



$B \rightarrow \eta^{(\prime)} h^{(*)}$

Jan Schümann, KEK  
(for the Belle Collaboration)

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Hawaii

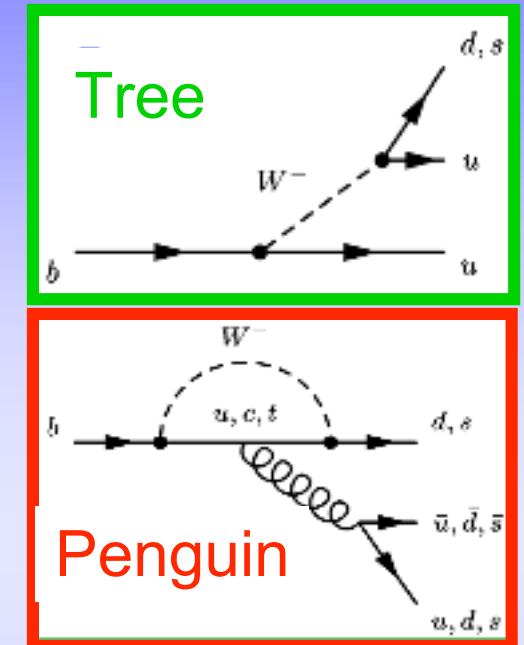


# Outline

- Introduction
- Experiment / Analysis overview
- Results
  - $\eta K^+$ ,  $\eta K^0$                       update with **500 fb<sup>-1</sup>**
  - $\eta \pi^+$                               update with **500 fb<sup>-1</sup>**
  - $\eta K^{*+}$ ,  $\eta K^{*0}$                       update with **414 fb<sup>-1</sup>**
  - $\eta \rho^+$ ,  $\eta \rho^0$                               **414 fb<sup>-1</sup>**
  - $\eta'$   $h^*$  with  $h^* = \rho^+, \rho^0, \phi, \eta, \eta'$  or  $\omega$       **500 fb<sup>-1</sup>**
- Summary

# Introduction

- Charmless two-body B decays  
⇒ B decay dynamics, CP violation
- Decay amplitudes dominated by
  - $b \rightarrow u$  Tree (T) CKM suppressed ( $|V_{ub}| \ll |V_{cb}|$ )
  - $b \rightarrow d,s$  Penguin (P) loop suppressed



- Interference b/w two decay amplitudes T and P  
⇒ Direct CPV:

$$A_{CP} = \frac{\Gamma(\bar{B} \rightarrow \bar{f}) - \Gamma(B \rightarrow f)}{\Gamma(\bar{B} \rightarrow \bar{f}) + \Gamma(B \rightarrow f)} = \frac{2r \sin\phi \sin\delta}{1 + r^2 + 2r \cos\phi \cos\delta}, \quad r = \frac{|P|}{|T|}$$

- Large CPV:
  - expected in SM for decays with similar T and P contributions
  - possible through New Physics



# Introduction

- Flavour singlet penguin
- Ratio charged / neutral  
⇒ additional SU(3) singlet contribution ?
- Close to theory expectations for unobserved decays
- New physics effects possible



# Introduction

- Theory expectation: Nucl.Phys. B675:333-415 (2003)

- $50 \times 10^{-6} B \rightarrow \eta' K$
- $11 \times 10^{-6} B \rightarrow \eta K^*$
- $4 \times 10^{-6} B \rightarrow \eta' K^*$
- $1 \times 10^{-6} B \rightarrow \eta K$

dominant, mixing enhanced  
 $b \rightarrow s$  penguin dominant

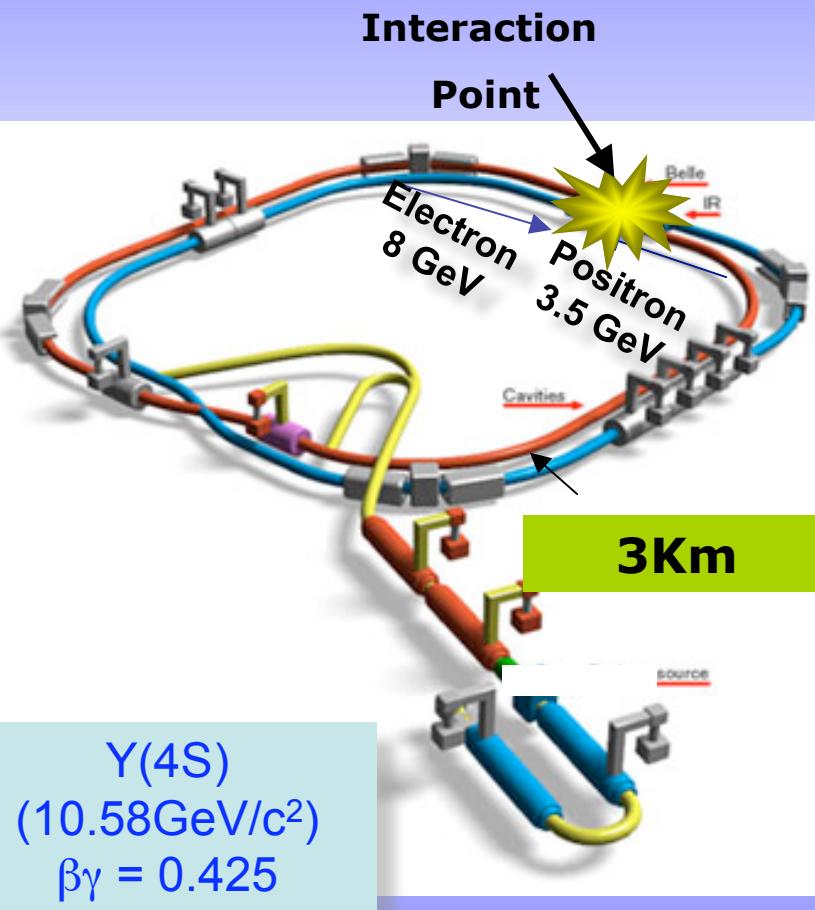
Charm/non-charm  
Interference  $\eta$

charged > neutral  $\rightarrow$  additional SU(3)  
singlet contrib. ?

$9 \times 10^{-6} B \rightarrow \eta \rho^+$
$6 \times 10^{-6} B \rightarrow \eta' \rho^+$
$5 \times 10^{-6} B \rightarrow \eta \pi^+$
$3 \times 10^{-6} B \rightarrow \eta' \pi^+$



