

# **$B \rightarrow D K$ measurements at CDF**

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# Outline

## Motivation

- determination of  $\gamma$  from  $B^+$  decays
- determination of  $\gamma$  from  $B_s^0$  decays

CDF measurement of  $\mathcal{B}(B^+ \rightarrow \overline{D}^0 K^+)/\mathcal{B}(B^+ \rightarrow \overline{D}^0 \pi^+)$

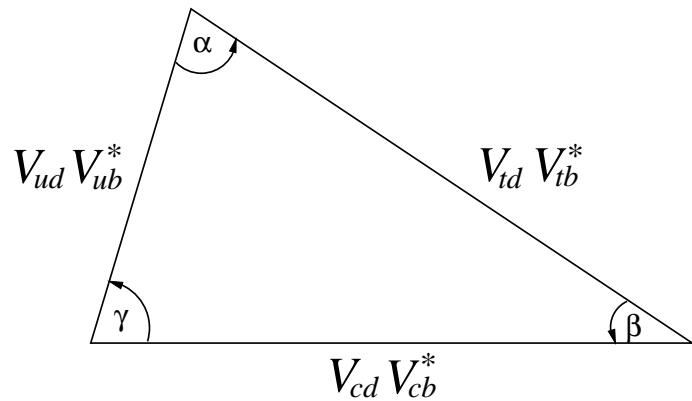
- sample
- fit method
- result

## Projection

- $B^+ \rightarrow \overline{D}^0 K^+$
- $B^+ \rightarrow D_{CP}^0 K^+$
- $B_s^0 \rightarrow D_s^\mp K^\pm$

## Motivation: CKM angle $\gamma$

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



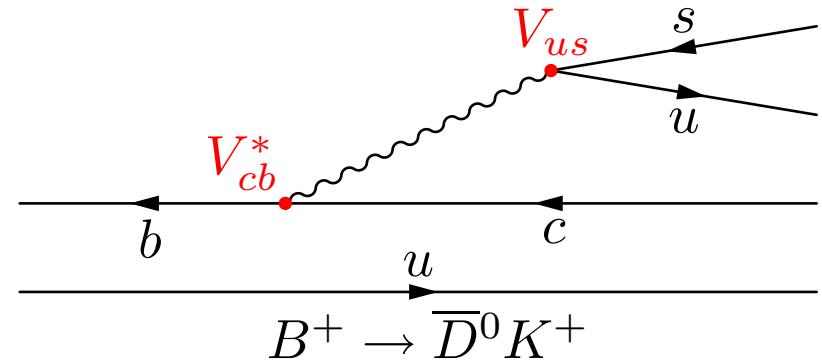
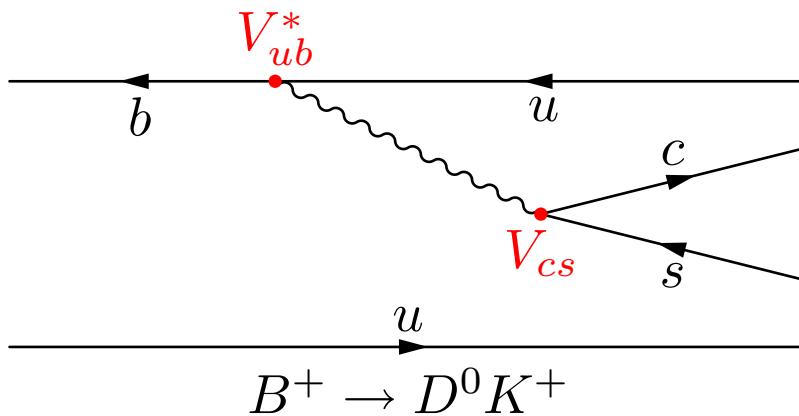
Unitarity:  $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$

$\gamma = \phi_3 = \arg(-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*)$  is the weak phase associated with  $b \rightarrow u$  transition

For observable effect, need interference:

- two diagrams with relative phase  $\gamma$
- and with comparable amplitude

## Determination of $\gamma$ from $B^+$ decays



$B^+ \rightarrow \bar{D}^0 K^+$  and  $B^+ \rightarrow D^0 K^+$  have relative weak phase  $\gamma$ ; decay width ratio  $\sim 10$

Multiple methods for interference: GLW<sup>1</sup>, ADS<sup>2</sup>, Dalitz plot<sup>3</sup>

GLW uses  $B^+ \rightarrow \bar{D}^0 (\rightarrow f_{CP}) K^+$ ,  $B^+ \rightarrow D^0 (\rightarrow f_{CP}) K^+$

At CDF:  $f_{CP}$  is  $D_{CP+}^0 \rightarrow K^+ K^-$ ,  $D_{CP+}^0 \rightarrow \pi^+ \pi^-$

Advantage of  $B^+$  measurement: no  $B$ -tagging, no time-dependence required

<sup>1</sup>M. Gronau and D. London., Phys. Lett. B **253**, 483 (1991); M. Gronau and D. Wyler, Phys. Lett. B **265**, 172 (1991).

