

# Measurements of Exclusive Charmless $B$ Decays Related to $\Delta S_{\phi K^0}$ and $\Delta S_{\eta' K^0}$ at BaBar

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Representing the BABAR Collaboration

DPF 2006 & JPS 2006, Honolulu, Hawaii

October 29 - November 3, 2006



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## Modes Covered

- Modes covered and data sample used

Modes	Data ( $BB$ )	Reference
$B^0 \rightarrow \eta K^0, \eta\eta, \eta'\eta', \eta\phi, \eta'\phi$	324 M	PRD <b>74</b> , 051106(R) (2006)
$B^0 \rightarrow \eta\eta', \eta'\pi^0, \eta\pi^0$	232 M	PRD <b>73</b> , 071102(R) (2006)
$B \rightarrow \phi\pi$	232 M	PRD <b>74</b> , 011102(R) (2006)
$B^0 \rightarrow \bar{K}^{*0} K^0 \dagger$	232 M	PRD <b>74</b> , 072008 (2006)

† First search, others updates

- Submodes included:

$$\begin{array}{lll}
 K^0 \rightarrow K_S^0(\pi^+\pi^-) & \pi^0 \rightarrow \gamma\gamma & \phi \rightarrow K^+K^- \\
 \eta_{3\pi} \rightarrow \pi^+\pi^-\pi^0 & \eta_{\gamma\gamma} \rightarrow \gamma\gamma & \bar{K}^{*0} \rightarrow K^-\pi^+ \\
 \eta'_{\eta\pi\pi} \rightarrow \eta_{\gamma\gamma}\pi^+\pi^- & \eta'_{\gamma\rho} \rightarrow \gamma\rho^0 & \rho^0 \rightarrow \pi^+\pi^-
 \end{array}$$

- All submodes are combined to obtain final results:

# Motivations

- Motivation: difference of  $\mathcal{A}_{CP}$  for  $b \rightarrow s\bar{s}s$  penguin processes and  $b \rightarrow c\bar{c}s$  ( $\Delta S = S_f - \sin 2\beta \sim 3\sigma$  difference)

◇ Sensitive to

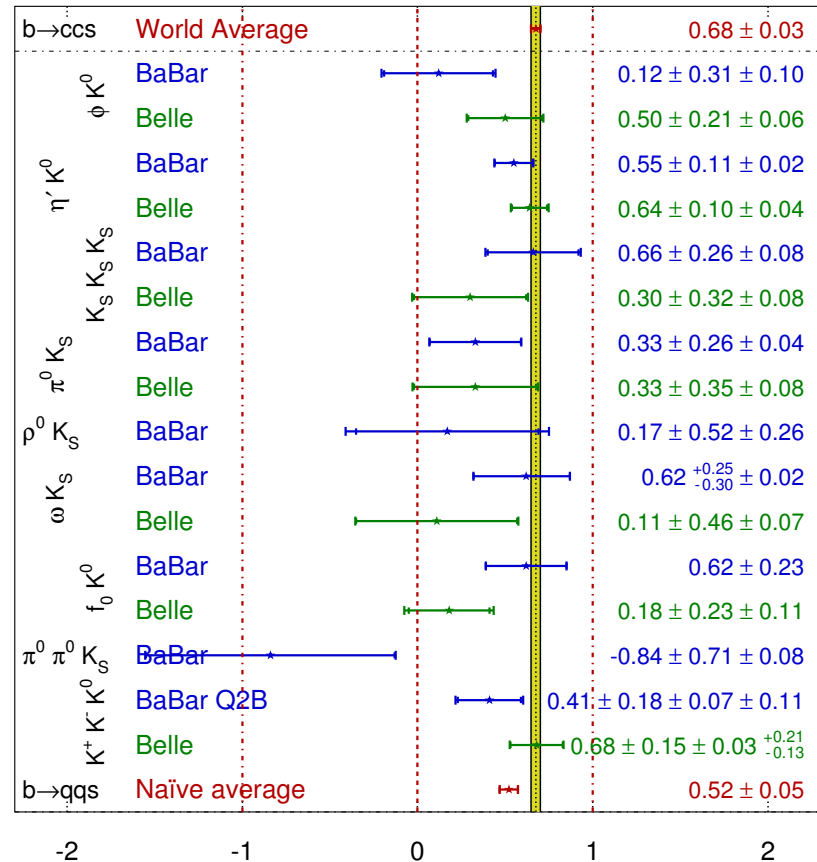
- a) New Physics
- b) SM solution ( $b \rightarrow u$ );

◇  $B^0 \rightarrow \eta^{(\prime)}X$ ,  $\phi X$  and  $K^*K$  help understand the SM solution for  $S_{\phi K^0}$  and  $S_{\eta' K^0}$ .