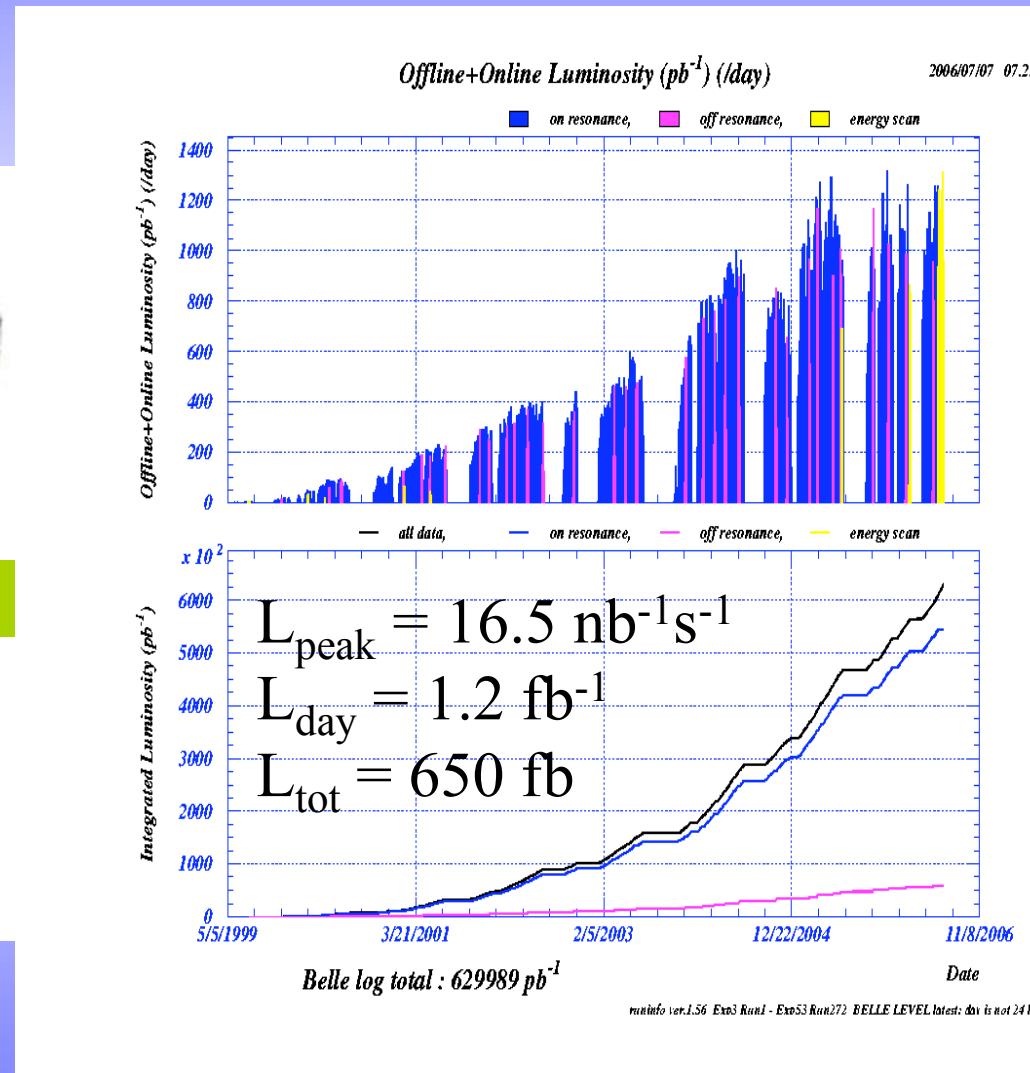
# KEKB



JPS/DPF 2006, 1. November

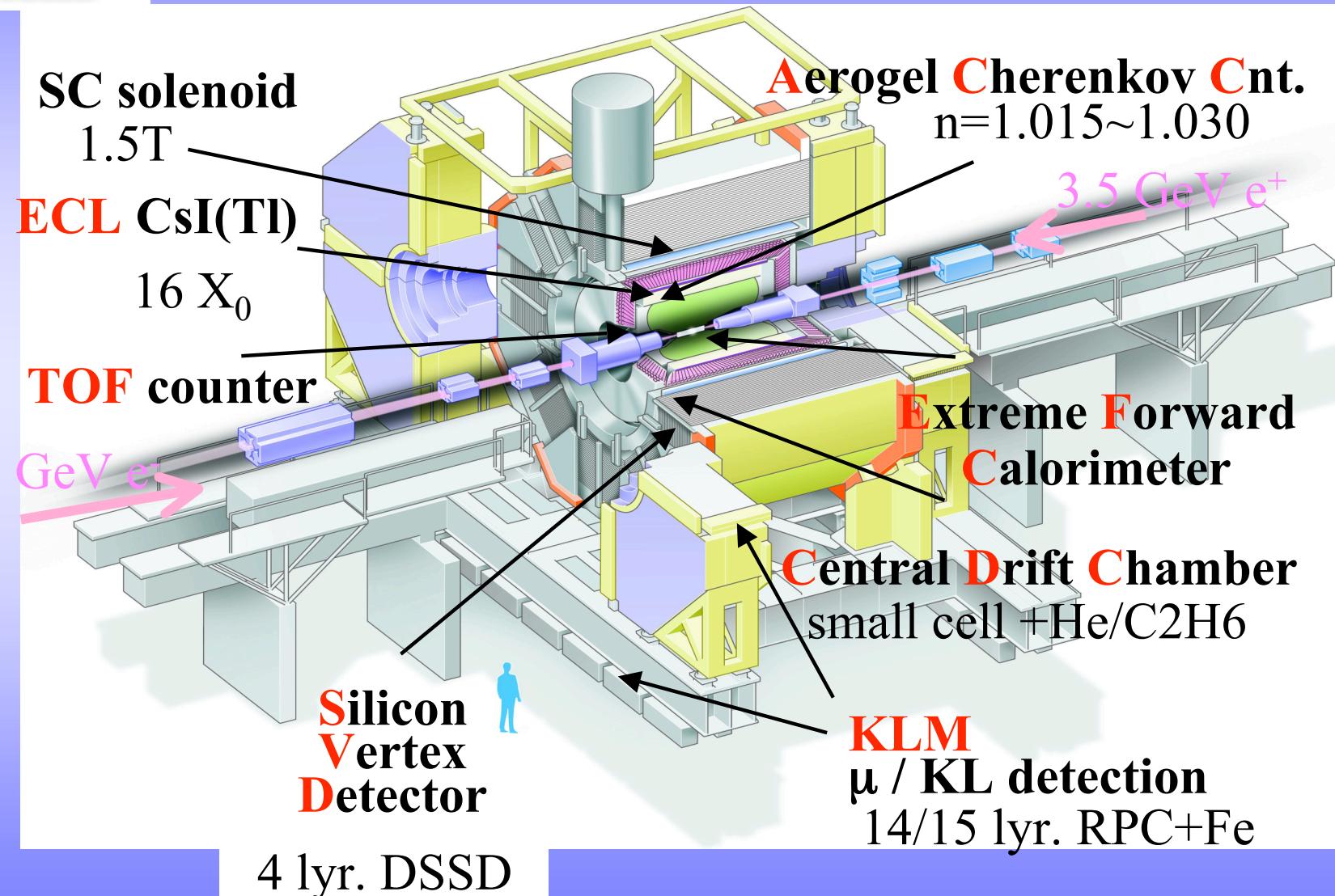
$B \rightarrow \eta^{(\prime)} h^{(*)}$  at Belle

Jan Schümann, KEK





# Belle Detector





# B reconstruction

$B \rightarrow \eta \pi^+$

Two kinematic variables:

$$M_{bc} = \sqrt{(E_{beam}^*)^2 - p_B^2}$$

or

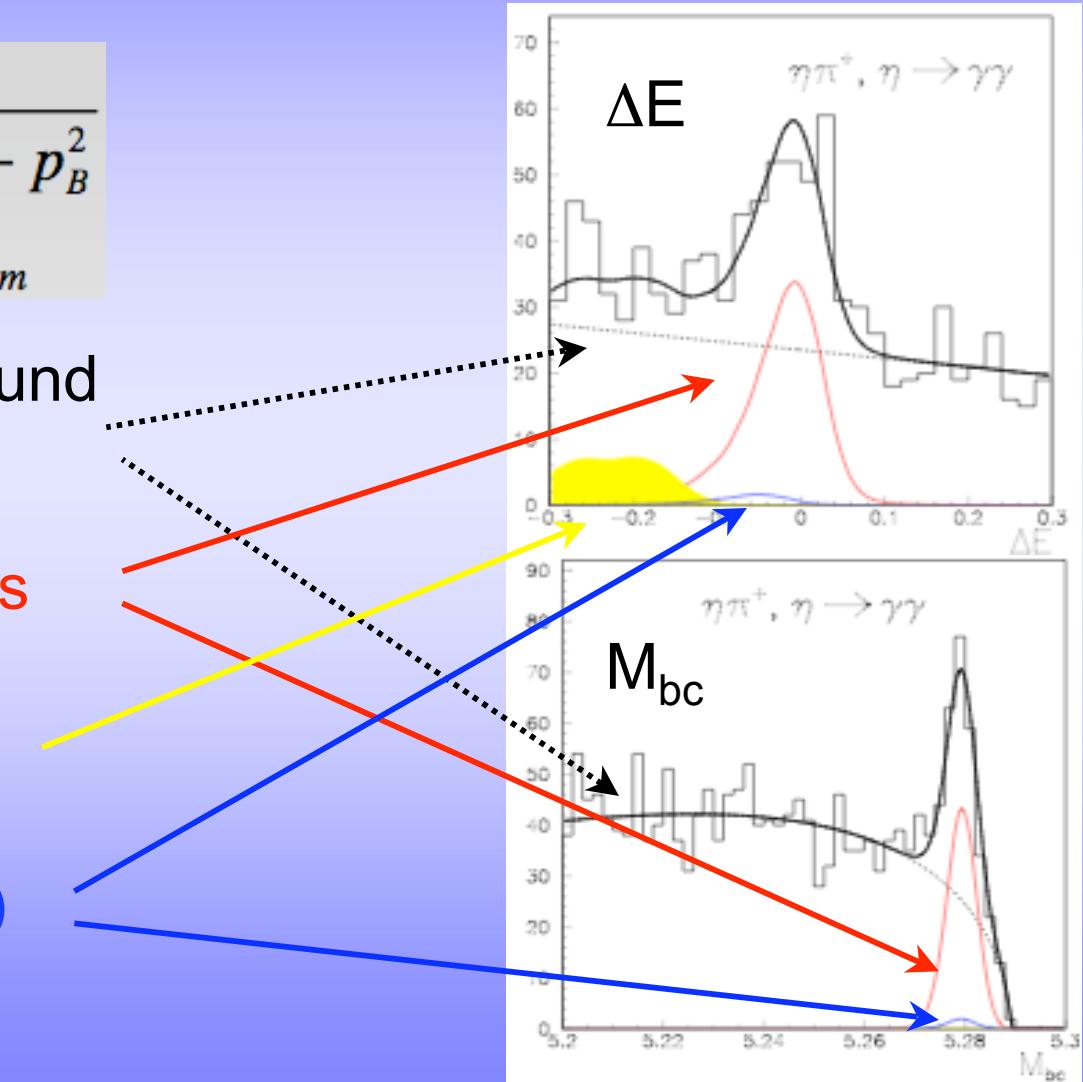
$$\Delta E = E_B - E_{beam}^*$$

Continuum background  
(dominant)

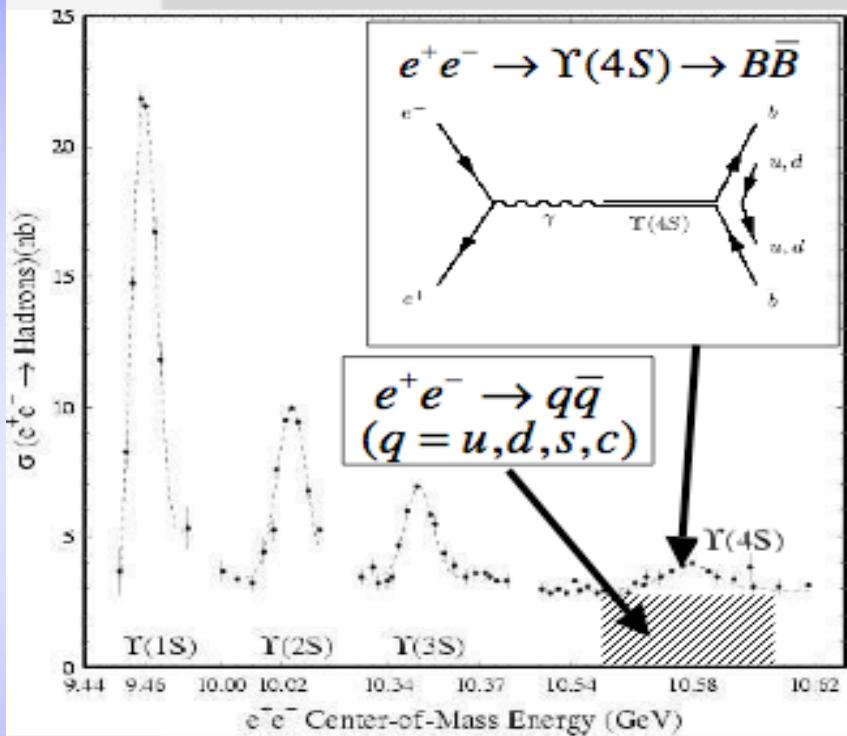
Signal events

Rare B decays  
(well understood)

