

Leptonic EDM's from Heavy Right-Handed Neutrinos

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with

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Electric Dipole Moment (EDM)

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Non-zero d violates **P** and **CP**.

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- ⑥ CP violation in the quark sector
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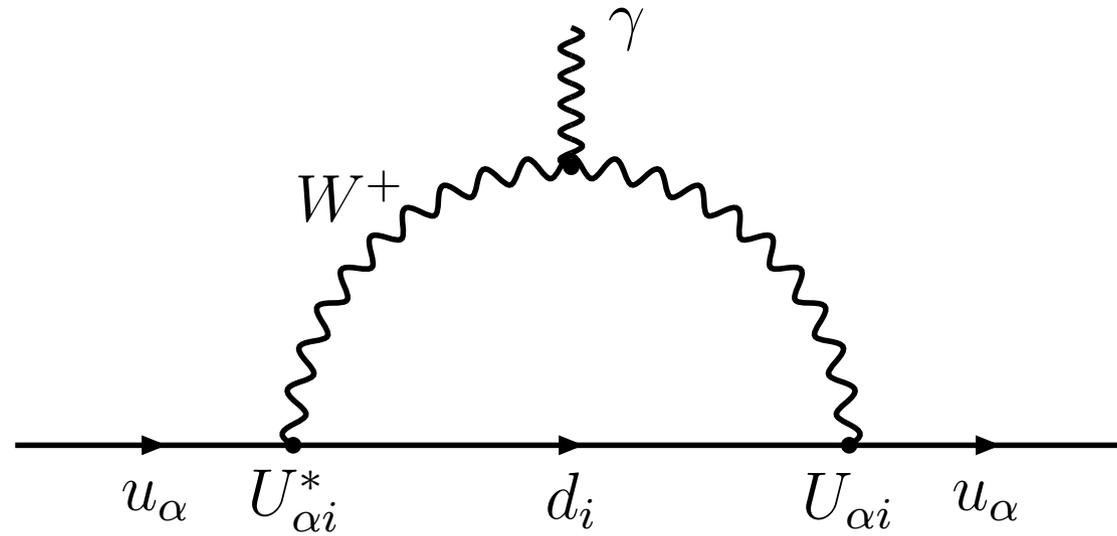
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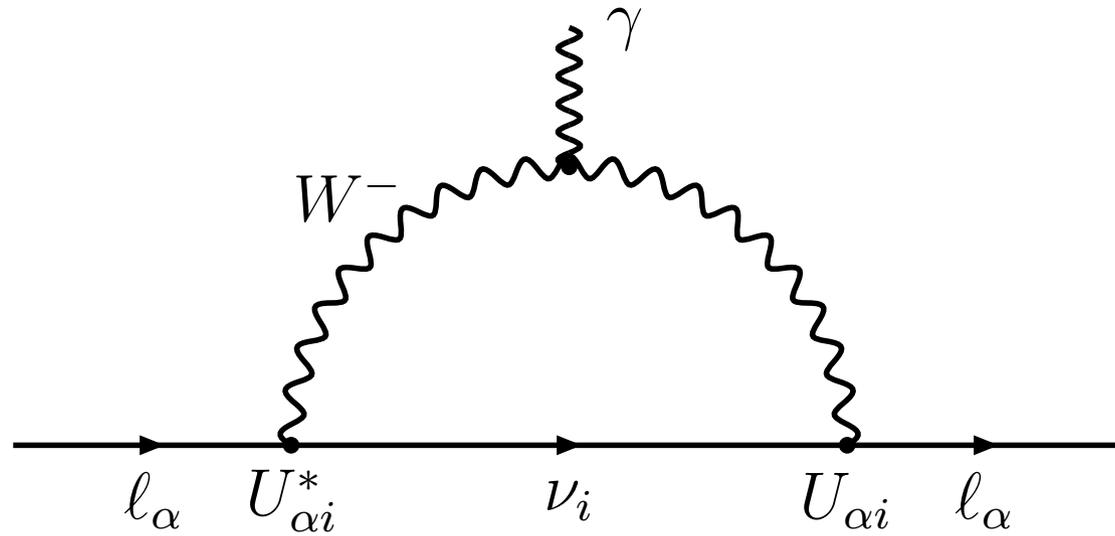
- ⑥ CP violation in the lepton sector
 - △ Unconstrained. Could be big.
 - △ Could be a source of leptogenesis
 - △ Lepton EDM's generated at the **2-loop** level