- Theoretical interest:  $SU(3)_f$ , QCDF, soft collinear eff. theory:

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}}) \quad \text{HFAF}$$

ICHEP 2006  
PRELIMINARY



## Analysis Strategy

- Reconstructed  $B$  (PID applicable)  
( $\Delta E$ ,  $M_{ES}/M_B$ )
- Event shape: continuum  $\sim$  jetlike,  
 $B\bar{B} \sim$  isotropic

$q\bar{q}$ :  $|\cos\theta_T|$  peak near 1,  $B\bar{B}$ : flat in CMS

- Build standard unbinned maximum likelihood:

$$\mathcal{L} = \frac{1}{N!} \exp\left(-\sum_j n_j\right) \prod_{i=1}^N \left[ \sum_j n_j \mathcal{P}_j(\vec{x}_i, \vec{\alpha}_j) \right],$$

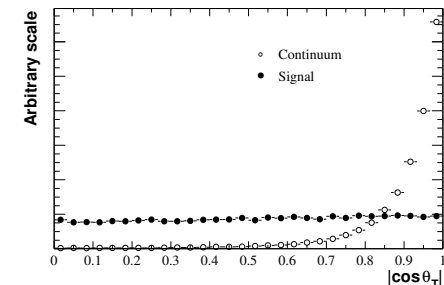
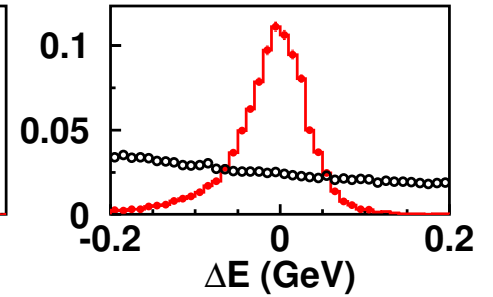
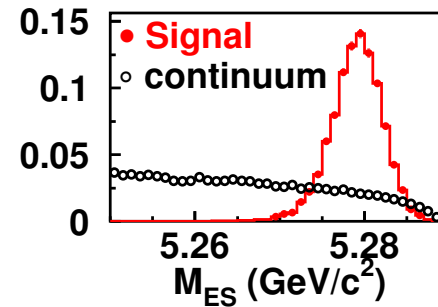
$N = \sum_j n_j$ : total events#,  $n_j$ : events# of the  $j^{\text{th}}$  component ( $j \geq 3$ ),

$\vec{x}$ : variables ( $M_{ES}/M_B$ ,  $\Delta E$ , event shape ( $\mathcal{F}$ ),  $M_R$ ,  $\cos\theta_V \dots$ ),

$\vec{\alpha}_j$ : parameters for probability density functions (PDFs),

$\mathcal{P}_j(\vec{x}_i)$ : probability of event  $i$  to be component  $j$ .

- Corrected bias if applicable due to correlations between variables neglected in ML (for detail, see references).