K/ $\pi$  reflection (PID)

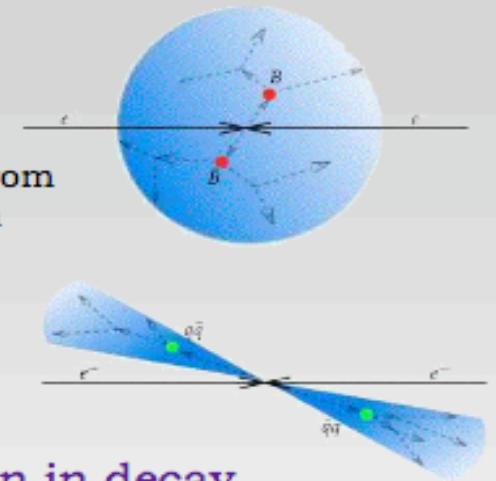


# Background suppression

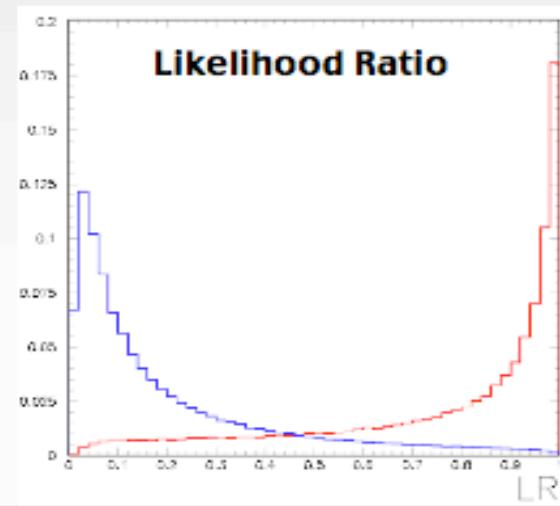


→ Event topology

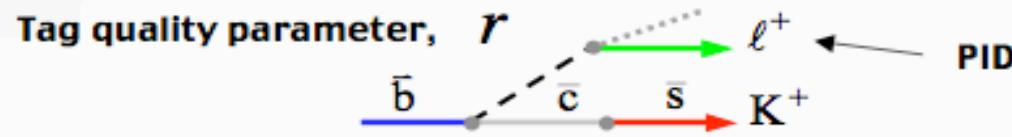
Fisher discriminant from modified Fox-Wolfram moments.



→  $J^P$  conservation in decay  
B flight direction variable,  $\cos\theta_B$



→ B-flavour tagging information





# Results

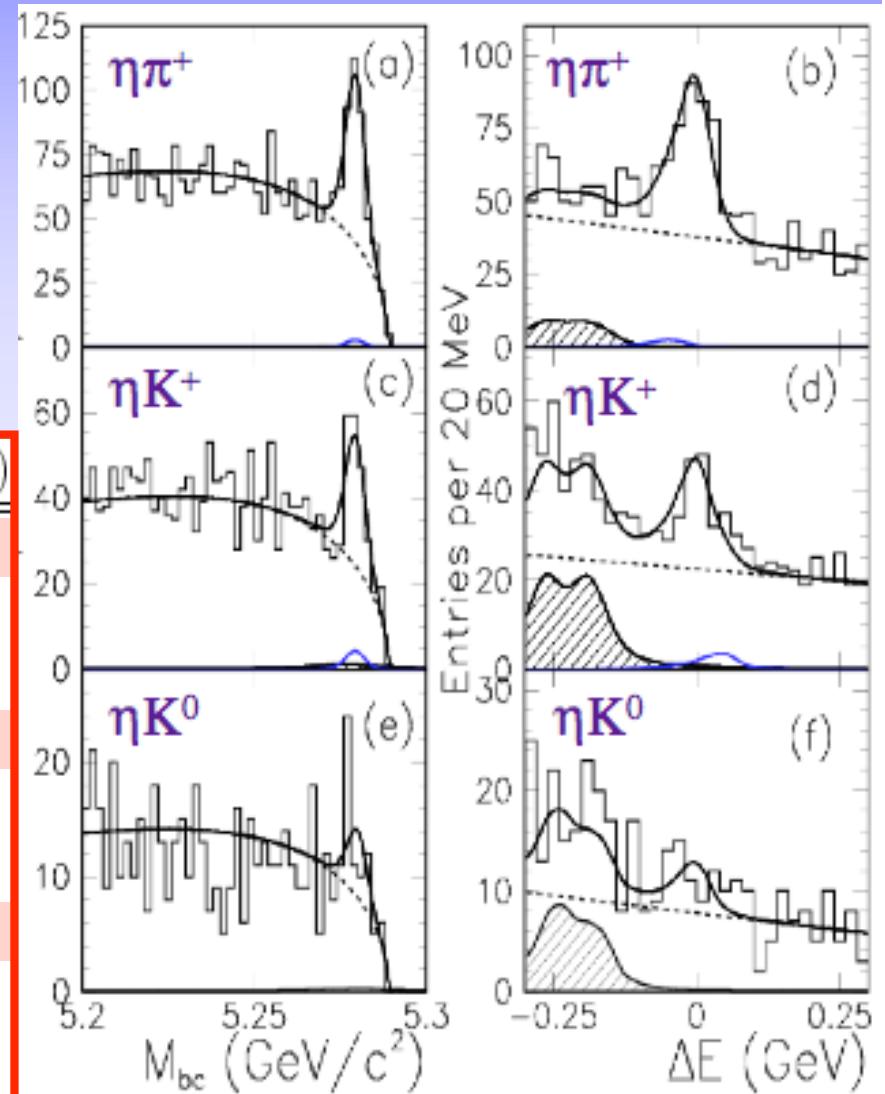


$$B \rightarrow \eta h$$

$\eta K$ :  $b \rightarrow s$  penguin,  $b \rightarrow u$  tree  
 $\eta \pi$ :  $b \rightarrow u$  tree, ( $b \rightarrow d$  penguin)

- Unbinned max. likelihood fit to  $(\Delta E, M_{bc})$
- $\eta \rightarrow \gamma\gamma / \eta \rightarrow \pi^+\pi^-\pi^0$  decays

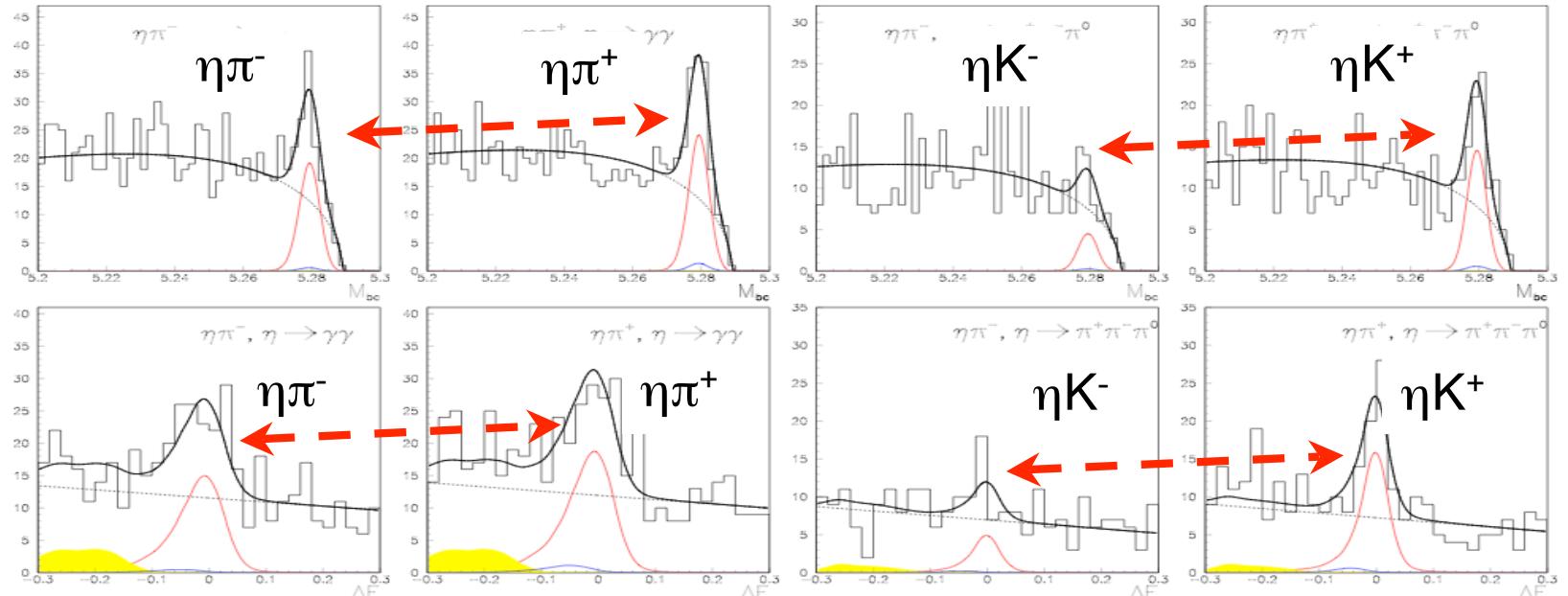
Mode	$\epsilon(\%)$	Yield	Sig.	$\mathcal{B}(10^{-6})$	UL( $10^{-6}$ )
$B^\pm \rightarrow \eta \pi^\pm$			15.0	$4.2 \pm 0.4 \pm 0.2$	
$\eta_{\gamma\gamma} \pi^\pm$	8.32	$182.7^{+20.2+4.8}_{-19.5-5.4}$	12.1	$4.1^{+0.5}_{-0.4} \pm 0.2$	
$\eta_{3\pi} \pi^\pm$	3.11	$73.1^{+12.6+2.2}_{-11.8-2.6}$	8.8	$4.4^{+0.8}_{-0.7} \pm 0.3$	
$B^\pm \rightarrow \eta K^\pm$			8.1	$1.9 \pm 0.3^{+0.2}_{-0.1}$	
$\eta_{\gamma\gamma} K^\pm$	7.29	$71.7^{+14.3+4.4}_{-13.4-3.1}$	6.5	$1.9^{+0.4}_{-0.3} \pm 0.1$	
$\eta_{3\pi} K^\pm$	2.66	$28.8^{+8.4}_{-7.6} \pm 1.8$	4.9	$2.0^{+0.6}_{-0.4} \pm 0.2$	
$B^0 \rightarrow \eta K^0$			2.9	$1.1 \pm 0.4 \pm 0.1$	$< 1.9$
$\eta_{\gamma\gamma} K^0$	2.68	$16.4^{+8.4}_{-7.7} \pm 1.0$	2.6	$1.1^{+0.6}_{-0.5} \pm 0.1$	$< 2.2$
$\eta_{3\pi} K^0$	1.01	$4.6^{+4.6}_{-3.7} \pm 0.3$	1.2	$0.9^{+0.9}_{-0.7} \pm 0.1$	$< 2.4$