1-loop diagram



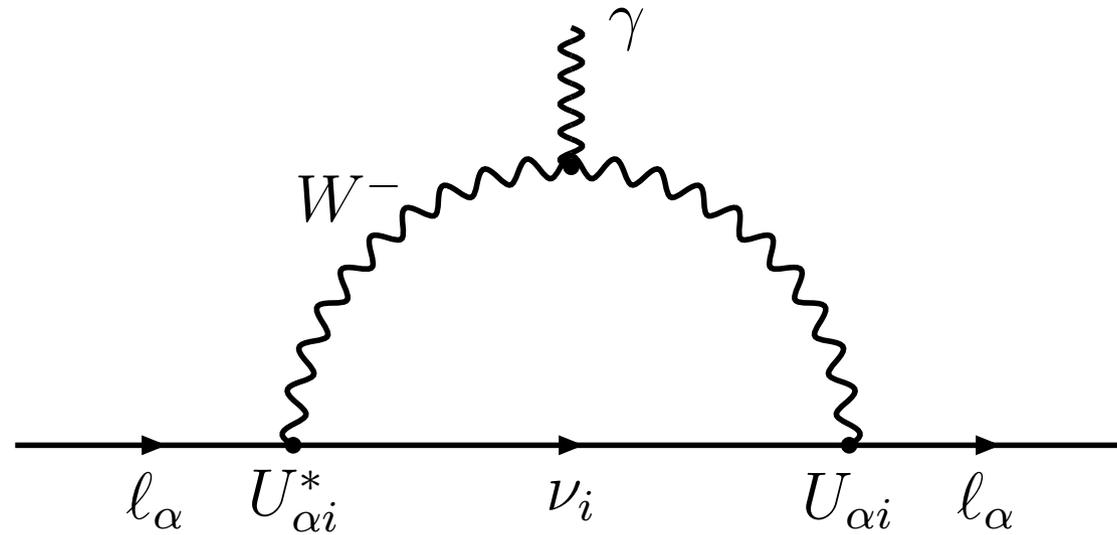
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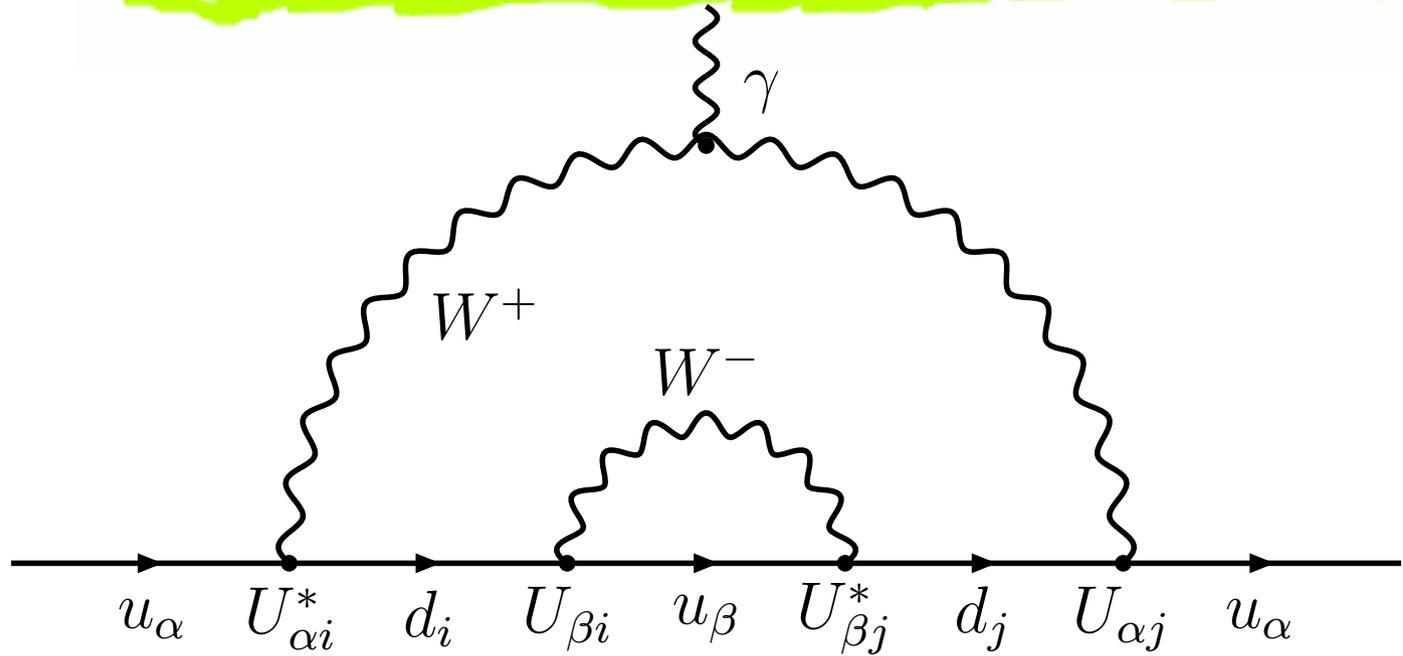
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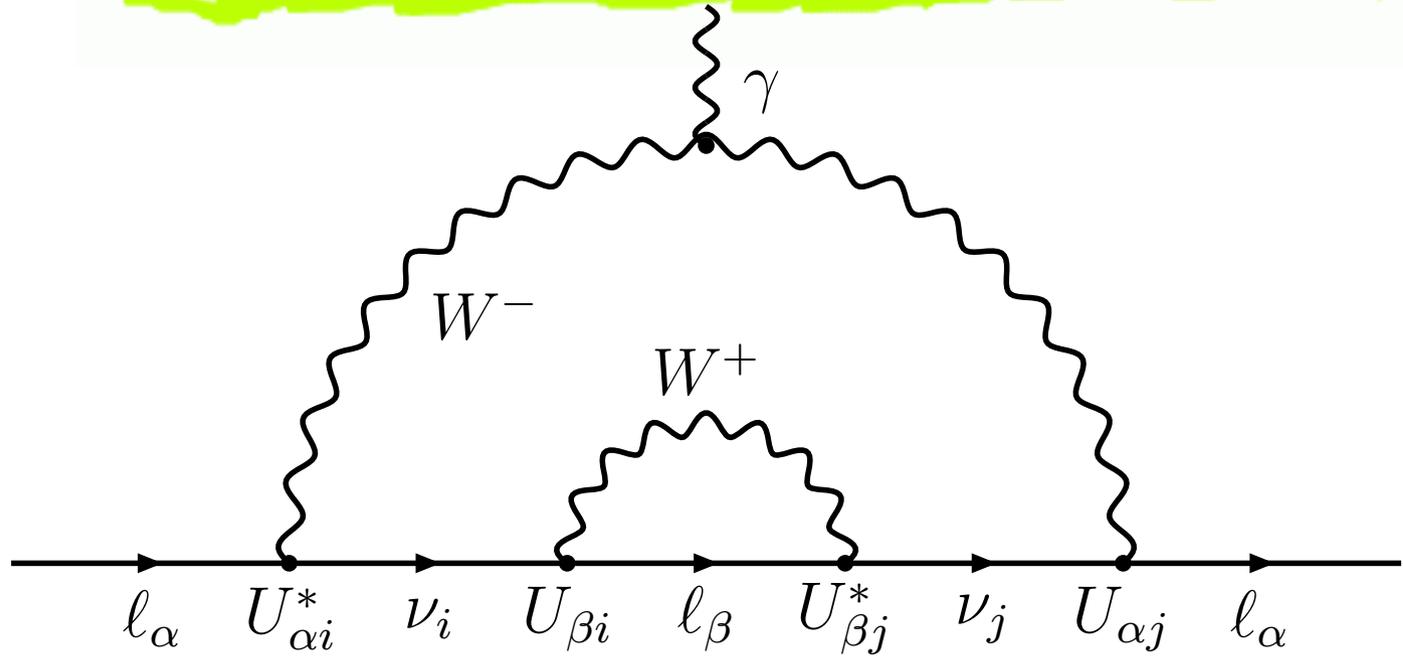
Insensitive to complex phases