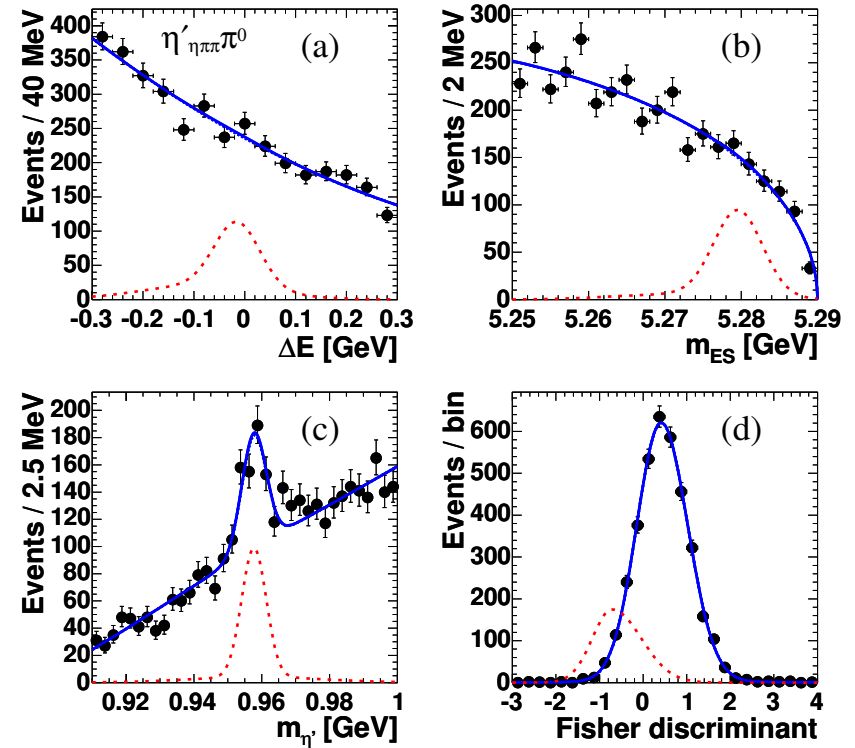


# $B^0 \rightarrow \eta\pi^0, \eta'\pi^0$ and $\eta\eta'$

Mode	$\mathcal{B} (\times 10^{-6})$	$\mathcal{S}(\sigma)$	UL(CL=90%)
$\eta\pi^0$	$0.6^{+0.5}_{-0.4} \pm 0.1$	1.3	$< 1.3$
$\eta'\pi^0$	$0.8^{+0.8}_{-0.6} \pm 0.1$	1.4	$< 2.1$
$\eta\eta'$	$0.2^{+0.7}_{-0.5} \pm 0.4$	1.3	$< 1.7$

- PRD **73**, 071102(R) (2006)
- constrain  $\Delta S_{\eta'K^0}$
- e.g.  $B^0 \rightarrow \eta'_{\eta\pi\pi}\pi^0 \Rightarrow$ 
  - $\mathcal{B} = (0.8^{+0.8}_{-0.6} \pm 0.1) \times 10^{-6}$  measured
  - assumed  $\mathcal{B} = 50 \times 10^{-6}$  (red lines X62.5)
- consistent with BELLE

Mode	$\mathcal{B} (\times 10^{-6})$	$\mathcal{S}(\sigma)$	UL(CL=90%)
$\eta\pi^0$	$1.2 \pm 0.7 \pm 0.1$	1.8	$< 2.5$
$\eta'\pi^0$	$2.79^{+1.02+0.25}_{-0.96-0.34}$	3.1	



BELLE: PRL **97**, 061802 (2006),  
PRD **71**, 091106(R) (2005)

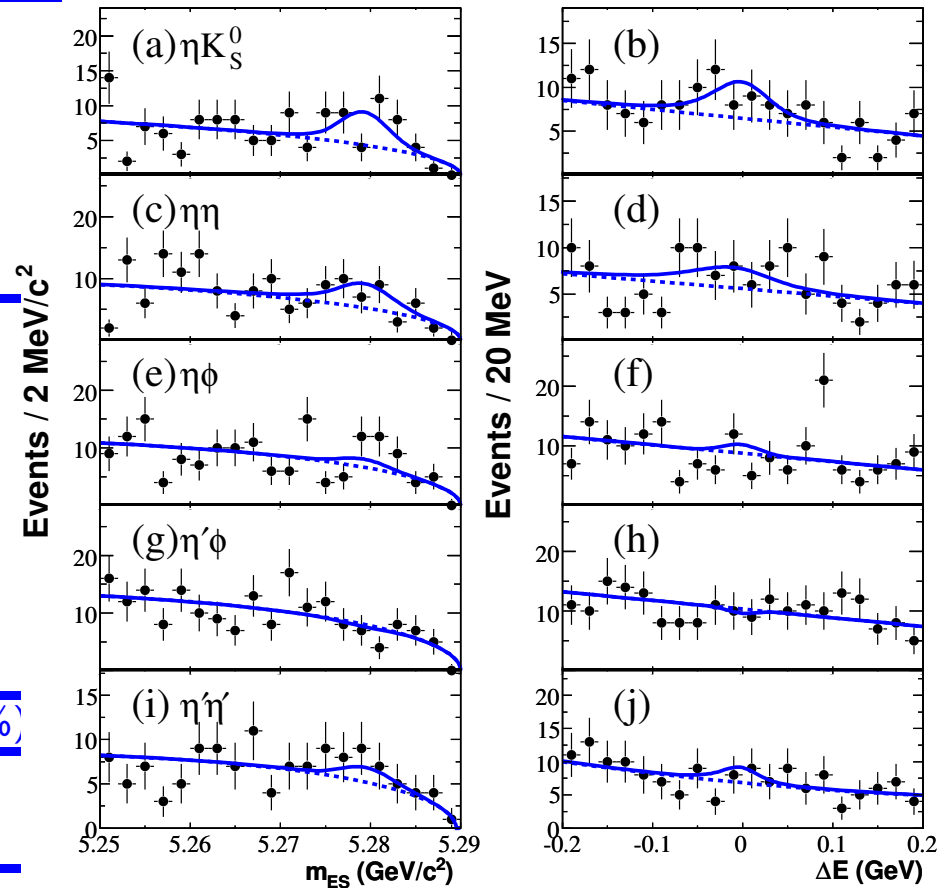
# $B^0 \rightarrow \eta K^0, \eta\eta, \eta\phi, \eta'\phi, \text{ and } \eta'\eta'$