$B \rightarrow \eta \ h \ A_{CP}$

535 Mio  $B\bar{B}$



Mode	$A_{CP}$
$B^\pm \rightarrow \eta \pi^\pm$	$-0.23 \pm 0.09 \pm 0.02$
$\eta_{\gamma\gamma} \pi^\pm$	$-0.11 \pm 0.11 \pm 0.01$
$\eta_{3\pi} \pi^\pm$	$-0.52 \pm 0.16 \pm 0.02$
$B^\pm \rightarrow \eta K^\pm$	$-0.39 \pm 0.16 \pm 0.03$
$\eta_{\gamma\gamma} K^\pm$	$-0.30 \pm 0.19 \pm 0.02$
$\eta_{3\pi} K^\pm$	$-0.55^{+0.27+0.05}_{-0.28-0.04}$

2.5  $\sigma$  from zero

2.4  $\sigma$  from zero

} Need more statistics



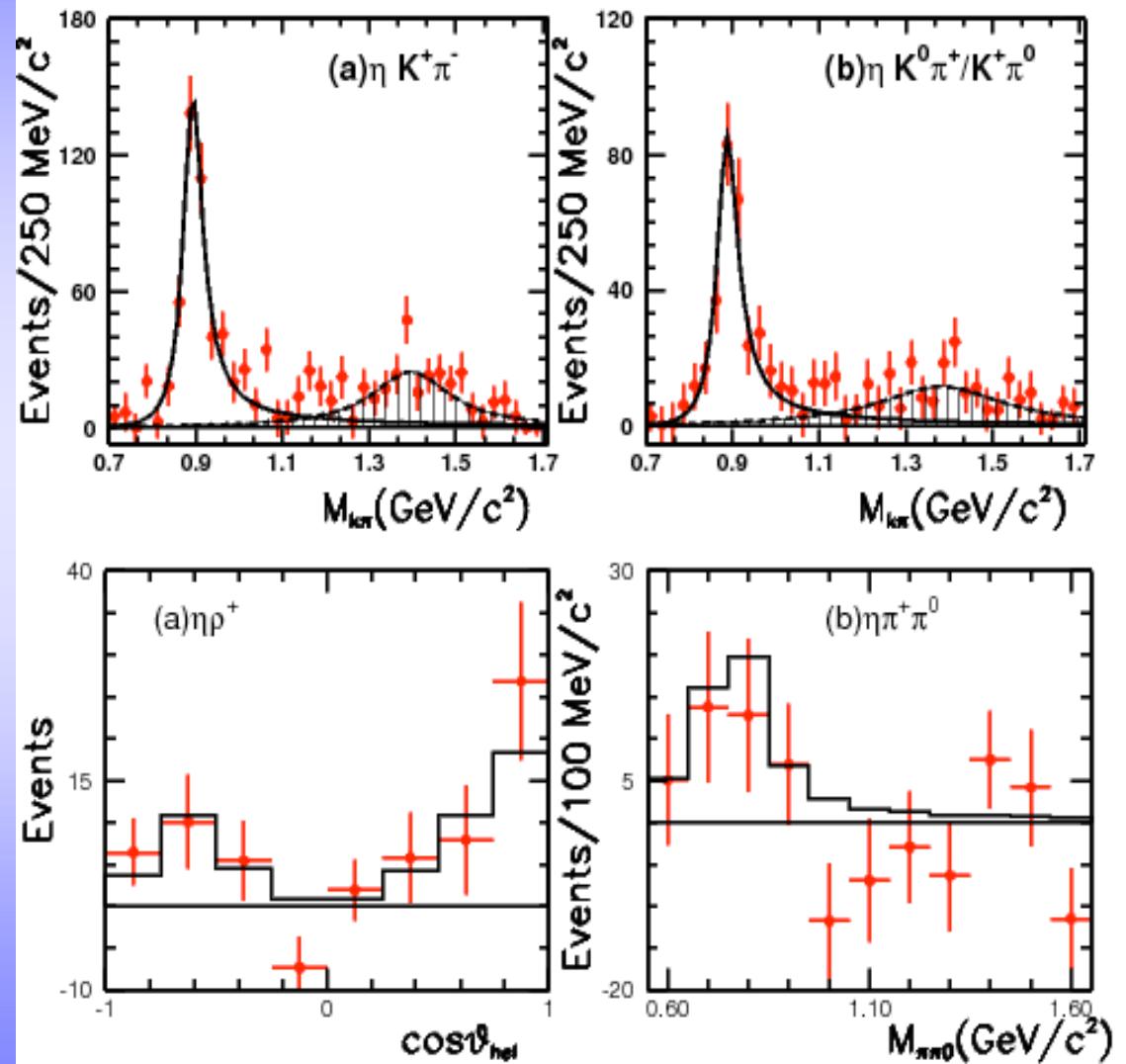
$B \rightarrow \eta h^*$

$\eta K^*$ : b $\rightarrow$ s penguin

$\eta \rho$ : b $\rightarrow$ u tree

# $K^*$ purity / $\rho$ consistent

- Study non  $K^*$  resonant behaviour
- Scan wide mass range
- Correct branching fraction
- Clear  $\rho$  helicity structure
- Consistent with expectation
- No significant non-resonant contribution



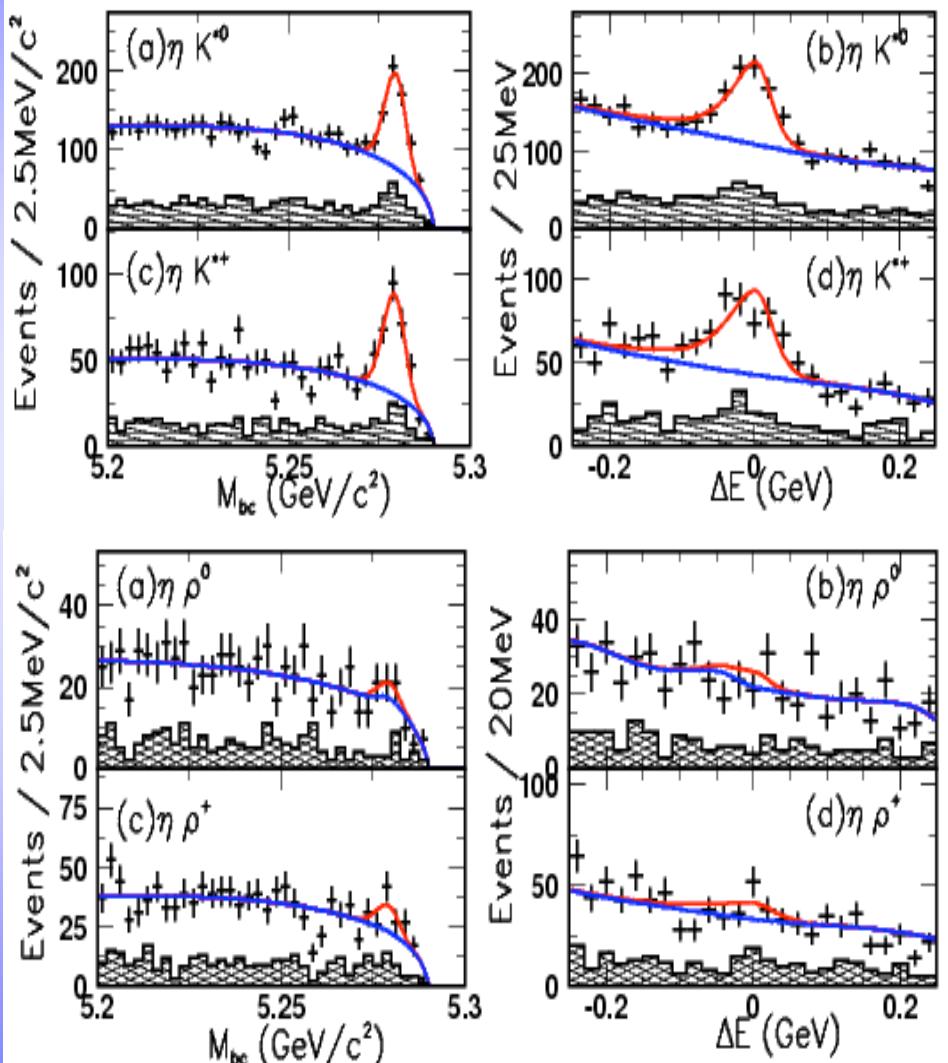


$B \rightarrow \eta h^*$

449 Mio  $B\bar{B}$

- Unbined max. likelihood fit to  $(\Delta E, M_b)$
- $\eta \rightarrow \gamma\gamma / \eta \rightarrow \pi^+\pi^-\pi^0$  decays
- $K^{*0} \rightarrow K^0\pi^0 / K^{*0} \rightarrow K^+\pi^-$

