

# Lepton non-universality at LEP and charged Higgs

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Joint Meeting of Pacific Region Particle Physics Communities  
Sheraton Waikiki Hotel, Honolulu, Hawaii, 2006-10-31

Based on JHEP10(2006)077 [[hep-ph/0607280](https://arxiv.org/abs/hep-ph/0607280)].

# Lepton universality in charged current interactions

- SM predicts lepton universality.
- $W$  boson couplings to  $e, \mu, \tau$  are determined by SU(2) gauge invariance.

$$\mathcal{L}_{\text{CC}} = \frac{g}{\sqrt{2}} \sum_{l=e,\mu,\tau} W_{\mu}^{\dagger} \bar{\nu}_l \gamma^{\mu} \left( \frac{1-\gamma_5}{2} \right) l + \text{h.c.}$$

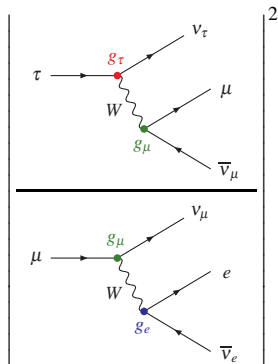
- Thoroughly tested in  
 $\mu \rightarrow e \nu \nu, \tau \rightarrow \mu \nu \nu, \tau \rightarrow e \nu \nu, \pi \rightarrow e \nu, \pi \rightarrow \mu \nu, \tau \rightarrow \pi \nu, \dots$   
All these consistent with lepton universality.

# Test of lepton universality at $\mu \rightarrow e\nu\nu$ and $\tau \rightarrow \mu\nu\nu$

- Use parameterization

$$\mathcal{L}_{\text{CC}} = \sum_{l=e,\mu,\tau} \frac{g_l}{\sqrt{2}} W_\mu^\dagger \bar{\nu}_l \gamma^\mu \left( \frac{1-\gamma_5}{2} \right) l + \text{h.c.}$$

- Take ratio  $\Gamma(\tau \rightarrow \mu\nu\nu)/\Gamma(\mu \rightarrow e\nu\nu)$ :



$$\rightsquigarrow (g_\tau/g_e)_{\tau\mu} = 1.0004 \pm 0.0022$$

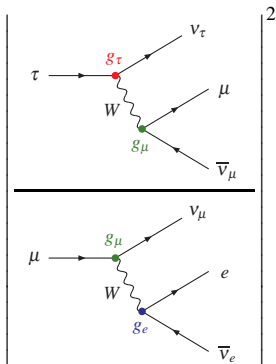
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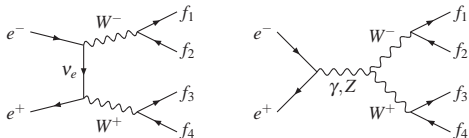
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Perfect agreement with  
lepton universality

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# Measurement of $B(W \rightarrow l\nu)$ at LEP

- LEP directly measured  $B(W \rightarrow e\nu_e)$ ,  $B(W \rightarrow \mu\nu_\mu)$ ,  $B(W \rightarrow \tau\nu_\tau)$ , from partial cross sections of  $WW \rightarrow 4f$ .



$(f_1, f_2) = (e, \bar{\nu}_e), (\mu, \bar{\nu}_\mu), (\tau, \bar{\nu}_\tau), (d, \bar{u}), (s, \bar{c})$ .

$(f_4, f_3)$  is a conjugate.

# Tau mode excess

LEP electroweak working group, hep-ex/0511027

- LEP results

| Experiment | $B(W \rightarrow e\nu_e)$ [%] | $B(W \rightarrow \mu\nu_\mu)$ [%] | $B(W \rightarrow \tau\nu_\tau)$ [%] |
|------------|-------------------------------|-----------------------------------|-------------------------------------|
| ALEPH      | $10.78 \pm 0.29^*$            | $10.87 \pm 0.26^*$                | $11.25 \pm 0.38^*$                  |
| DELPHI     | $10.55 \pm 0.34^*$            | $10.65 \pm 0.27^*$                | $11.46 \pm 0.43^*$                  |
| L3         | $10.78 \pm 0.32^*$            | $10.03 \pm 0.31^*$                | $11.89 \pm 0.45^*$                  |
| OPAL       | $10.40 \pm 0.35$              | $10.61 \pm 0.35$                  | $11.18 \pm 0.48$                    |
| LEP        | $10.65 \pm 0.17$              | $10.59 \pm 0.15$                  | $11.44 \pm 0.22$                    |