2-loop diagram



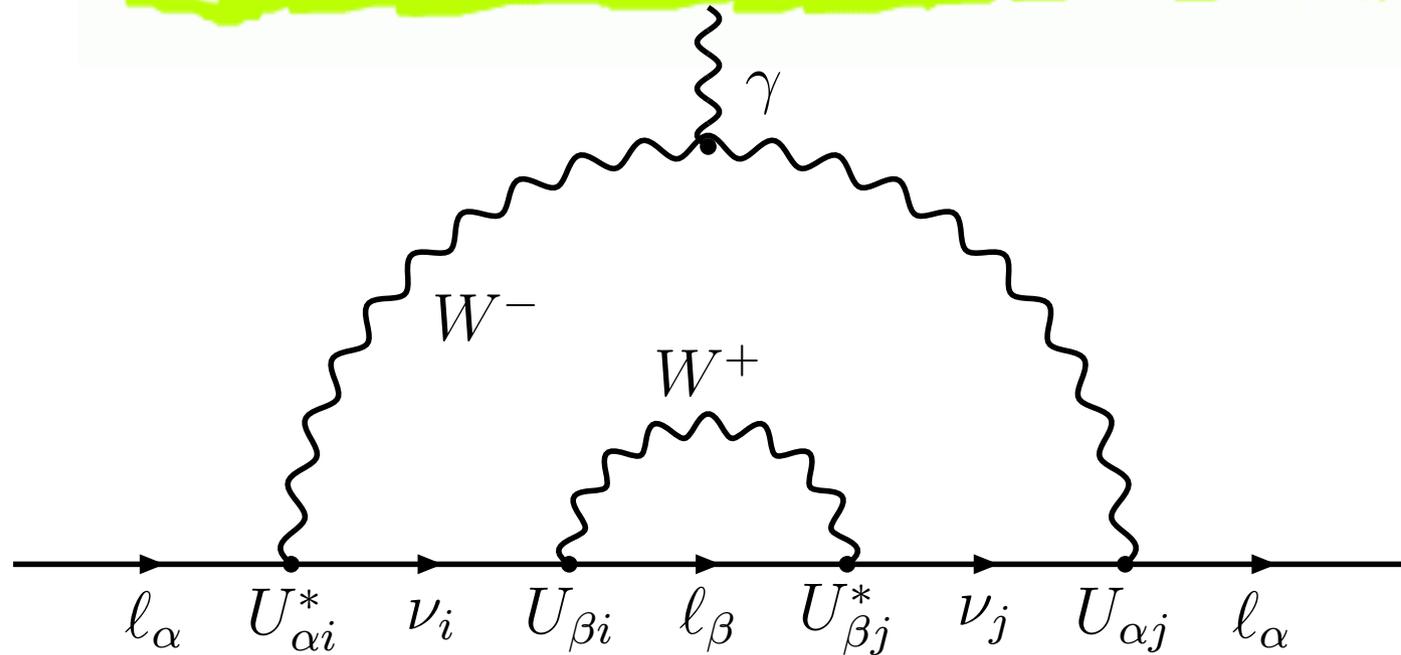
$$\propto (U_{\alpha i}^* U_{\beta i})(U_{\alpha j} U_{\beta j}^*)$$