Mode	$\mathcal{B}(10^{-6})$	$S(\sigma)$	UL(CL=90%)
$\eta K^0$	$1.8^{+0.7}_{-0.6} \pm 0.1$	3.6	$< 2.9$
$\eta\eta$	$1.1^{+0.5}_{-0.4} \pm 0.1$	3.1	$< 1.8$
$\eta\phi$	$0.1 \pm 0.2 \pm 0.1$	—	$< 0.6$
$\eta'\phi$	$0.2^{+0.4}_{-0.3} \pm 0.1$	0.5	$< 1.0$
$\eta'\eta'$	$1.0^{+0.8}_{-0.6} \pm 0.1$	1.8	$< 2.4$

- PRD **74**, 051106(R) (2006)
- constrain  $\Delta S_{\eta'K^0}$  and  $\Delta S_{\phi K^0}$
- good agreement with BELLE (hep-ex/0608033, PRD, **71** 091106 (2005) )

Mode	$\mathcal{B} (\times 10^{-6})$	$S(\sigma)$	UL(CL=90%)
$\eta K^0$	$1.1 \pm 0.4 \pm 0.1$	2.9	$< 1.9$
$\eta\eta$	$0.7^{+0.7}_{-0.6} \pm 0.1$	1.1	$< 2.0$

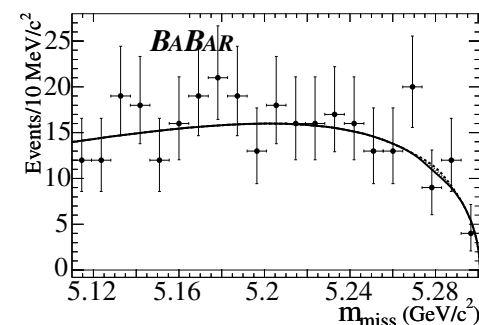
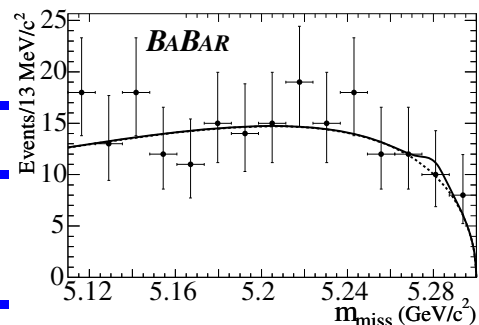
- Projections w/ a cut on  $L_S/(L_S + \sum L_{bg})$



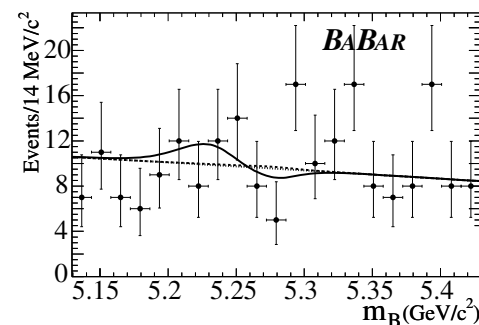
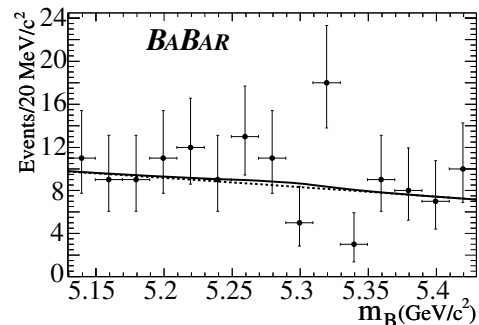
# $B \rightarrow \phi\pi$

- $B^0 \rightarrow \phi\pi^0$  (left),  $B^+ \rightarrow \phi\pi^+$  (right)

Mode	$\mathcal{B}(\times 10^{-6})$	UL
$B^+ \rightarrow \phi\pi^+$	$-0.04 \pm 0.17^{+0.04}_{-0.04}$	0.28
$B^0 \rightarrow \phi\pi^0$	$0.12 \pm 0.13^{+0.03}_{-0.04}$	0.24



