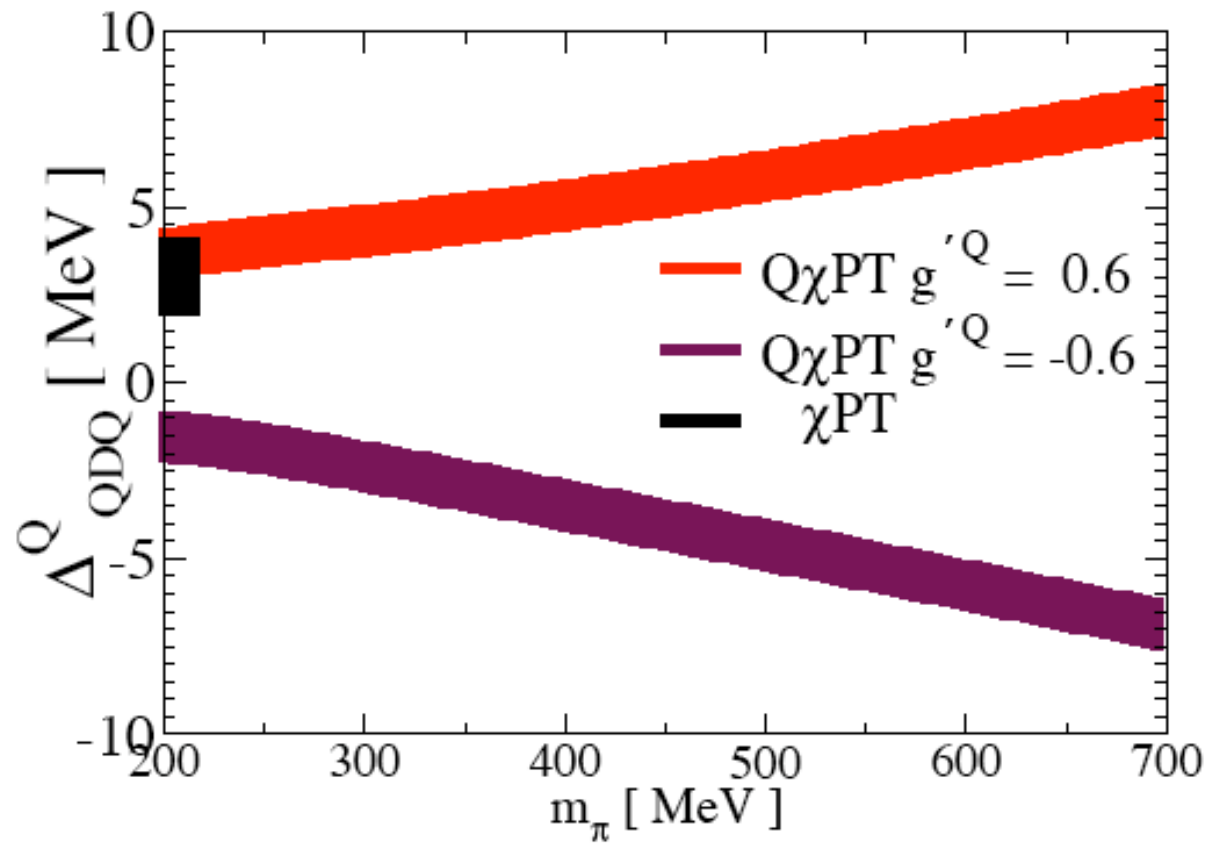
- Small Corrections ( $< 10$  MeV) to Quark-Diquark Symmetry Prediction for hyperfine splittings



$$\delta\chi_{QDQ} = \left[ M_{\Xi^*}^{(3/2)} - M_{\Xi}^{(3/2)} - \frac{3}{4} \left( M_{P^*}^{(3/2)} - M_P^{(3/2)} \right) \right]_{\text{PQ}\chi\text{PT}}$$

$$- \left[ M_{\Xi^*}^{(3/2)} - M_{\Xi}^{(3/2)} - \frac{3}{4} \left( M_{P^*}^{(3/2)} - M_P^{(3/2)} \right) \right]_{\chi\text{PT}}$$