- Under assumption of  $B(W \rightarrow e\nu_e) = B(W \rightarrow \mu\nu_\mu)$ ,

$$\frac{B(W \rightarrow \tau\nu_\tau)}{[B(W \rightarrow e\nu_e) + B(W \rightarrow \mu\nu_\mu)]/2} \Big|_{\text{LEP}} = 1.077 \pm 0.026$$

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**7.7% or 2.8  $\sigma$**  departure from lepton universality.

- New physics?



# Previous attempts for explanation

X.-Y. Li, E. Ma, hep-ph/0507017

- Gauge model of generation non-universality.
- Two SU(2) gauge groups:  
one for 1st and 2nd family fermions, the other for 3rd.
- Mixing of gauge bosons leads to flavor-dependent lightest  $W$  boson couplings to leptons.
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- Can fit leptonic  $W$  branching ratios.
- **However**, it decreases

$$\Gamma(\tau \rightarrow \mu \nu \nu) / \Gamma(\mu \rightarrow e \nu \nu)$$

by **7%  $\approx 15 \sigma$**   $\longrightarrow$  **ruled out.**

# Dilemma

- A model leading to effective interactions

$$\mathcal{L}_{CC} = \sum_{l=e,\mu,\tau} \frac{g_l}{\sqrt{2}} W_\mu^\dagger \bar{\nu}_l \gamma^\mu \left( \frac{1-\gamma_5}{2} \right) l + \text{h.c.},$$

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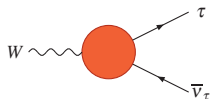
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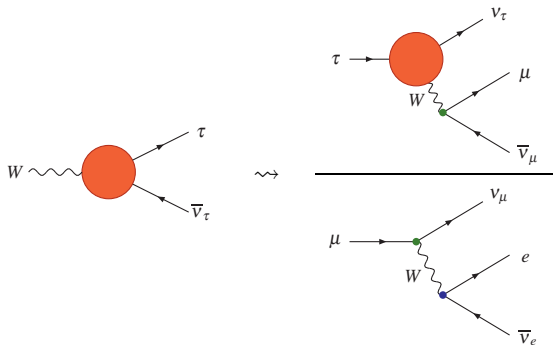
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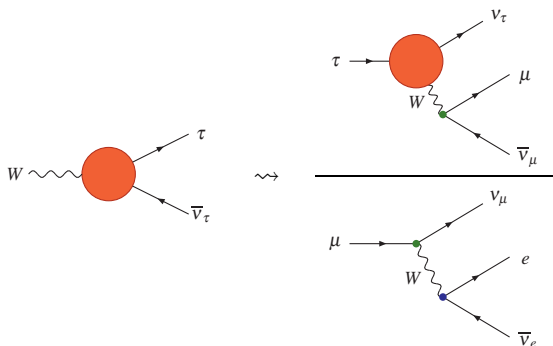
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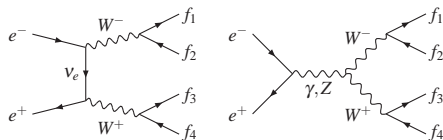
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# Outline

- 1 Introduction
- 2 Charged Higgs solution
- 3 Constraints from data
- 4 Effects on  $B(W \rightarrow l\nu)$
- 5 Test at future experiments

# Can charged Higgs be a solution?

- Suppose  $H^+H^-$  pairs were produced at LEP.



- $B(W \rightarrow l\nu)$  is measured by counting final state fermions.

- $\sigma_{HH}$  is a decreasing function of  $m_{H^\pm}$   $\rightarrow$   $m_{H^\pm} \approx m_W$  desirable.

See the plot on Page 16.