- PRD 74, 011102(R) (2006)
- constrain  $\Delta S_{\phi K^0}$

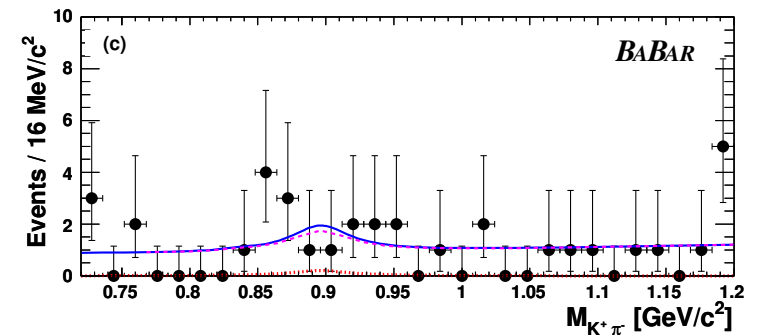
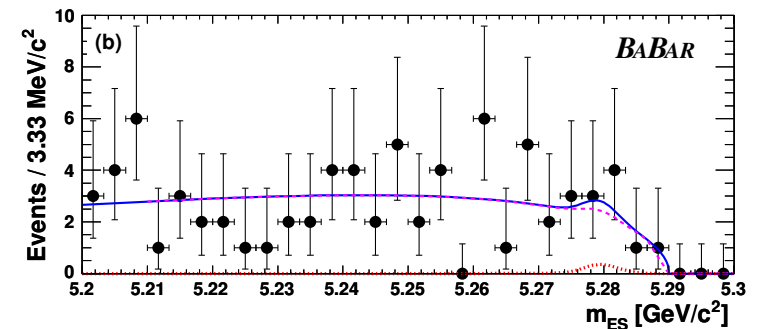
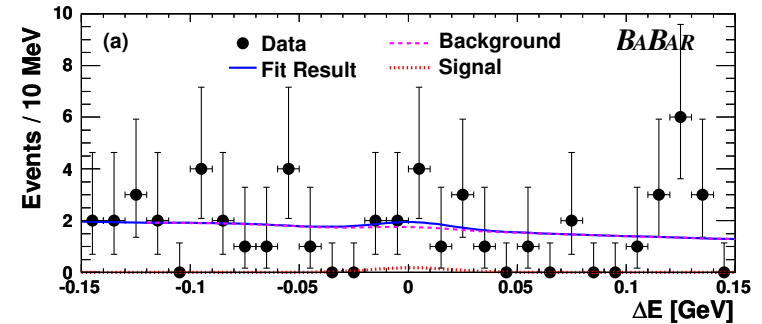


$$B \rightarrow \bar{K}^{*0} K^0$$

- First search for  $B \rightarrow \bar{K}^{*0} K^0$

$\mathcal{B}(\times 10^{-6})$	$\mathcal{S}(\sigma)$	UL(CL=90%)
$0.2^{+0.9+0.1}_{-0.8-0.3}$	0.3	$< 1.9$