Mode	$N_S$	$\epsilon(\%)$	$\Sigma$	$\mathcal{B}(10^{-6})$
$\eta\gamma\gamma K_{K^+\pi^-}^{*0}$	$336.2^{+30.1}_{-29.2}$	16.9	14.2	$16.9^{+1.5}_{-0.9}$
$\eta\pi\pi\pi^0 K_{K^+\pi^-}^{*0}$	$93.4^{+14.6}_{-13.8}$	9.8	8.7	$14.1^{+2.2}_{-2.1}$
$\eta\gamma\gamma K_{K^0\pi^0}^{*0}$	$20.1^{+7.5}_{-6.7}$	2.1	3.6	$16.7^{+6.3}_{-5.6}$
$\eta\pi\pi\pi^0 K_{K^0\pi^0}^{*0}$	$9.5^{+5.0}_{-4.2}$	1.3	2.6	$21.6^{+11.5}_{-9.7}$
$\eta K^{*0}$	-	-	17.1	$16.1 \pm 1.2$
$\eta\gamma\gamma K_{K^+\pi^0}^{*+}$	$79.8^{+16.1}_{-15.3}$	6.7	6.1	$20.1^{+4.1}_{-3.9}$
$\eta\pi\pi\pi^0 K_{K^+\pi^0}^{*+}$	$24.1^{+8.7}_{-7.9}$	4.2	3.5	$17.0^{+6.1}_{-5.6}$
$\eta\gamma\gamma K_{K^0\pi^+}^{*+}$	$120.3^{+16.2}_{-15.4}$	4.5	10.1	$22.6^{+3.1}_{-2.9}$
$\eta\pi\pi\pi^0 K_{K^0\pi^+}^{*+}$	$29.2^{+7.3}_{-6.6}$	2.6	6.2	$17.0^{+4.8}_{-3.8}$
$\eta K^{*+}$	-	-	13.8	$20.3^{+2.0}_{-1.9}$
$\eta\gamma\gamma\rho^0$	$19.5^{+11.3}_{-10.4}$	8.9	2.1	$1.25^{+0.73}_{-0.67}$
$\eta\pi\pi\pi^0\rho^0$	$0.9^{+4.6}_{-3.9}$	5.5	0.2	$0.17^{+0.84}_{-0.66}$
$\eta\rho^0$	-	-	1.6	$0.84^{+0.56}_{-0.51} (< 1.5)$
$\eta\gamma\gamma\rho^+$	$38.1^{+16.1}_{-15.2}$	5.5	2.6	$3.9^{+1.7}_{-1.6}$
$\eta\pi\pi\pi^0\rho^+$	$15.8^{+8.9}_{-8.0}$	3.50	2.1	$4.4^{+2.5}_{-2.2}$
$\eta\rho^+$	-	-	3.4	$4.1^{+1.4}_{-1.3}$



# $B \rightarrow \eta \ h^* \ A_{CP}$

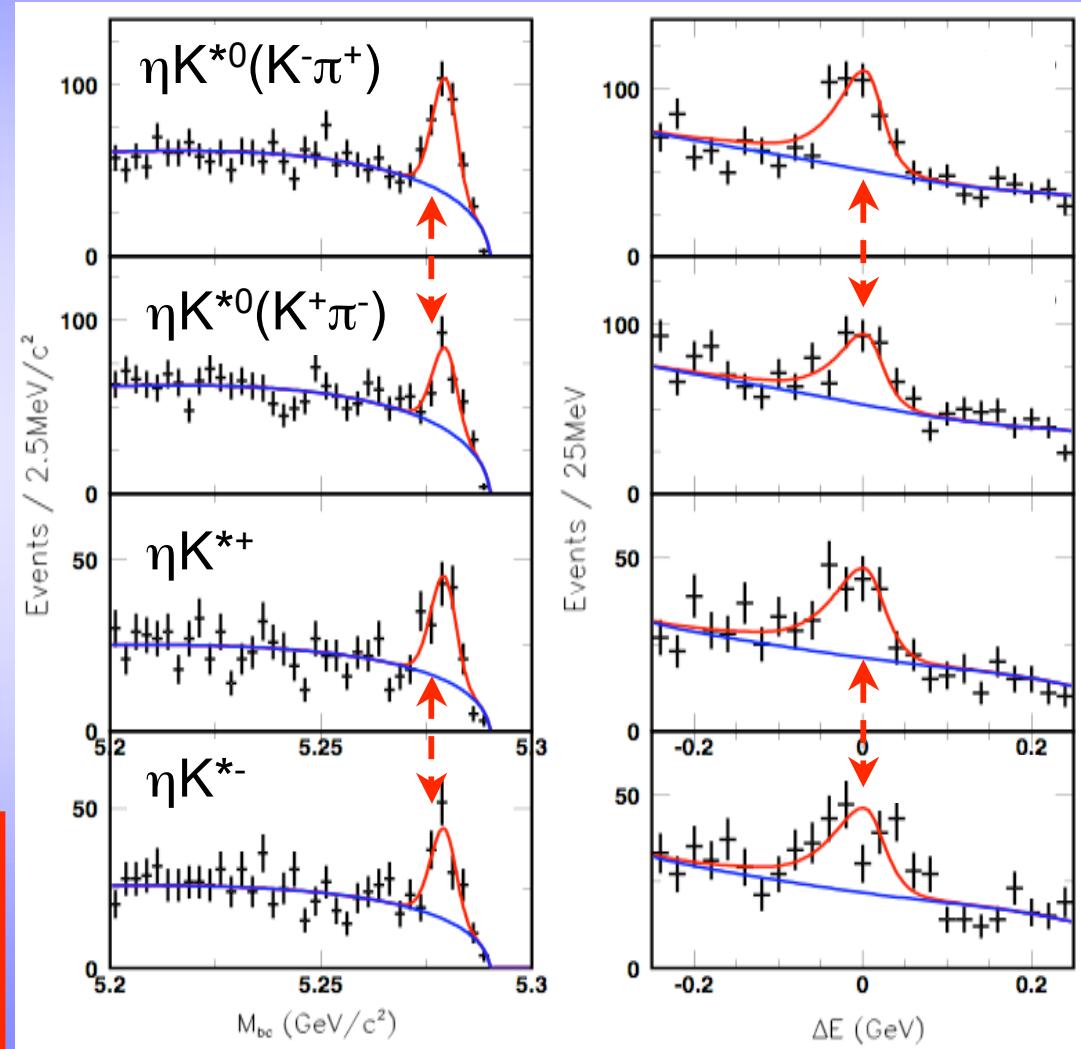
- Consistent with **no**  $A_{CP}$  asymmetry
- Consistent with SM

$\eta K^{*0}$	$\mathcal{A}_{cp}$	$\mathcal{A}_{cp,qq}$
$\eta_{2\gamma}$	$0.21 \pm 0.09$	$-0.023 \pm 0.089$
$\eta_{3\pi}$	$-0.06 \pm 0.15$	$-0.025 \pm 0.015$
$\eta K_{K^+\pi^0}^{*+}$	$\mathcal{A}_{cp}$	$\mathcal{A}_{cp,qq}$
$\eta_{2\gamma}$	$-0.04 \pm 0.19$	$-0.019 \pm 0.020$
$\eta_{3\pi}$	$0.37 \pm 0.33$	$-0.043 \pm 0.031$
$\eta K_{K^-\pi^+}^{*+}$	$\mathcal{A}_{cp}$	$\mathcal{A}_{cp,qq}$
$\eta_{2\gamma}$	$-0.08 \pm 0.13$	$-0.012 \pm 0.020$
$\eta_{3\pi}$	$0.28 \pm 0.23$	$0.035 \pm 0.036$
$\eta \rho^+$	$\mathcal{A}_{cp}$	$\mathcal{A}_{cp,qq}$
$\eta_{2\gamma}$	$-0.36^{+0.41}_{-0.48}$	$-0.030 \pm 0.017$
$\eta_{3\pi}$	$0.55^{+0.78}_{-0.53}$	$-0.023 \pm 0.027$