- Hard to realize in MSSM due to

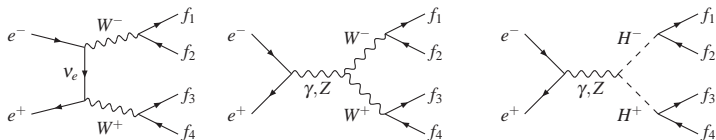
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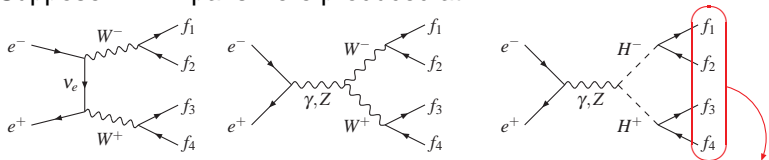
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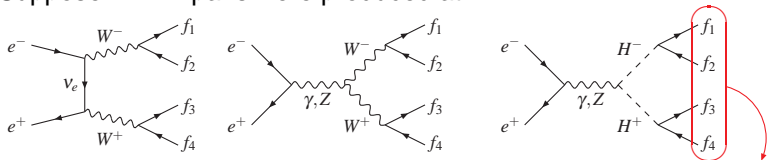
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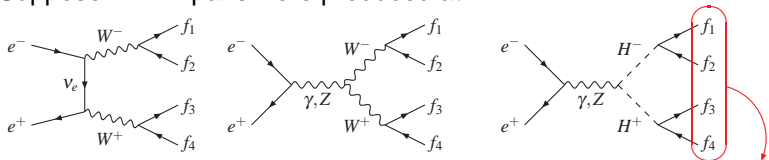
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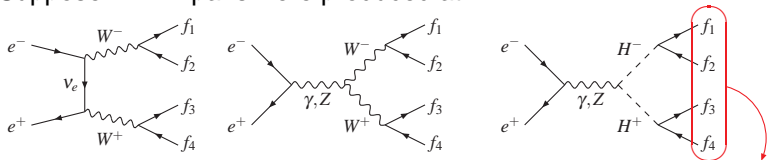
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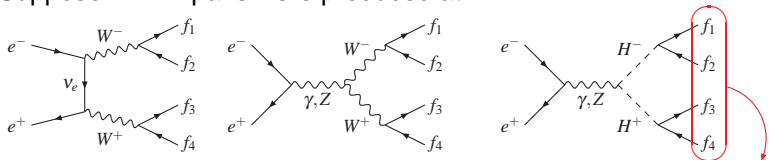
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## 2HDM's free of tree-level FCNC

- Make assumptions on Higgs Yukawa couplings for suppressing tree-level FCNC.
- Four example models

Model labels borrowed from Barger, Hewett, Phillips, PRD(1990)

| Models                                   | I                | II              | III              | IV               |
|--|------------------|-----------------|------------------|------------------|
|  | VEV $A_f$        | VEV $A_f$       | VEV $A_f$        | VEV $A_f$        |
| $\begin{pmatrix} u \\ d \end{pmatrix}$   | $H_2 \cot\beta$  | $H_2 \cot\beta$ | $H_2 \cot\beta$  | $H_2 \cot\beta$  |
|  | $H_2 -\cot\beta$ | $H_1 \tan\beta$ | $H_1 \tan\beta$  | $H_2 -\cot\beta$ |
| $\begin{pmatrix} \nu \\ l \end{pmatrix}$ | $H_2 -\cot\beta$ | $H_1 \tan\beta$ | $H_2 -\cot\beta$ | $H_1 \tan\beta$  |

$$\tan\beta \equiv v_2/v_1$$

- $H^\pm$ -fermion-fermion interaction Lagrangian

$$\mathcal{L} = \frac{g}{\sqrt{2}m_W} H^+ [V_{ij} m_{u_i} A_u \bar{u}_{Ri} d_{Lj} + V_{ij} m_{d_j} A_d \bar{u}_{Li} d_{Rj} + m_l A_l \bar{\nu}_L l_R] + \text{h.c.}$$

governs  $b \rightarrow s\gamma$ ,  $H^\pm \rightarrow \tau\nu_\tau, \dots$

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$H^+$  in **Model I** becomes **fermiophobic** for high  $\tan\beta$