<sup>2</sup>D. Atwood, I. Dunietz and A. Soni, Phys. Rev. D **63**, 036005 (2001) [arXiv:hep-ph/0008090].

<sup>3</sup>A. Giri, Y. Grossman, A. Soffer and J. Zupan, Phys. Rev. D **68**, 054018 (2003) [arXiv:hep-ph/0303187].

## Determination of $\gamma$ from $B^+$ decays

Need to measure:<sup>4</sup>

$$R = \frac{\mathcal{B}(B^+ \rightarrow \bar{D}^0 K^+)}{\mathcal{B}(B^+ \rightarrow \bar{D}^0 \pi^+)}$$

$$R_{\pm} = \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm}^0 K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm}^0 \pi^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm}^0 \pi^+)}$$

$$A_{CP\pm} = \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm}^0 K^-) - \mathcal{B}(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm}^0 K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm}^0 K^+)}$$

$$r = \frac{\mathcal{B}(B^+ \rightarrow D^0 K^+)}{\mathcal{B}(B^+ \rightarrow \bar{D}^0 K^+)} \approx 0.1$$

to extract  $\gamma$ , strong phase  $\delta$  (and  $r$ ):

$$R_{CP\pm} = R_{\pm}/R = 1 + r^2 \pm 2r \cos \delta \cos \gamma$$

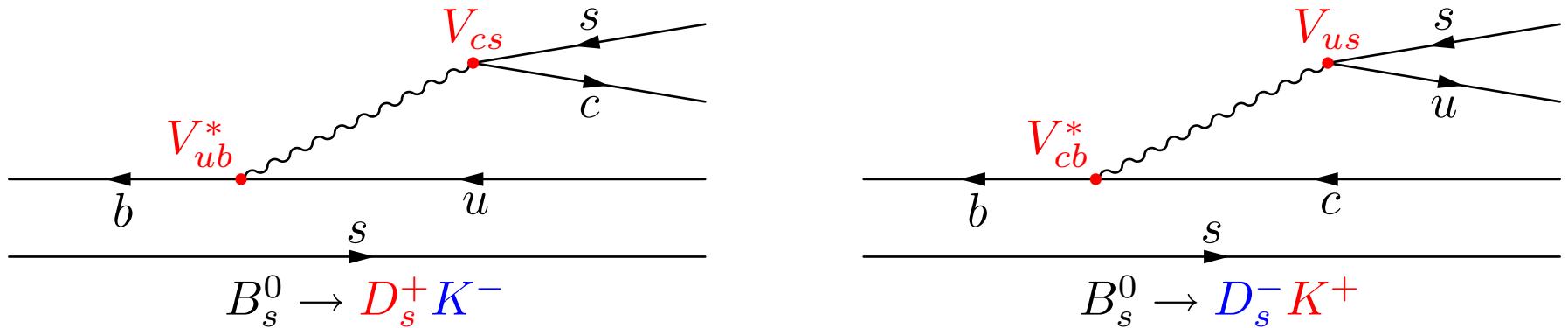
$$A_{CP+} R_{CP+} = -A_{CP-} R_{CP-} = 2r \sin \delta \sin \gamma$$

Measurement can be done with ratios of branching ratios

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<sup>4</sup>M. Gronau, Phys. Rev. D **58**, 037301 (1998) [arXiv:hep-ph/9802315].