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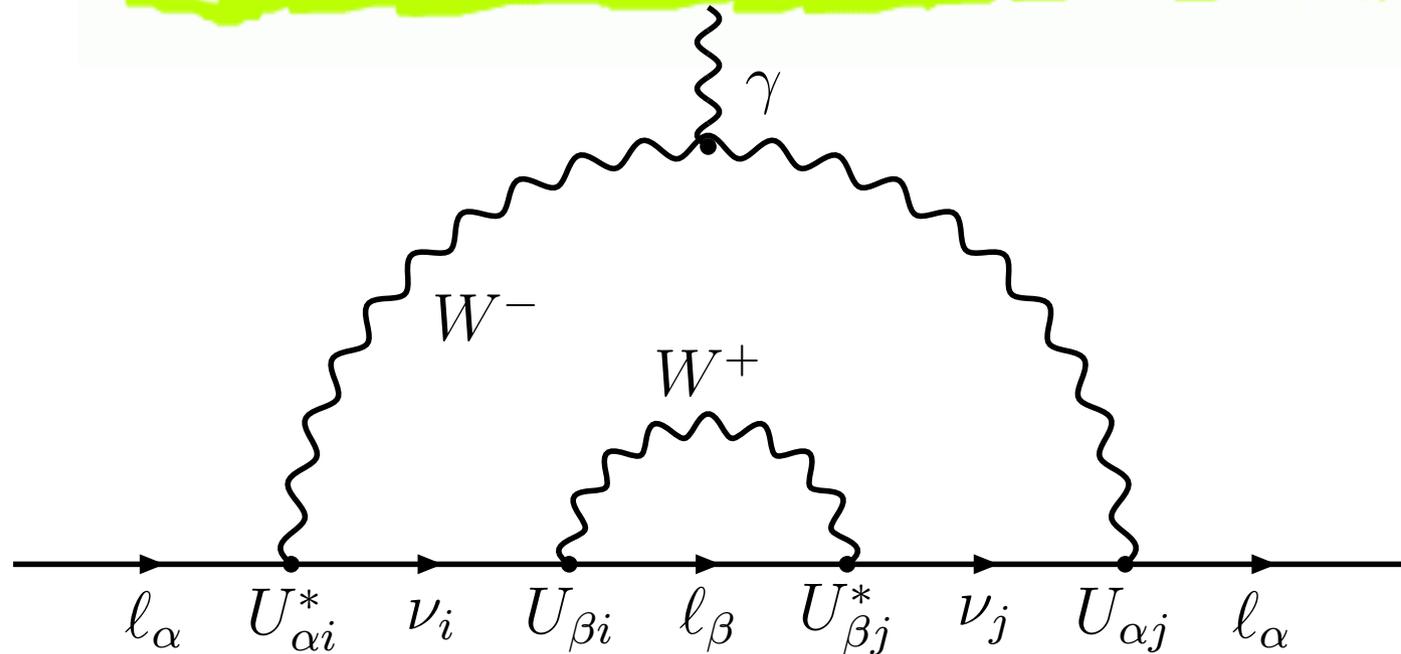
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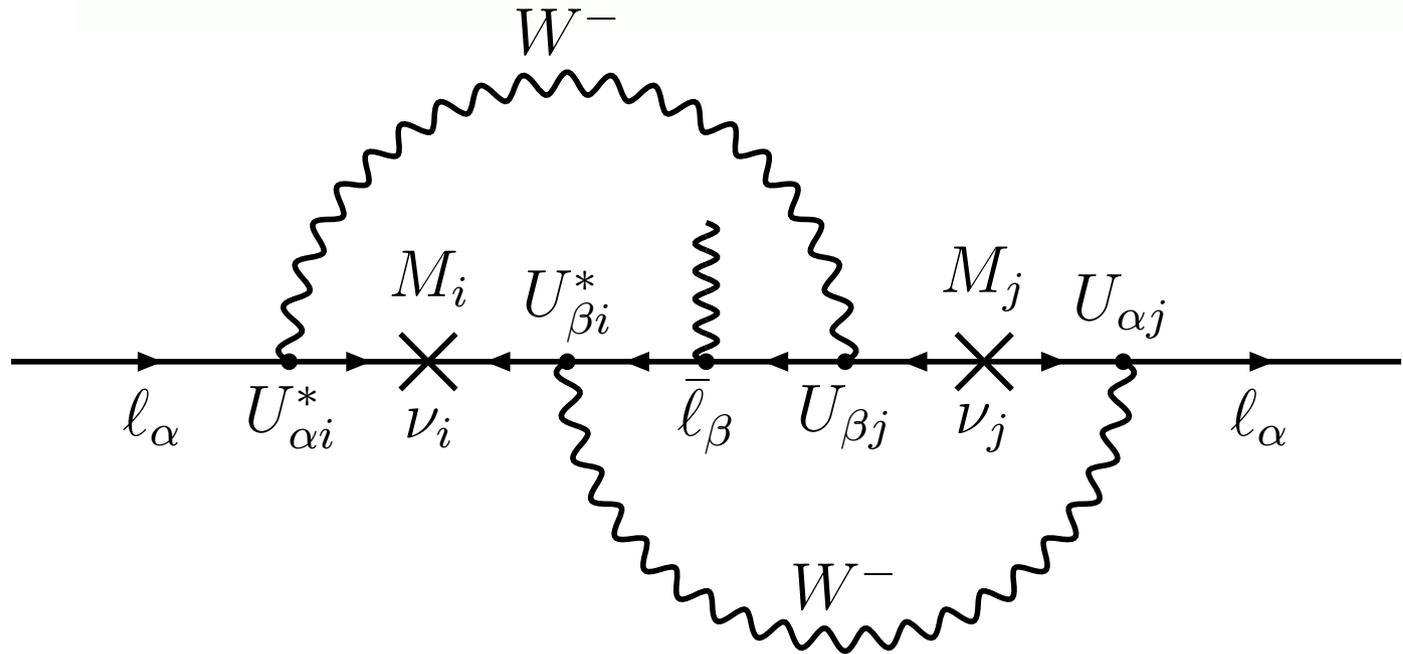