## $b \rightarrow s\gamma$ constraint

- One of the most stringent constraints on  $m_{H^\pm}$ .
- Branching ratio in 2HDM:

$$\frac{B(B \rightarrow X_s \gamma)}{B_{\text{SM}}(B \rightarrow X_s \gamma)} = \left| \frac{C_{7\gamma}^{\text{SM}}(m_b) + C_{7\gamma}^{H^\pm}(m_b)}{C_{7\gamma}^{\text{SM}}(m_b)} \right|^2 = \left| 1 + 0.71 A_u A_d + 0.15 A_u^2 \right|^2$$

- In Models **II** and **III**,  $A_u A_d = 1$ , and therefore

$$\frac{B(B \rightarrow X_s \gamma)}{B_{\text{SM}}(B \rightarrow X_s \gamma)} \geq 2.9 \quad \text{for} \quad m_{H^\pm} \approx m_W$$

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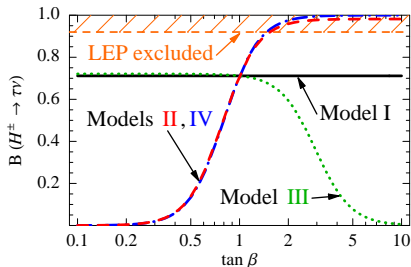
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Models **I** and **IV** survive if  $\tan \beta \gtrsim 4$

## Direct constraints on $m_{H^\pm}$

- $B(H^\pm \rightarrow \tau\nu_\tau)$  as a function of  $\tan\beta$ :

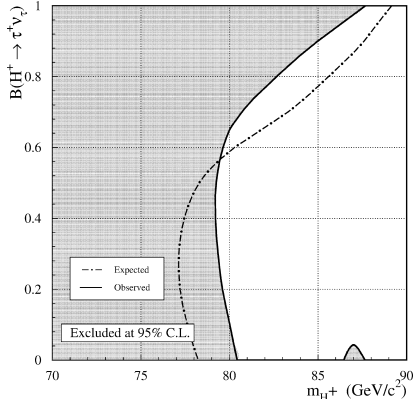
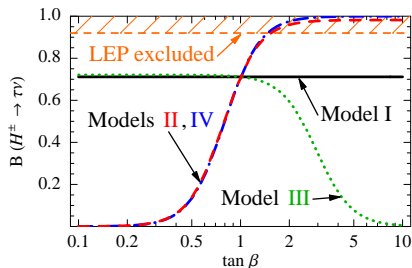


Hatched region is excluded for  $m_{H^\pm} = 86$  GeV [plot on Page 16].

- Model IV leads to  $B(H^\pm \rightarrow \tau\nu_\tau) \gtrsim 0.99$  for  $\tan\beta \gtrsim 4$ .
- $b \rightarrow s\gamma$  and direct search largely determine one viable model.
- Consider only **Model I** from here on.

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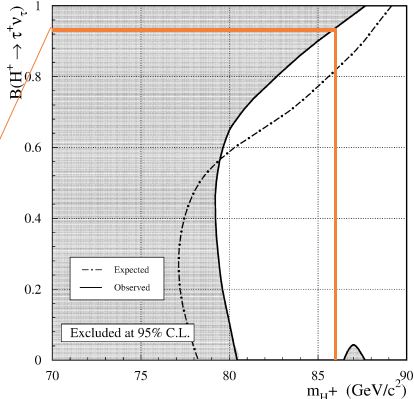
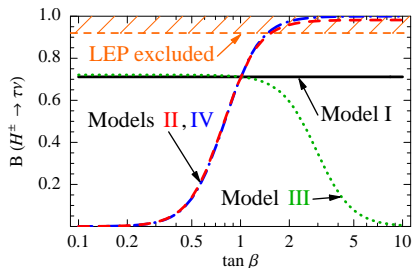
ALEPH, PLB(2002)