$$\mathcal{A}_{cp}(\eta K^{*0}) = 0.174 \pm 0.076 \pm 0.01,$$

$$\mathcal{A}_{cp}(\eta K^{*+}) = 0.032 \pm 0.095 \pm 0.01,$$

$$\mathcal{A}_{cp}(\eta \rho^+) = -0.040^{+0.34}_{-0.32} \pm 0.01.$$





$B \rightarrow \eta' h$

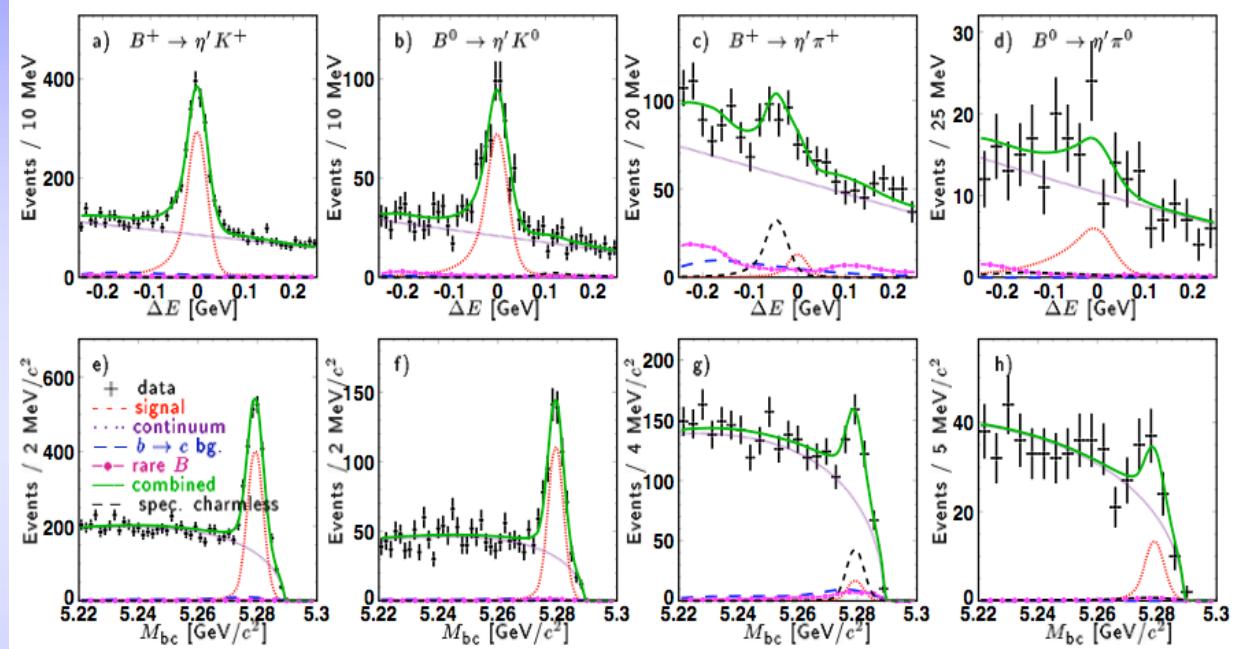
(published, PRL 97,061802)

$\eta' K$  :  $b \rightarrow s$  penguin  
 $\eta' \pi$  :  $b \rightarrow u$  tree



# $B \rightarrow \eta' h$

- $\eta' \rightarrow \eta\pi^+\pi^- / \eta' \rightarrow \rho\gamma$  decays
- Extended unbinned likelihood fit
- First evidence of  $B \rightarrow \eta' \pi^0$**
- $A_{CP}$  included in fit



	$B^+ \rightarrow \eta' K^+$	$B^0 \rightarrow \eta' K^0$	$B^+ \rightarrow \eta' \pi^+$	$B^0 \rightarrow \eta' \pi^0$
$N_S$	$1895.7 \pm 59.5$	$515.3 \pm 31.7$	$39.0 \pm 13.2$	$35.8 \pm 12.7$
$N_{tot}$	25281	6044	8411	1345
$\mathcal{B}[10^{-6}]$	$69.2 \pm 2.2 \pm 3.7$	$58.9^{+3.6}_{-3.5} \pm 4.3$	$1.76^{+0.67+0.15}_{-0.62-0.14}$	$2.79^{+1.02+0.25}_{-0.96-0.34}$
$A_{CP}$	$0.028 \pm 0.028 \pm 0.021$	—	$0.20^{+0.37}_{-0.36} \pm 0.04$	—
$\sigma$	$> 10$	$> 10$	3.2	3.1



$B \rightarrow \eta' h^*$

$\eta' K^*$ : b $\rightarrow$ s penguin  
 $\eta' \rho$ : b $\rightarrow$ u tree

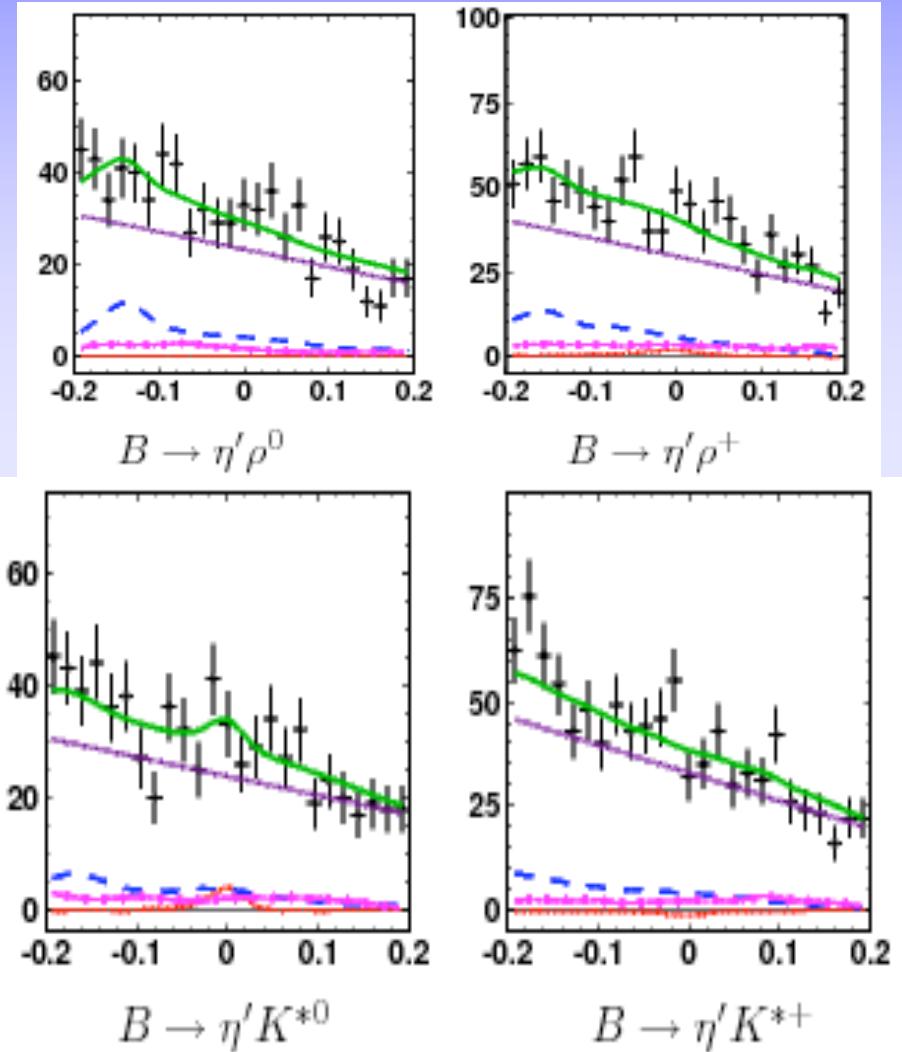


$B \rightarrow \eta^{(\prime)} h^*$

535 Mio  $B\bar{B}$

- $\eta' \rightarrow \eta\pi^+\pi^- / \eta' \rightarrow \rho\gamma$  decays
- No significant signal
- Extended unbinned likelihood fit
- 90% conf. level UL

	$N_S$	Upper limit ( $\times 10^{-6}$ )
$B \rightarrow \eta'\rho^0$	$0.1^{+0.2}_{-7.0}$	1.26
$B \rightarrow \eta'\rho^+$	$18.5^{+23.3}_{-21.7}$	4.7
$B \rightarrow \eta'K^{*0}$	$14.2^{+9.1}_{-8.0}$	2.6
$B \rightarrow \eta'K^{*+}$	$-6.4^{+10.9}_{-7.9}$	2.8