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Diagram is **symmetric** under the interchange $i \leftrightarrow j$
 \implies Imaginary parts of $(U_{\alpha i}^* U_{\beta i})(U_{\alpha j} U_{\beta j}^*)$ **cancel**

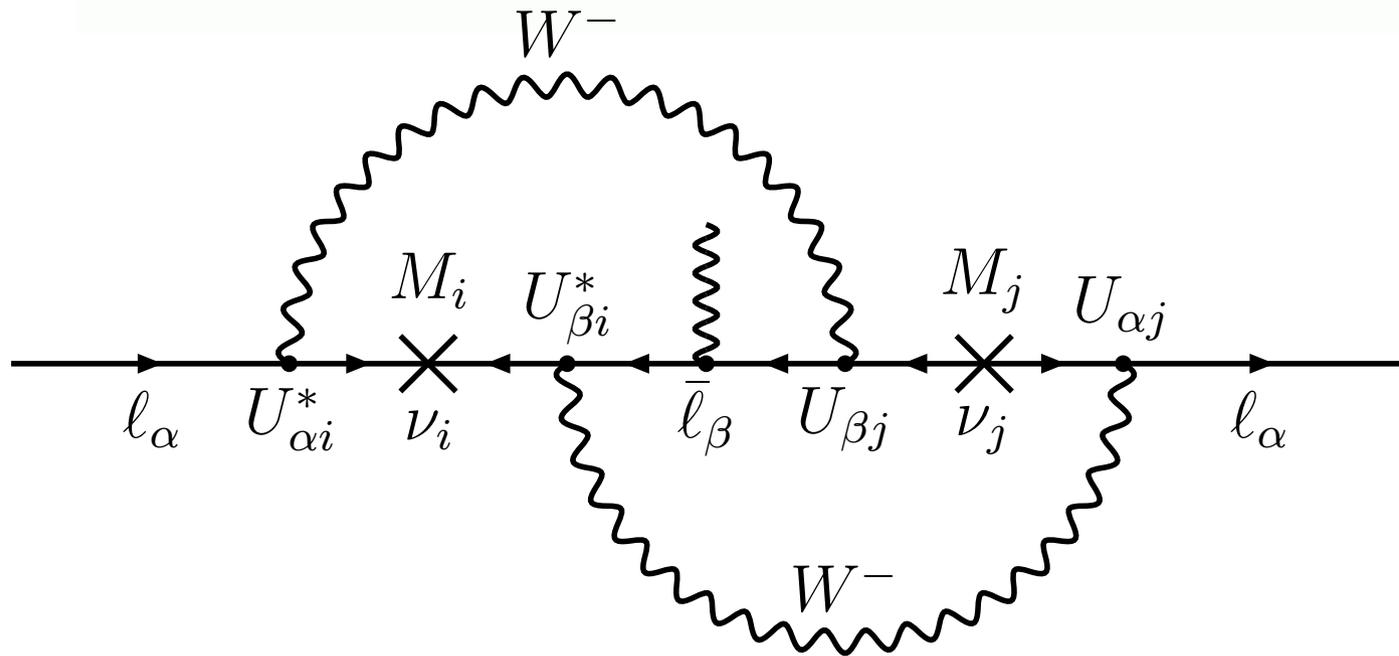
Shabalin, Sov. J. Nucl. Phys. 28 (1978) 75