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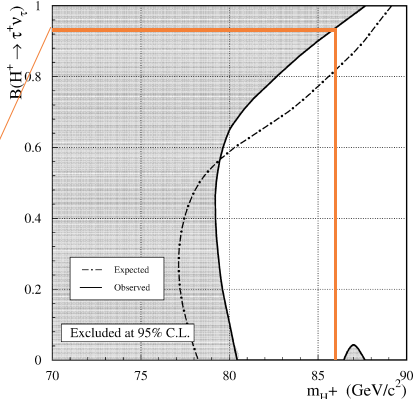
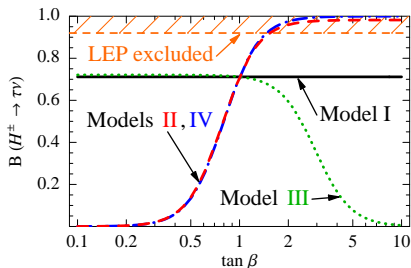
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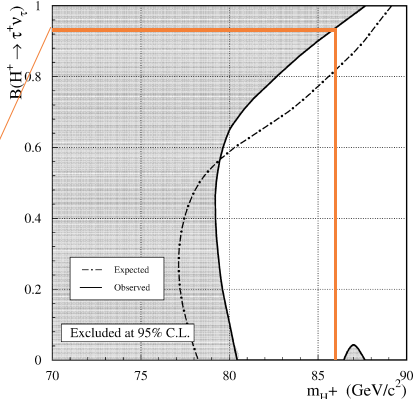
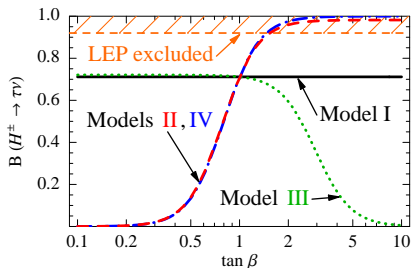
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Okay thanks to  $H^+$ 's fermiophobia for high  $\tan\beta$

# How effective is charged Higgs contribution?

- Take  $m_{H^\pm} = 81 \text{ GeV}$ ,  $\sqrt{s} = 200 \text{ GeV} \rightarrow \sigma_{HH} = 0.14 \text{ pb}$ ,  $\sigma_{WW} = 17 \text{ pb}$
- For Model I,  $B(H^\pm \rightarrow qq) = 0.3$  and  $B(H^\pm \rightarrow \tau\nu_\tau) = 0.7$
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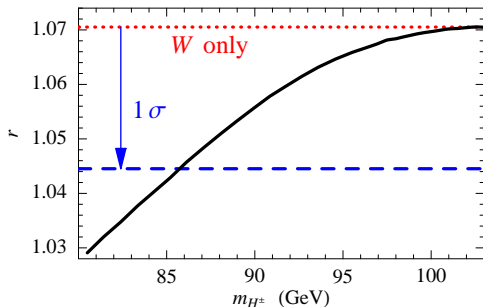
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**Lepton non-universality reduced to 1.4  $\sigma$**

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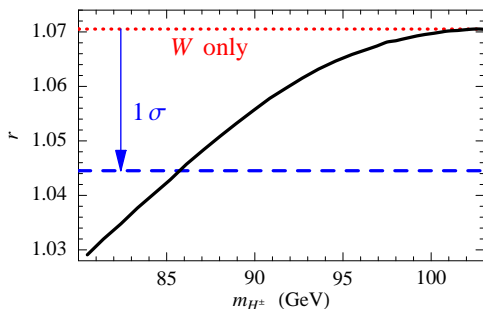


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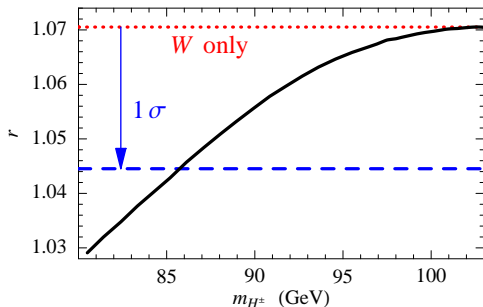
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# Test at ILC