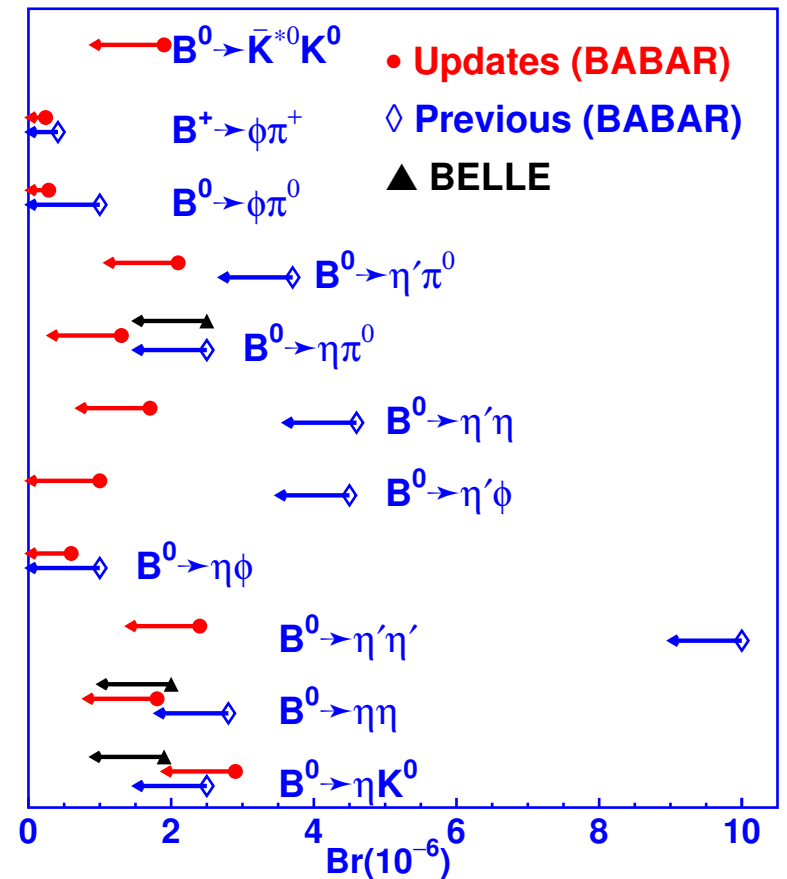
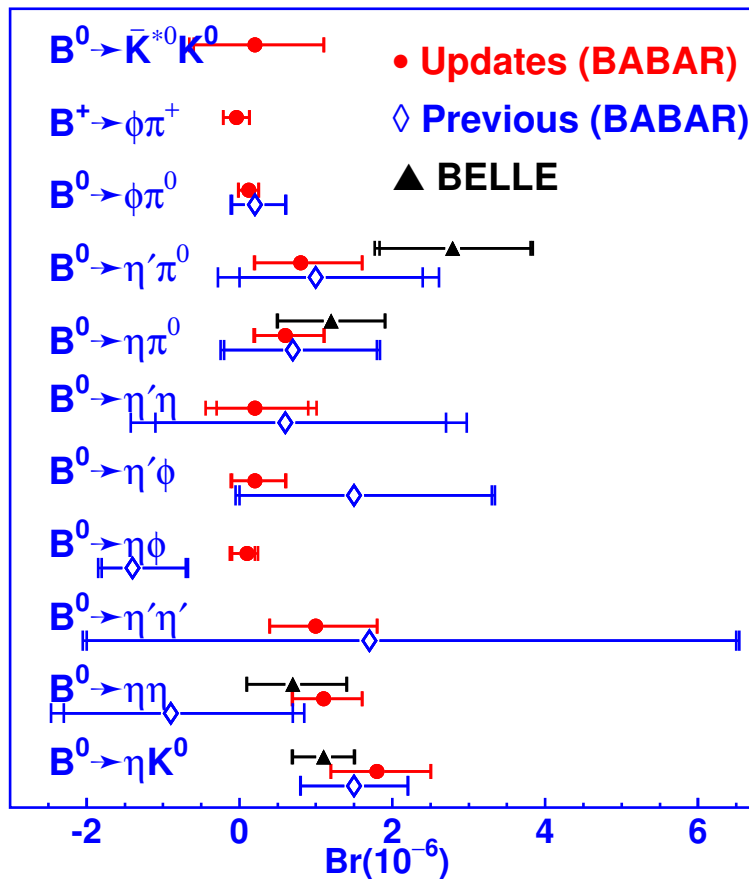
- PRD 74, 072008 (2006)
- constrain  $\Delta S_{\phi K^0}$





# Summary of Results

- Comparison with the previous BABAR and BELLE results



- Much tighter ULs

## Constraints on $\Delta S$

- Grossman *et al.*:  $|\Delta S| \equiv |S - \sin 2\beta| = 2 \cos 2\beta \sin \gamma \cos \delta |\xi|$

where  $\xi \equiv \frac{V_{ub}^* V_{us}}{V_{cb}^* V_{cs}} \frac{a^u}{a^c}$  (PRD 68,015005 (2003))

SU(3) relates  $a_f^{c,u}$  of  $A_f \equiv A(B^0 \rightarrow f) = V_{cb}^* V_{cs} a_f^c + V_{ub}^* V_{us} a_f^u$

to sum of  $b_{f'}^{c,u}$  of non-s. amp.  $A_{f'} \equiv A(B^0 \rightarrow f') = V_{cb}^* V_{cd} b_{f'}^c + V_{ub}^* V_{ud} b_{f'}^u$

to obtain bound on  $\hat{\xi} \equiv \left| \frac{V_{us}}{V_{ud}} \times \frac{V_{cb}^* V_{cd} a^c + V_{ub}^* V_{ud} a^u}{V_{cb}^* V_{cs} a^c + V_{ub}^* V_{us} a^u} \right| = \left| \frac{\xi_f + (V_{us} V_{cd}) / (V_{ud} V_{cs})}{1 + \xi_f} \right|$