2-loop diagram unique to leptons



$$\propto (U_{\alpha i}^* U_{\beta i}^*) (U_{\alpha j} U_{\beta j})$$

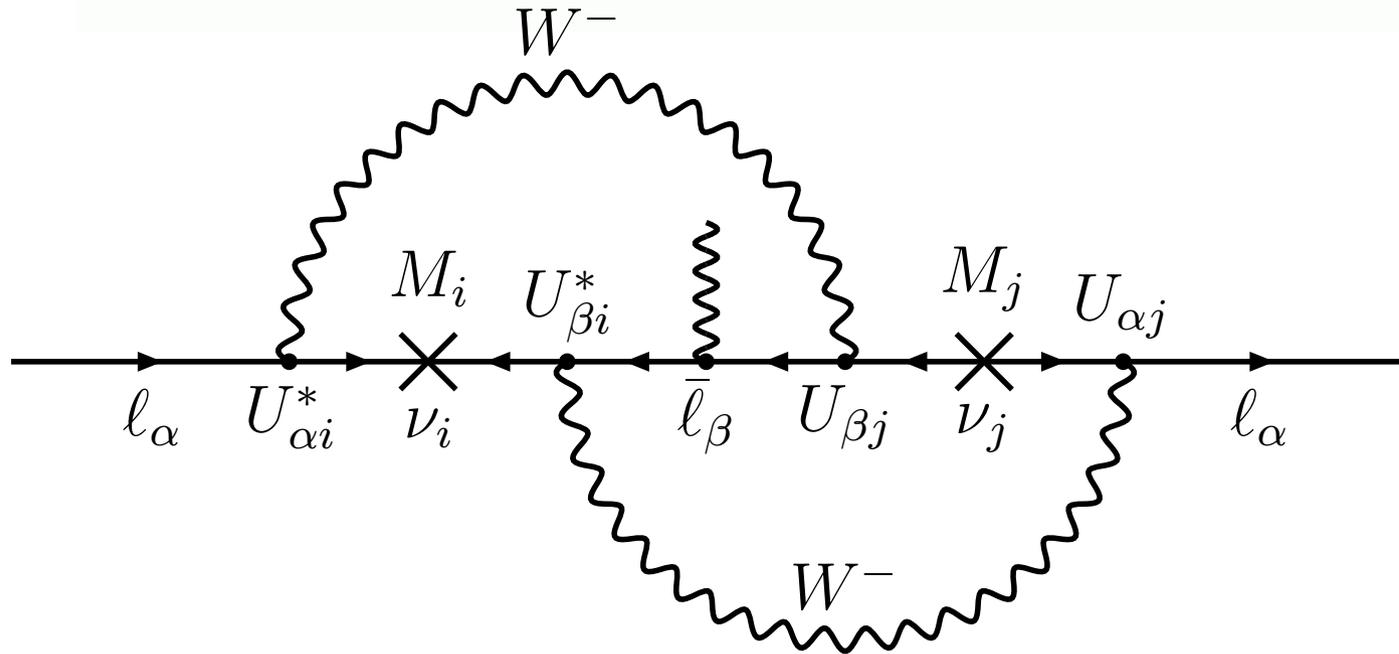
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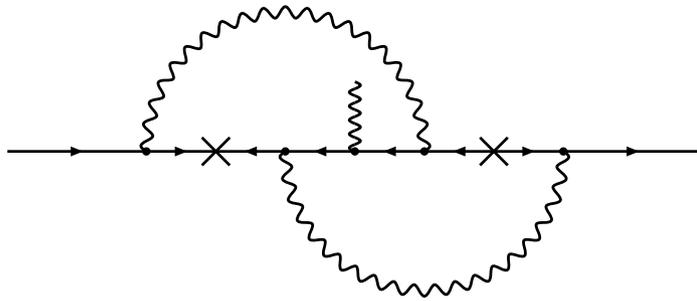


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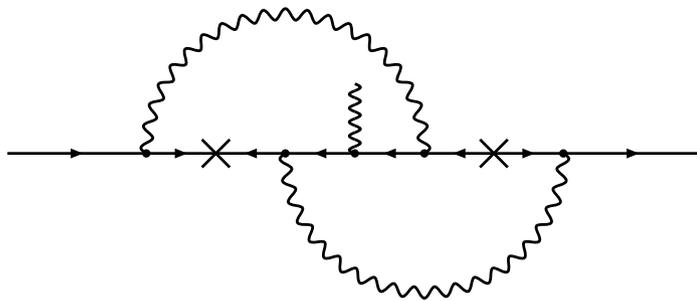
\implies Imaginary parts of $(U_{\alpha i}^* U_{\beta i}^*) (U_{\alpha j} U_{\beta j})$ **survive**

Is it significant?



$$\propto M_i M_j (U_{\alpha i}^* U_{\beta i}^*) (U_{\alpha j} U_{\beta j})$$

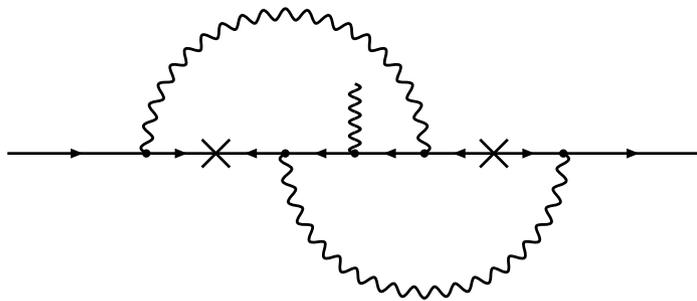
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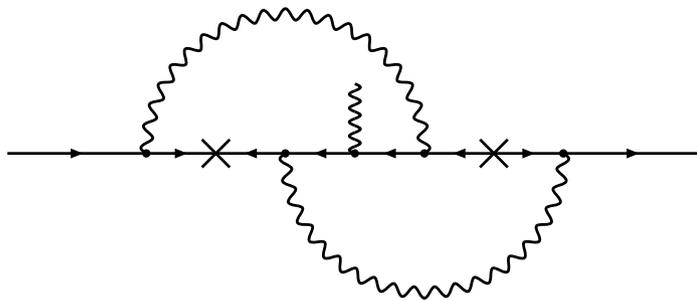
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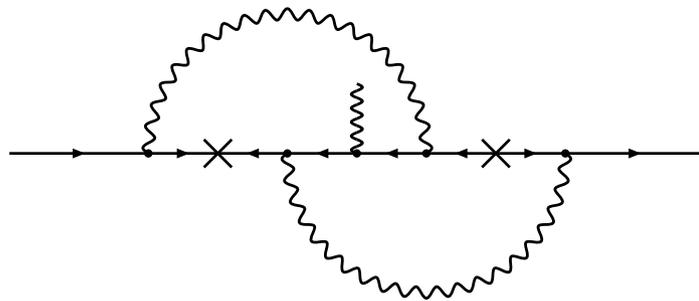
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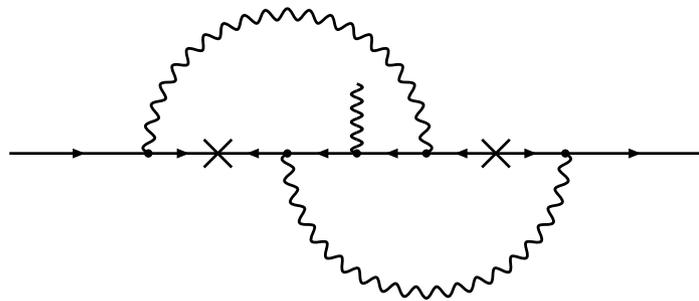
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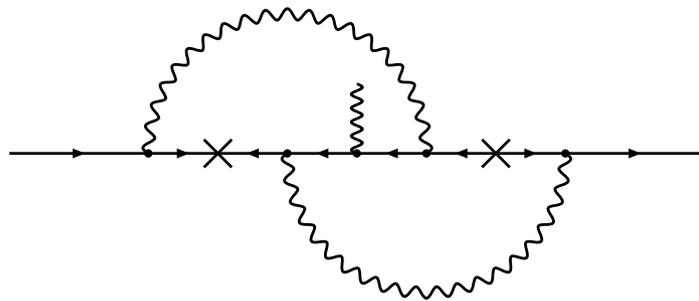
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→ same order as the light neutrino contribution.