- What to look for: charged Higgs with  $m_{H^\pm} \approx m_W$  that couples very weakly to fermions.
- Test of scenario is charged Higgs search.
- Doable at ILC.
- Beam polarization helps a lot.

| $e^-/e^+$ polarization | $\sigma_{HH}$ [pb] | $\sigma_{WW}$ [pb] | $\sigma_{HH}/\sigma_{WW}$ [%] |
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| 0%/ 0%                 | 0.10               | 7.13               | 1.4                           |
| 80%/ 0%                | 0.05               | 1.47               | 3.3                           |
| 90%/ 0%                | 0.04               | 0.76               | 5.4                           |
| 80%/60%                | 0.06               | 0.65               | 8.7                           |
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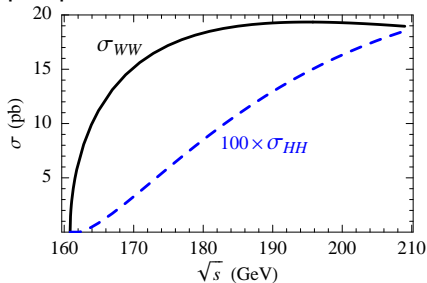
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# Summary

- A resolution is proposed of the possible lepton non-universality observed at the  $W$ -pair production experiments at LEP.
- $H^\pm$  **almost degenerate with  $W$** , within 2HDM, **could reduce 2.8  $\sigma$  of deviation down to 1.4  $\sigma$ .**
- No conflict with the existing direct or indirect constraints.  
In particular,  $\mu$ ,  $\tau$ ,  $\pi$ ,  $K$  **decays are safe.**
- Charged Higgs direct search at LEP in combination with  $b \rightarrow s\gamma$  singles out one viable type of 2HDM out of the four that are free of tree-level FCNC interactions.
- No  $\tan\beta$  dependence in prediction.
- Testable at ILC.

## More plots

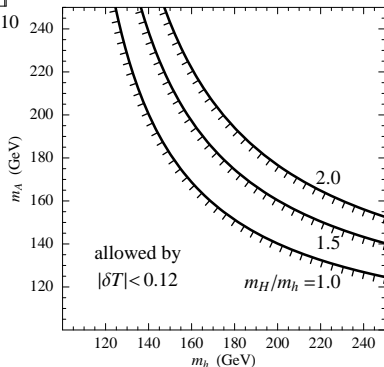
- $W$ -pair production cross section



Error of  $\sigma_{WW}$  is between 0.21 pb and 0.7 pb.

- $S, T, U$  constraints

Constraints on  $m_h$  and  $m_A$  from  $\delta T$ , with  $m_H/m_h$  fixed at 1.0, 1.5, and 2.0, respectively.  $S$  and  $U$  constraints are weaker.



# Fit in 2HDM

- Modify channel cross sections as

$$\sigma_s^{qq\tau\nu} = \sigma_{WW,s} \cdot 2B(W \rightarrow qq)B(W \rightarrow \tau\nu_\tau) + \sigma_{HH,s} \cdot 2B(H^\pm \rightarrow qq)B(H^\pm \rightarrow \tau\nu_\tau)$$

$$\sigma_s^{\tau\nu\tau\nu} = \sigma_{WW,s} \cdot B^2(W \rightarrow \tau\nu_\tau) + \sigma_{HH,s} \cdot B^2(H^\pm \rightarrow \tau\nu_\tau)$$

$$\sigma_s^{qqqq} = \sigma_{WW,s} \cdot B^2(W \rightarrow qq) + \sigma_{HH,s} \cdot B^2(H^\pm \rightarrow qq)$$

- Use  $B(H^\pm \rightarrow qq) = 0.3$  and  $B(H^\pm \rightarrow \tau\nu_\tau) = 0.7$  for Model I, and calculated  $\sigma_{HH,s}$ .
- Fit variables are  $B(W \rightarrow e\nu_e), B(W \rightarrow \mu\nu_\mu), B(W \rightarrow \tau\nu_\tau), \sigma_{WW,s}$ .