in terms of Br's or UL's as

$$|\hat{\xi}_{\eta' K^0}| \leq \left| \frac{V_{us}}{V_{ud}} \right| \left\{ 0.59 \sqrt{\frac{\mathcal{B}(\eta' \pi^0)}{\mathcal{B}(\eta' K^0)}} + 0.33 \sqrt{\frac{\mathcal{B}(\eta \pi^0)}{\mathcal{B}(\eta' K^0)}} + 0.14 \sqrt{\frac{\mathcal{B}(\pi^0 \pi^0)}{\mathcal{B}(\eta' K^0)}} \right. \\ \left. + 0.53 \sqrt{\frac{\mathcal{B}(\eta' \eta')}{\mathcal{B}(\eta' K^0)}} + 0.38 \sqrt{\frac{\mathcal{B}(\eta \eta)}{\mathcal{B}(\eta' K^0)}} + 0.96 \sqrt{\frac{\mathcal{B}(\eta \eta')}{\mathcal{B}(\eta' K^0)}} \right\}.$$

$\beta, \gamma(\delta)$  weak (strong) phase

- We find  $|\Delta S_{\eta' K^0}| < 0.15$  (0.22 formerly) for  $S_{\eta' K^0}$  @CL=90%
- Gronau *et. al.*,  $C_{\eta' K^0}$  and  $S_{\eta' K^0}$   $-0.133 < \Delta S_{\eta' K^0} < 0.152$  (6 modes) and  $-0.046 < \Delta S_{\eta' K^0} < 0.094$  ( $\eta \pi^0, \eta' \pi^0$  and  $\eta \eta'$ , see hep-ph/0608085)

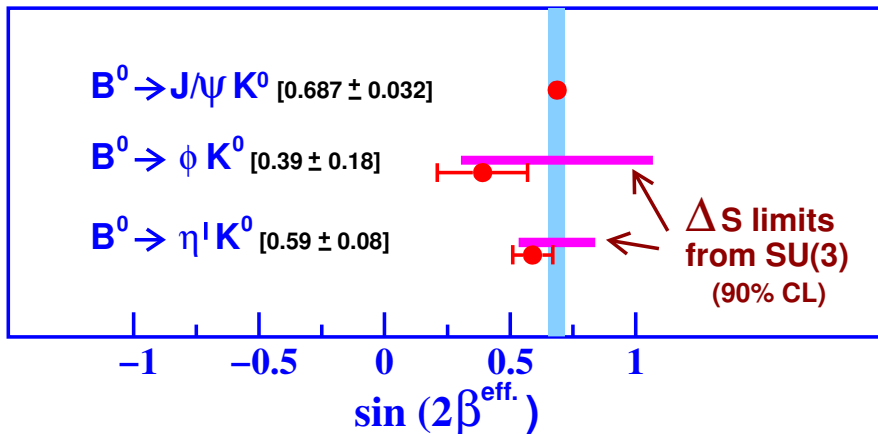
## ΔS for φK<sup>0</sup>

- ΔS<sub>φK<sup>0</sup></sub>

$$\hat{\xi}_{\phi K^0} \leq \left| \frac{V_{us}}{V_{ud}} \right| \left\{ \frac{1}{2} \left[ \frac{\mathcal{B}(\bar{K}^{*0} K^0) + \mathcal{B}(K^{*0} \bar{K}^0)}{\mathcal{B}(\phi K^0)} \right] + \frac{\sqrt{6}}{4} \left[ \frac{t\mathcal{B}(\phi\eta) + s\mathcal{B}(\phi\eta')}{\mathcal{B}(\phi K^0)} \right] \right. \\ \left. \frac{\sqrt{3}}{4} \left[ \frac{t\mathcal{B}(\omega\eta) + s\mathcal{B}(\omega\eta')}{\mathcal{B}(\phi K^0)} \right] + \frac{\sqrt{3}}{4} \left[ \frac{t\mathcal{B}(\rho^0\eta) + s\mathcal{B}(\rho^0\eta')}{\mathcal{B}(\phi K^0)} \right] \right. \\ \left. \frac{1}{4} \left[ \frac{\mathcal{B}(\rho^0\pi^0) + \mathcal{B}(\omega\pi^0)}{\mathcal{B}(\phi K^0)} \right] + \frac{1}{2\sqrt{2}} \frac{\mathcal{B}(\phi\pi^0)}{\mathcal{B}(\phi K^0)} \right\}$$

$$t \equiv \cos \theta_{\eta\eta'} = 0.94, s = \sin \theta_{\eta\eta'} = 0.34 \text{ with } \theta_{\eta\eta'} = 20^\circ$$