TeV-Scale Seesaw Models

Example: Okamura Texture [PRD 68, 073001 \(2003\)](#)

$$\begin{bmatrix} 0 & 0 & 0 & \alpha D & \beta D & \gamma D \\ 0 & 0 & 0 & \alpha D & \beta D & \gamma D \\ 0 & 0 & 0 & \alpha D & \beta D & \gamma D \\ \alpha D & \alpha D & \alpha D & \alpha M & 0 & 0 \\ \beta D & \beta D & \beta D & 0 & \beta M & 0 \\ \gamma D & \gamma D & \gamma D & 0 & 0 & \gamma M \end{bmatrix}$$

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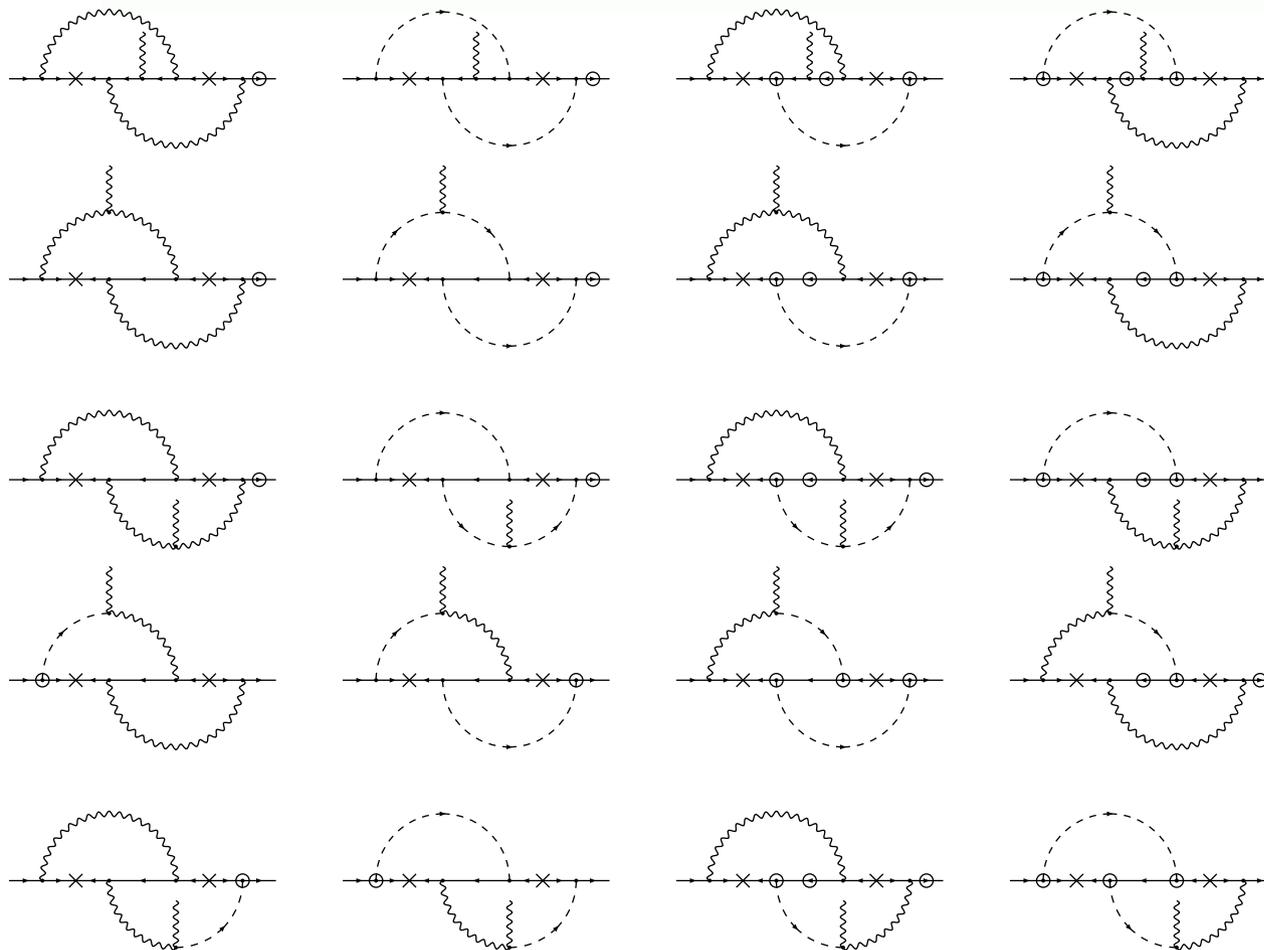
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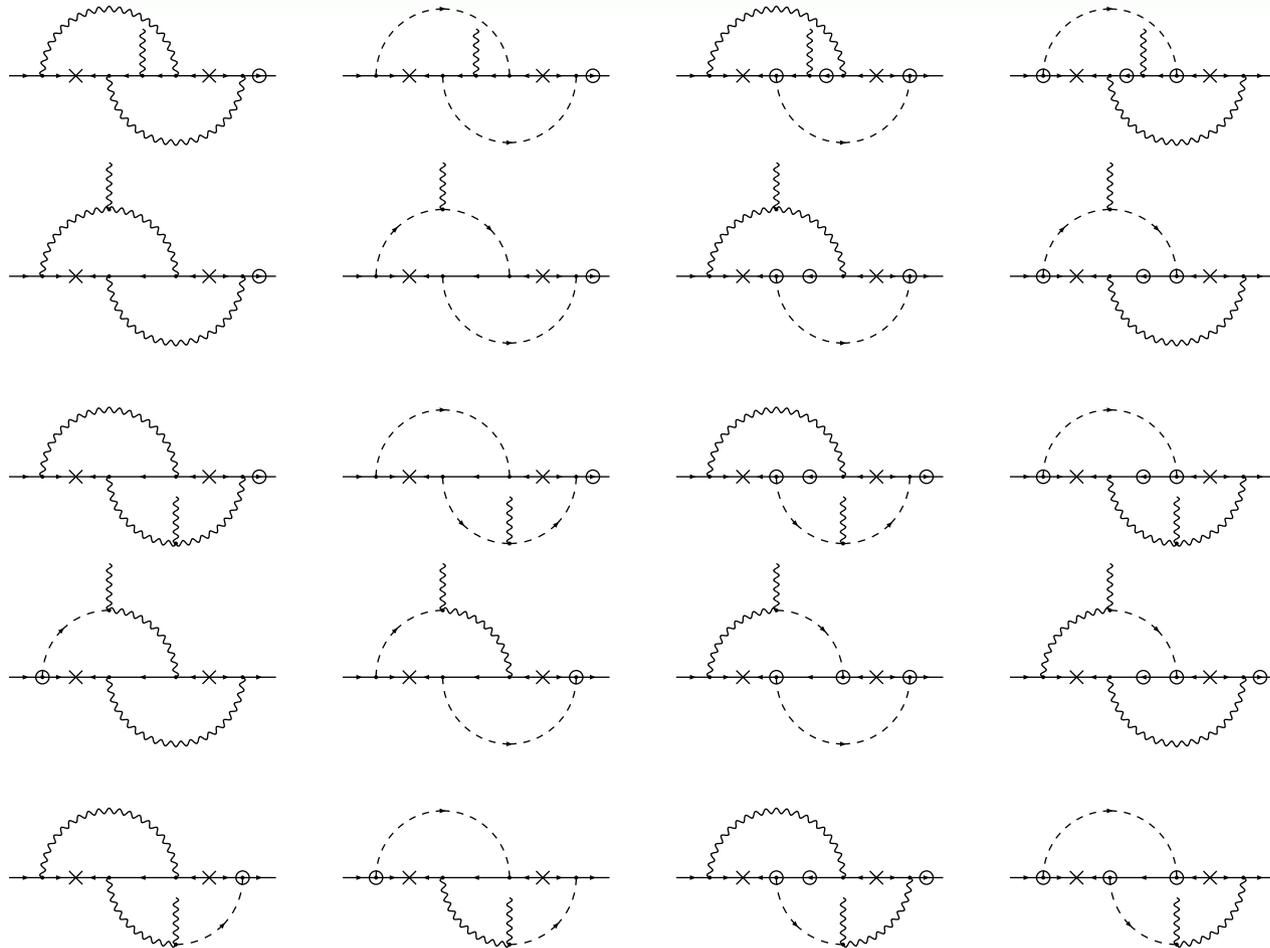
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 - light masses automatically zero.
 - mixings and masses are independent.
 - lepton EDM's can be **large**!?

20 Diagrams



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Give to graduate student!

Results (by Saifuddin Rayyan)



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- ⑥ Paper in preparation.

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Current Experimental Limits:

$$d_e = (6.9 \pm 7.4) \times 10^{-28} \text{ e} \cdot \text{cm}$$
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Preliminary Result for Okamura Model:

$$d_e \leq O(10^{-28}) \text{ e} \cdot \text{cm}$$

(Actual number depends on choice of parameters.)