$$B \rightarrow \eta' h^*$$

$\eta\phi$ : A tree, penguin A

$\eta'\eta$ :  $b \rightarrow d$  penguin, C  $b \rightarrow u$  tree

$\eta'\eta'$ :  $b \rightarrow d$  penguin, C  $b \rightarrow u$  tree

$\eta'\omega$ : C  $b \rightarrow u$  tree

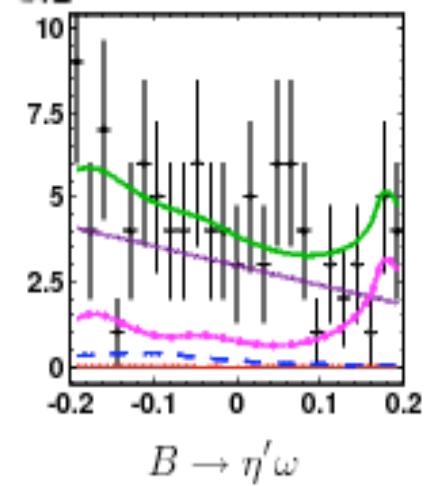
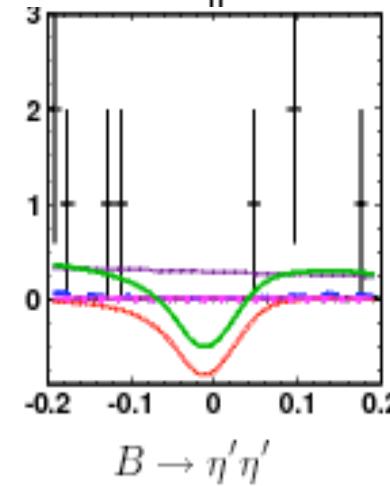
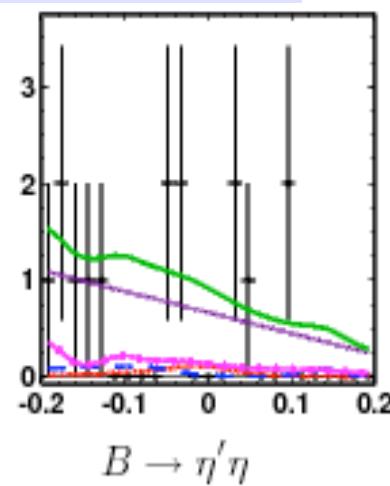
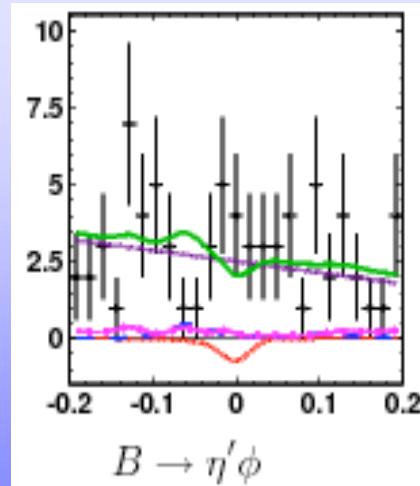


$B \rightarrow \eta^{(\prime)} h^*$

535 Mio  $B\bar{B}$

- $\eta' \rightarrow \eta\pi^+\pi^- / \eta' \rightarrow \rho\gamma$  decays
- No significant signal
- Extended unbinned likelihood fit
- 90% conf. level UL

	$N_S$	Upper limit ( $\times 10^{-6}$ )
$B \rightarrow \eta'\phi$	$-2.4^{+2.5}_{-3.5}$	0.5
$B \rightarrow \eta'\eta$	$1.0^{+4.6}_{-3.6}$	4.0
$B \rightarrow \eta'\eta'$	$-6.3^{+2.2}_{-2.1}$	7.7
$B \rightarrow \eta'\omega$	$0.9^{+6.3}_{-5.2}$	2.2





# Hirachy of $\eta/\eta'$ $h^{(*)}$

	Exp. (Belle)	[10 <sup>-6</sup> ]	Theory (Nucl.Phys. B675:333-415)
• $B \rightarrow \eta' K^+/K^0$	69 / 59	49 / 47	
• $B \rightarrow \eta K^{*+}/K^{*0}$	20 / 16	11 / 11	
• $B \rightarrow \eta \pi^+/\pi^0$	4 / --	5 / 0.3	
• $B \rightarrow \eta' \pi^+/\pi^0$	2 / 3	3 / 0.2	
• $B \rightarrow \eta K^+/K^0$	2 / 1	2 / 1	
• $B \rightarrow \eta' K^{*+}/K^{*0}$	<3 / <3	5 / 4	
• $B \rightarrow \eta \rho^+/\rho^0$	4 / <1.5	9 / 0.03	
• $B \rightarrow \eta' \rho^+/\rho^0$	<4 / <1	6 / 0.01	
• $B \rightarrow \eta' \text{other}$	< 4	< 0.4	



# Conclusion

- Updated results for  $B \rightarrow \eta K$  and  $B \rightarrow \eta \pi$
- Updated result for  $B \rightarrow \eta K^*$
- First evidence of  $B \rightarrow \eta \rho$
- New upper limits for  $B \rightarrow \eta' h^*$
- Now (nearly complete)  $B \rightarrow \eta^{(\prime)} h^{(*)}$  information available from Belle with  $> 414 \text{ fb}^{-1}$
- Good situation to study penguin and singlet contributions

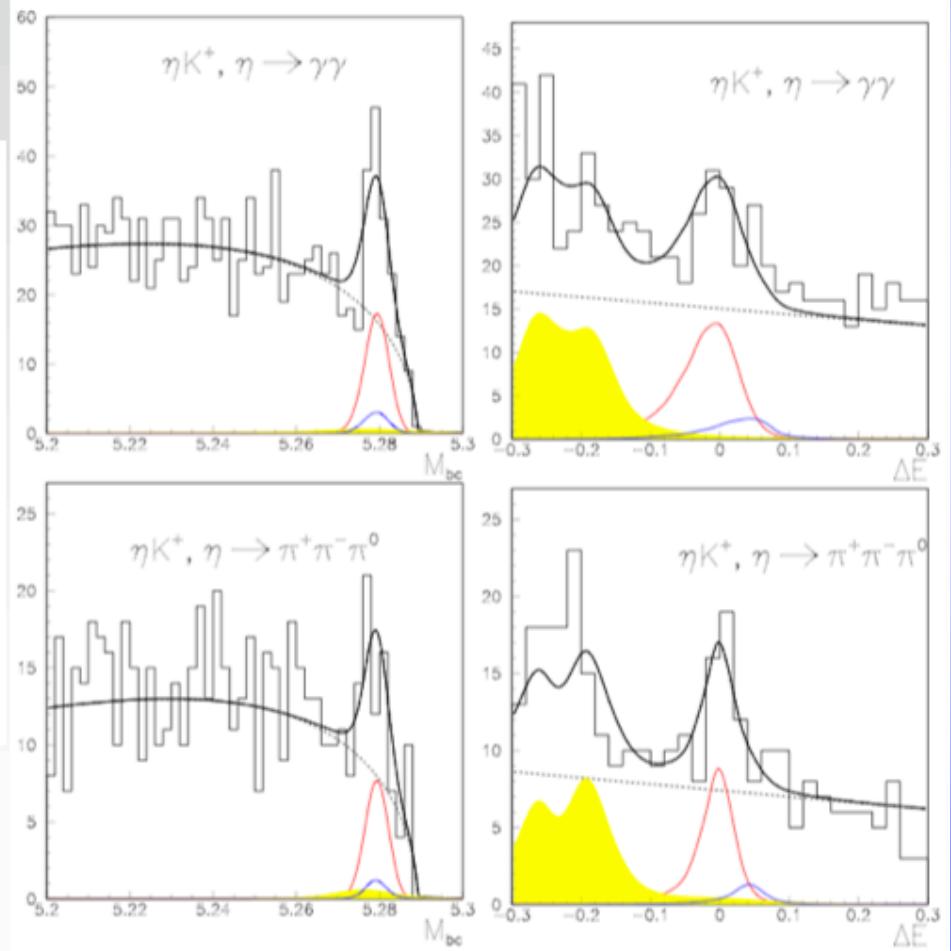


# Backup

# $B \rightarrow \eta' K^+$ breakdown

TABLE VII: Results of likelihood fit for  $B^\pm \rightarrow \eta K^\pm$

Mode	Yield	Eff.	Sig.	$\mathcal{B}$ ( $10^{-6}$ )	$A_{CP}$
$\gamma\gamma$	$71.7^{+14.3}_{-13.4}$	-	<b>6.9</b>	$1.85^{+0.37}_{-0.34}$	$-0.298^{+0.188}_{-0.191}$
SVDI	$26.6^{+7.6}_{-6.8}$	7.17%	-	-	-
SVDII	$45.1^{+12.1}_{-11.6}$	7.34%	-	-	-
$\pi^+\pi^-\pi^0$	$28.8^{+8.4}_{-7.6}$	-	<b>5.1</b>	$2.02^{+0.59}_{-0.54}$	$-0.549^{+0.273}_{-0.276}$
SVDI	$9.3^{+4.6}_{-3.8}$	2.72%	-	-	-
SVDII	$19.5^{+7.1}_{-6.6}$	2.64%	-	-	-