- Small Corrections in Quenched Theory as well



- Chiral Extrapolation For EM decays (PQQ $\chi$ PT)

$$\Gamma(\Xi_a^* \rightarrow \Xi_a \gamma) = \frac{4\alpha}{9} \left[ \left( \beta Q_a - \frac{Q'}{2m_Q} + \delta\beta_a \right)^2 + \frac{3}{4} E_\gamma^2 \left( \frac{\beta_{E2} Q_a}{m_Q \Lambda_\chi} + \delta\beta_{E2a} \right)^2 \right] \frac{M_\Xi}{M_{\Xi^*}} E_\gamma^3$$



- Expanding in  $\Delta/m_{GB}$  and keeping  $O(\sqrt{m_q})$  correction only, gives  $\lesssim 10\%$  error for physical meson masses

# Summary/Outlook

- Heavy Quark-Diquark Symmetry: useful for doubly heavy baryons

$$\bar{Q}\bar{Q}\bar{q} \leftrightarrow Q\bar{q}$$

- NRQCD required for doubly heavy baryons  
Quark-Diquark symmetry at lowest order in  $v$  expansion

- Chiral Lagrangians with Quark-Diquark Symmetry

predictions for  $\Xi_{cc}^* \rightarrow \Xi_{cc} + \gamma$  in conflict with SELEX

- Partially Quenched/Quenched Generalizations

light quark mass dependence of hyperfine splittings, em decays

- **Future Work**

ChPT: develop covariant formalism, apply to weak decays

NRQCD:  $v^2$ ,  $\alpha_s$  corrections

lattice studies: how heavy must quarks be  
for Q-DQ symmetry to hold?

# Extra Slides



- One loop mass corrections



$$\delta m_{\Xi_a^*} = \sum_{i,b} C_{ab}^i \frac{g^2}{16\pi^2 f^2} \left( \frac{5}{9} K(m_{\Xi_b^*} - m_{\Xi_a^*}, m_i, \mu) + \frac{4}{9} K(m_{\Xi_b} - m_{\Xi_a^*}, m_i, \mu) \right)$$

$$\delta m_{\Xi_a} = \sum_{i,b} C_{ab}^i \frac{g^2}{16\pi^2 f^2} \left( \frac{1}{9} K(m_{\Xi_b} - m_{\Xi_a}, m_i, \mu) + \frac{8}{9} K(m_{\Xi_b^*} - m_{\Xi_a}, m_i, \mu) \right)$$

$$\delta m_{H_a} = \sum_{i,b} C_{ab}^i \frac{g^2}{16\pi^2 f^2} K(m_{H_b^*} - m_{H_a}, m_i, \mu)$$

$$\delta m_{H_a^*} = \sum_{i,b} C_{ab}^i \frac{g^2}{16\pi^2 f^2} \left( \frac{1}{3} K(m_{H_b} - m_{H_a^*}, m_i, \mu) + \frac{2}{3} K(m_{H_b^*} - m_{H_a^*}, m_i, \mu) \right)$$

$$K(\delta, m) = (-2\delta^3 + 3m^2\delta) \ln\left(\frac{m^2}{\mu^2}\right) + 2\delta(\delta^2 - m^2) F\left(\frac{\delta}{m}\right) + 4\delta^3 - 5\delta m^2 \quad + \text{cntrtm.}$$

$$F(x) = 2 \frac{\sqrt{1-x^2}}{x} \left[ \frac{\pi}{2} - \text{Tan}^{-1} \left( \frac{x}{\sqrt{1-x^2}} \right) \right] \quad |x| < 1$$

$$= -2 \frac{\sqrt{x^2-1}}{x} \ln(x + \sqrt{x^2-1}) \quad |x| > 1$$

- $g = 0.6$ ,  $\Delta_H = 140$  MeV, double charm SU(3) splitting of  $\delta_s = 100$  MeV
- nonanalytic corrections to hyperfine splitting

$$\delta m_{\Xi_{cc}^*} - \delta m_{\Xi_{cc}} = \begin{cases} -7.0 \text{ MeV} & \mu = 500 \text{ MeV} \\ 8.1 \text{ MeV} & \mu = 1000 \text{ MeV} \\ 16.9 \text{ MeV} & \mu = 1500 \text{ MeV} \end{cases}$$

$$\delta m_{\Xi_{cc}^*} - \delta m_{\Xi_{cc}} - \frac{3}{4}(\delta m_{D^*} - \delta m_D) = \begin{cases} 3.9 \text{ MeV} & \mu = 500 \text{ MeV} \\ 5.3 \text{ MeV} & \mu = 1000 \text{ MeV} \\ 6.1 \text{ MeV} & \mu = 1500 \text{ MeV} \end{cases}$$