- We find the first constraint (SU(3)<sub>f</sub>) |ΔS<sub>φK<sup>0</sup></sub>| < 0.38 for S<sub>φK<sup>0</sup></sub> @ CL=90%



- consistent with the constraints
- Both charmless  $S$  and constraints on ΔS need further improvement  
 $S_{J/\psi K^0} \sim 5\%$ ,  $S_{\eta' K^0} \sim 14\%$   
 $S_{\phi K^0} \sim 50\%$

## Summary

- Improved ULs for  $B \rightarrow VP/PP$  ( $\Delta S = S_f - \sin 2\beta$  for  $\mathcal{A}_{CP}^{\eta'K^0}$  and  $\mathcal{A}_{CP}^{\phi K^0}$ )

Modes	Reference
$B^0 \rightarrow \eta K^0, \eta\eta, \eta'\eta', \eta\phi, \eta'\phi$	PRD <b>74</b> , 051106(R) (2006)
$B^0 \rightarrow \eta\eta', \eta'\pi^0, \eta\pi^0$	PRD <b>73</b> , 071102(R) (2006)
$B \rightarrow \phi\pi$	PRD <b>74</b> , 011102(R) (2006)
$B^0 \rightarrow \bar{K}^{*0} K^0$	PRD <b>74</b> , 072008 (2006)

- Much tighter constraint on  $|\Delta S_{\eta'K^0}| < 0.15$  (0.22 formerly) for  $S_{\eta'K^0}$  @CL=90%
- We find the first constraint  $|\Delta S_{\phi K^0}| < 0.38$  for  $S_{\phi K^0}$  @ CL=90%
- $S_{\eta'K^0}$  and  $S_{\phi K^0}$  consistent with current constraints.

## Summary of the Results

- BABAR results (blue), BELLE (black)

Mode	$\mathcal{S}(\sigma)$	$\mathcal{B}(10^{-6})$	UL ( $(10^{-6})$ )	previous	Reference
$B^0 \rightarrow \eta K^0$	3.6	$1.8^{+0.7}_{-0.6} \pm 0.1$	$< 2.9$	$< 2.5$	PRD 74, 051106 (2006)
	2.9	$1.1 \pm 0.4 \pm 0.1$	$< 1.9$		hep-ex/0608033
$B^0 \rightarrow \eta\eta$	3.1	$1.1^{+0.5}_{-0.4} \pm 0.1$	$< 1.8$	$< 2.8$	
	1.1	$0.7^{+0.7}_{-0.6} \pm 0.1$	$< 1.9$		PRD 71, 091106 (2005)
$B^0 \rightarrow \eta'\eta'$	1.8	$1.0^{+0.8}_{-0.6} \pm 0.1$	$< 2.4$	$< 10$	
$B^0 \rightarrow \eta\phi$	0.0	$0.1 \pm 0.2 \pm 0.1$	$< 0.6$	$< 1.0$	
$B^0 \rightarrow \eta'\phi$	0.5	$0.2^{+0.4}_{-0.3} \pm 0.1$	$< 1.0$	$< 4.5$	
$B^0 \rightarrow \eta\eta'$	0.4	$0.2^{+0.7}_{-0.5} \pm 0.4$	$< 1.7$	$< 4.6$	PRD 73, 071102 (2006)
$B^0 \rightarrow \eta\pi^0$	1.3	$0.6^{+0.5}_{-0.4} \pm 0.1$	$< 1.3$	$< 2.5$	
	1.8	$1.2 \pm 0.7 \pm 0.1$	$< 2.5$		PRD 71, 091106 (2005)
$B^0 \rightarrow \eta'\pi^0$	1.4	$0.8^{+0.8}_{-0.6} \pm 0.1$	$< 2.1$	$< 3.7$	
	3.1	$2.79^{+1.02+0.25}_{-0.96-0.34}$			PRL 97, 061802 (2006)
$B^0 \rightarrow \phi\pi^0$	—	$0.12 \pm 0.13^{+0.03}_{-0.04}$	$< 0.28$	$< 0.41$	PRD 74, 011102 (2006)
$B^+ \rightarrow \phi\pi^+$	—	$-0.04 \pm 0.17^{+0.04}_{-0.04}$	$< 0.24$	$< 1.0$	
$B^0 \rightarrow \bar{K}^{*0} K^0$	0.3	$0.2^{+0.9+0.1}_{-0.8-0.3}$	$< 1.9$		PRD 74, 072008 (2006)