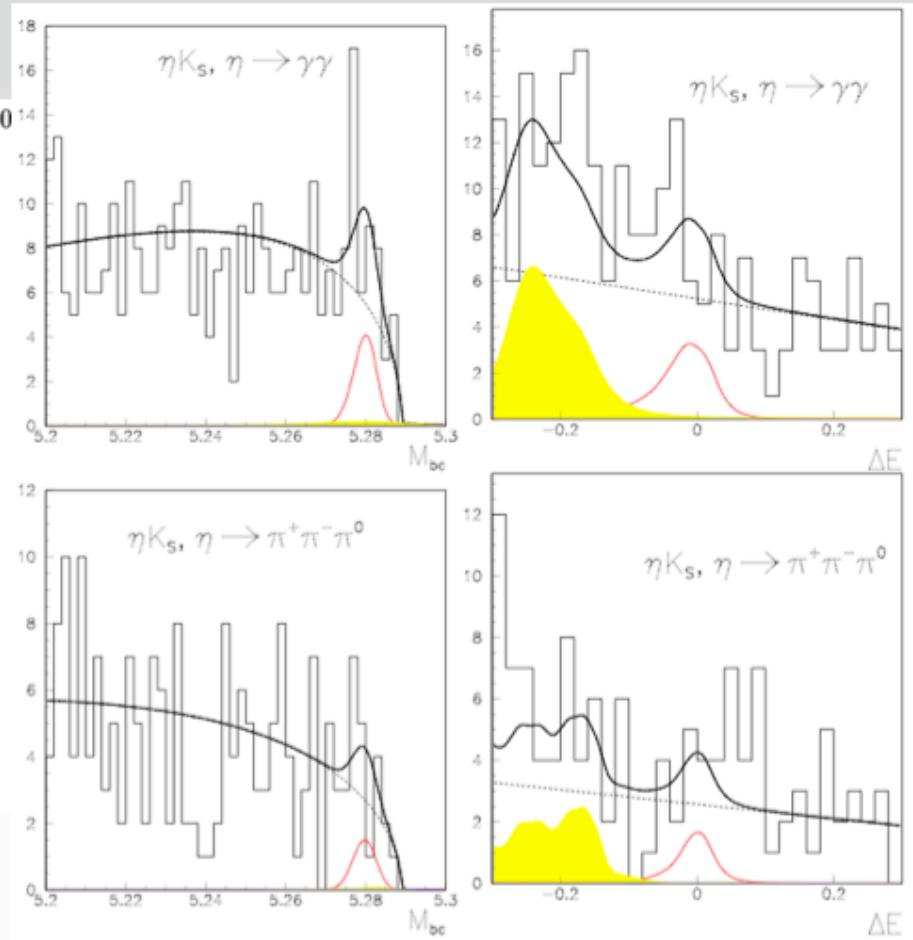




# $B \rightarrow \eta' K^0$ breakdown

TABLE IX: Results of likelihood fit for  $B^0 \rightarrow \eta K^0$

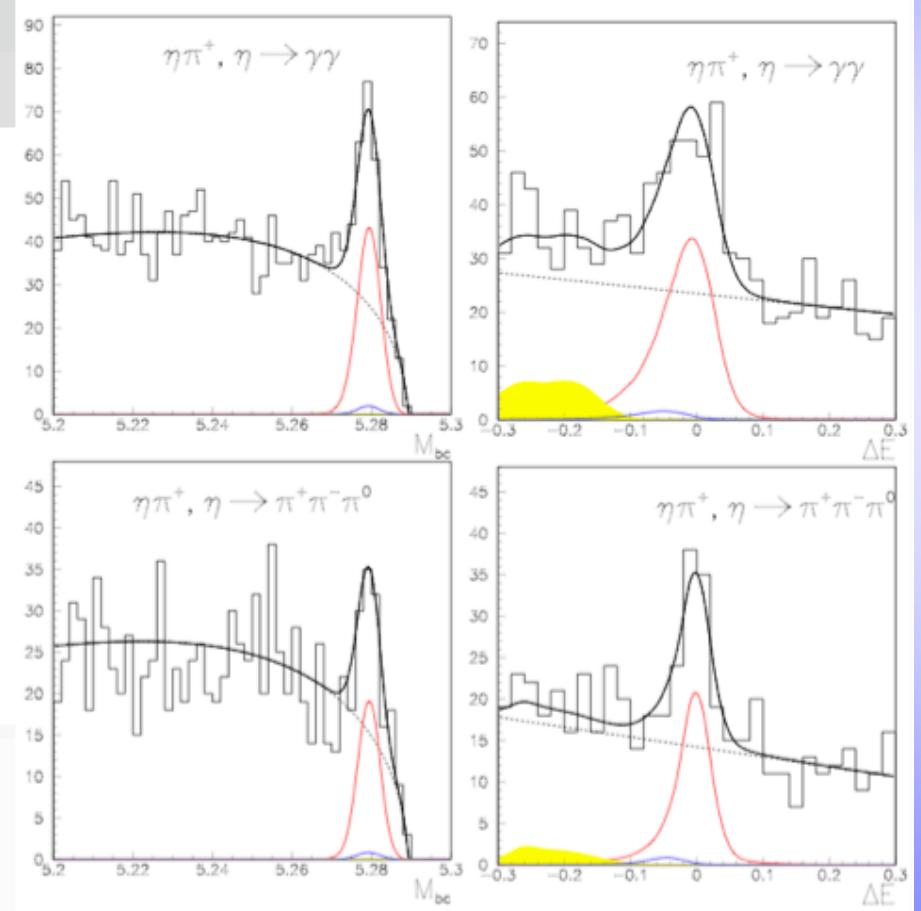
Mode	Yield	Eff.	Sig.	$\mathcal{B}$ ( $10^{-6}$ )
$\gamma\gamma$	$16.4^{+8.4}_{-7.5}$	—	<b>2.7</b>	$1.1^{+0.6}_{-0.5}$
SVDI	$0.4^{+4.3}_{-3.3}$	2.60%	-	—
SVDII	$16.0^{+7.3}_{-6.8}$	2.71%	—	—
$\pi^+\pi^-\pi^0$	$4.6^{+4.6}_{-3.7}$	-	<b>1.3</b>	$0.9^{+0.9}_{-0.7}$
SVDI	$1.2^{+2.6}_{-1.7}$	1.05%	—	—
SVDII	$3.4^{+3.8}_{-3.3}$	0.99%	—	—
Combined	-	-	2.1	$0.9 \pm 0.6$



$B \rightarrow \eta' \pi^+$ 

 TABLE IV: Results of likelihood fit for  $B^\pm \rightarrow \eta\pi^\pm$ 

Mode	Yield	Eff.	Sig.	$\mathcal{B}$ ( $10^{-6}$ )	$A_{CP}$
$\gamma\gamma$	$182.7^{+20.2}_{-19.5}$	—	12.1	$4.12^{+0.46}_{-0.44}$	$-0.114 \pm 0.106$
SVDI	$55.7^{+10.6}_{-9.9}$	8.23%	—	—	—
SVDII	$127.0^{+17.2}_{-16.8}$	8.36%	—	—	—
$\pi^+\pi^-\pi^0$	$73.1^{+12.6}_{-11.8}$	—	8.8	$4.42^{+0.76}_{-0.69}$	$-0.527 \pm 0.162$
SVDI	$16.3^{+6.1}_{-5.2}$	3.17%	—	—	—
SVDII	$56.9^{+11.0}_{-10.5}$	3.08%	—	—	—





# $\eta h^*$ Systematics

Table 16: Systematics for  $\eta\rho$ .

mode	$\eta_{2\gamma}\rho^0$ (%)	$\eta_{3\pi}\rho^0$ (%)	$<\eta\rho^0>$ (%)	$\eta_{2\gamma}\rho^+$ (%)	$\eta_{3\pi}\rho^+$ (%)	$<\eta\rho^+>$ (%)
Tracking	2	4	3.3	1	3	1.8
$\gamma\gamma, \pi^0$	2.0	4	3.2	4.5	5.7	4.8
$\eta$ mass cut	2.0	2	2	2.0	2.0	2
PID	1.3	1.8	1.6	0.8	1.3	0.8
$B_s$	0.66	1.77	1.4	0.66	1.77	0.8
$\rho$ mass cut	2	2	2	2	2	2
LR cut	2	2	2	2	2	2
non-resonance $\rho$	4	4	4	4	4	4
$N_{B\bar{B}}$	1	1	1	1	1	1
$\Sigma$	6.0	8.0	7.2	6.9	8.5	7.2
PDF	15.9	64.6	20.4	4.8	4.5	4.3
Total	17.0	65.0	21.6	8.5	9.6	8.0

Table 14: Systematics for  $\eta K^{*0}$ .

mode	$\eta_{2\gamma}K_{K^+\pi^-}^{*0}$ (%)	$\eta_{3\pi}K_{K^+\pi^-}^{*0}$ (%)	$\eta_{2\gamma}K_{K^0\pi^0}^{*0}$ (%)	$\eta_{3\pi}K_{K^0\pi^0}^{*0}$ (%)	$<\eta K^{*0}>$ (%)
TK, $K_s$	2	4	4.5	4.9	2.8
$\gamma\gamma, \pi^0$	2	4	4.5	5.7	2.8
$\eta$ mass cut	2	2	2	2	2
PID	1.4	1.6	-	1.1	1.4
LR	1.0	1.0	1.0	1.0	1.0
$K^*$ mass cut	2	2	2	2	2
$B_s$	0.66	1.77	0.66	1.77	1.0
non-resonance $K\pi$	0.5	0.5	0.5	0.5	0.5
$N_{B\bar{B}}$	1.0	1.0	1.0	1.0	1.0
$\Sigma$	4.5	6.9	7.1	8.4	4.3
Fitting PDF	$\pm 2.3$	2.5	2.6	4.6	2.1
Total	5.1	7.4	7.6	9.6	5.8

Table 15: Systematics for  $\eta K^{*+}$ .

mode	$\eta_{2\gamma}K_{K^-\pi^0}^{*+}$ (%)	$\eta_{3\pi}K_{K^-\pi^0}^{*+}$ (%)	$\eta_{2\gamma}K_{K^0\pi^+}^{*+}$ (%)	$\eta_{3\pi}K_{K^0\pi^+}^{*+}$ (%)	$<\eta K^{*+}>$ (%)
Tk, $K_s$	1	3	5.5	5.85	4.4
$\gamma\gamma, \pi^0$	4.5	5.7	2	4	3.5
$\eta$ mass cut	2	2	2	2	2
PID	1.1	1.3	0.8	1.3	1.0
$B_s$	0.66	1.77	0.66	1.77	1.0
$K^*$ mass cut	2	2	2	2	2
LR cut	1	1	1	1	1
non-resonance $K^*$	2	2	2	2	2
$N_{B\bar{B}}$	1	1	1	1	1
$\Sigma$	6.1	7.7	7.0	8.3	6.9
PDF	2.3	2.8	2.4	2.3	2.2
Total	6.5	8.2	7.4	8.6	7.2