- $\mu$  dependence cancelled by counterterms (not included)
- nonanalytic chiral corrections small

# Excited Doubly Heavy Baryons

- Light quark excitation energies

$$m_{D'} - m_D \sim 425 \text{ MeV} \quad m_{D'_s} - m_{D_s} \approx 350 \text{ MeV}$$

- P-wave  $\bar{c}\bar{c}$  diquark excitations

$$\Xi_{cc}^{P*}, \Xi_{cc}^P, \quad J^P = \frac{3}{2}^+, \frac{1}{2}^+ \quad \vec{S}_{cc} = 0 \quad \text{heavy quark singlets}$$

$$V_{cc} = \frac{1}{2} V_{c\bar{c}} \quad m_{\Xi^P} - m_{\Xi} = 225 \text{ MeV} \approx \frac{m_{h_c} - m_{J/\psi}}{2}$$

(numerical estimate from relativistic quark models)

- Lowest mass excited double charm baryons are diquark excitations

- **S-wave Strong Decays**

$$\Gamma[\Xi_{cc}^{\mathcal{P}*} \rightarrow \Xi_{cc}^* \pi] = \frac{\lambda_{3/2}^2}{2\pi f^2} \left( \frac{1}{2} E_{\pi^0}^2 p_{\pi^0} + E_{\pi^+}^2 p_{\pi^+} \right) \frac{m_{\Xi^*}}{m_{\Xi^{\mathcal{P}*}}} = \lambda_{3/2}^2 111 \text{ MeV}$$

$$\Gamma[\Xi_{cc}^{\mathcal{P}} \rightarrow \Xi_{cc} \pi] = \frac{\lambda_{1/2}^2}{2\pi f^2} \left( \frac{1}{2} E_{\pi^0}^2 p_{\pi^0} + E_{\pi^+}^2 p_{\pi^+} \right) \frac{m_{\Xi}}{m_{\Xi^{\mathcal{P}}}} = \lambda_{1/2}^2 111 \text{ MeV}.$$

- $\lambda_{1/2}, \lambda_{3/2} \sim \frac{\Lambda_{\text{QCD}}}{m_c}$  **Relatively narrow states ?**

- radial  $\bar{c}c$  diquark excitations

$$\Xi'_{cc}, \Xi'_{cc} \quad J^P = \frac{3}{2}^-, \frac{1}{2}^- \quad \text{heavy quark doublet}$$

$$m_{\Xi'} - m_{\Xi} = 300 \text{ MeV} \approx \frac{m_{\psi'} - m_{J/\psi}}{2}$$

(numerical estimate from relativistic quark models)

- P-wave Strong Decays**  $\tilde{g} \sim 1$  unknown coupling constant

Assume  $m_{\Xi} = 3440 \text{ MeV}$ ,  $m_{\Xi^*} = 3520 \text{ MeV}$

$$\Gamma[\Xi'_{cc}] = \tilde{g}^2 336 \text{ MeV}$$

$$\Gamma[\Xi'^*_{cc}] = \tilde{g}^2 78 \text{ MeV}$$

$$\frac{\Gamma[\Xi'^*_{cc} \rightarrow \Xi^*_{cc} \pi]}{\Gamma[\Xi'^*_{cc} \rightarrow \Xi_{cc} \pi]} = 0.56$$

$$\frac{\Gamma[\Xi'_{cc} \rightarrow \Xi^*_{cc} \pi]}{\Gamma[\Xi'_{cc} \rightarrow \Xi_{cc} \pi]} = 2.3$$

# Summary

- Heavy Quark-Diquark Symmetry: useful handle on doubly heavy baryons

$$\bar{Q}\bar{Q}\bar{q} \leftrightarrow Q\bar{q}$$

- NRQCD required for doubly heavy baryons

Quark-Diquark symmetry at lowest order in  $v$  expansion

$$m_{\Xi^*} - m_{\Xi} = \frac{3}{4}(m_{P^*} - m_P)$$

pNRQCD from vNRQCD

- Chiral Lagrangian with Quark-Diquark symmetry

new symmetry predictions:

em decays, chiral mass corrections

strong decays of excited states

- More experimental results in near future ...?