# Determination of $\gamma$ from $B_s^0$ decays



$B_s^0 \rightarrow D_s^- K^+$ ,  $B_s^0 \rightarrow D_s^+ K^-$  have relative phase  $\gamma$ , comparable amplitude

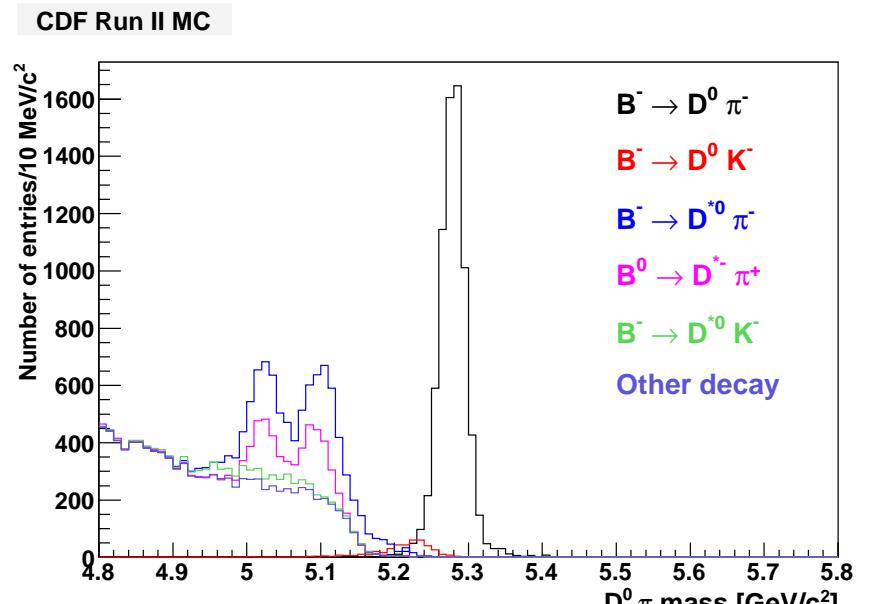
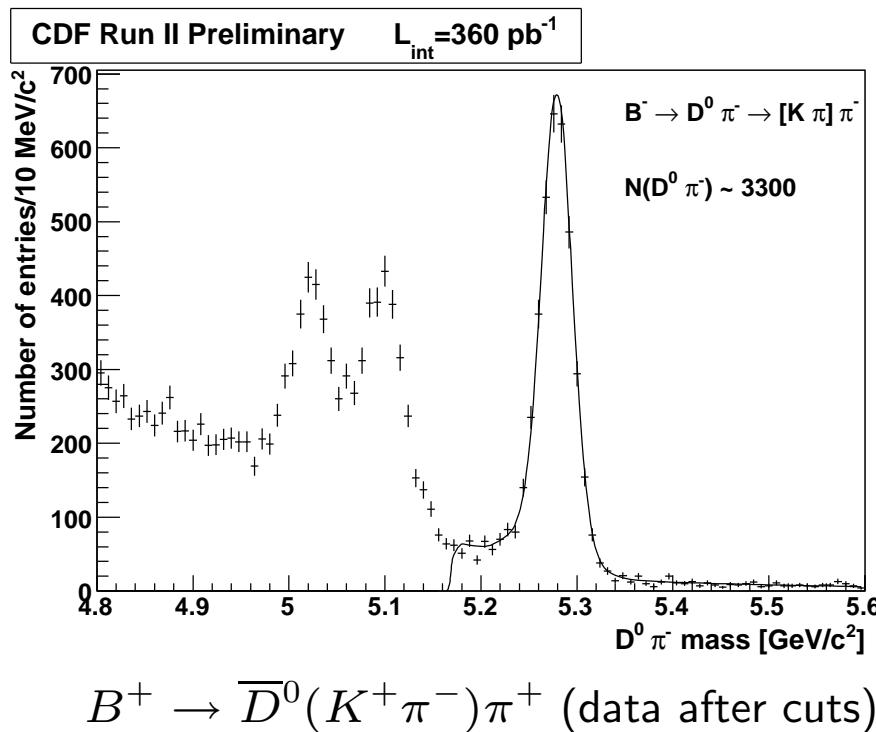
$B_s^0 \rightarrow D_s^- K^+$  interferes with  $B_s^0 \xrightarrow{\text{(mixing)}}$   $\bar{B}_s^0 \rightarrow D_s^- K^+$

Time-dependent, flavor-tagged measurement<sup>5</sup>

<sup>5</sup>R. Aleksan, I. Dunietz and B. Kayser, Z. Phys. C **54**, 653 (1992).

# Measuring $\mathcal{B}(B^+ \rightarrow \overline{D}^0 K^+)/\mathcal{B}(B^+ \rightarrow \overline{D}^0 \pi^+)$

$R = \mathcal{B}(B^+ \rightarrow \overline{D}^0 K^+)/\mathcal{B}(B^+ \rightarrow \overline{D}^0 \pi^+)$  is first experimental step in GLW method:  
high-statistics mode compared to  $D_{CP}^0$  modes

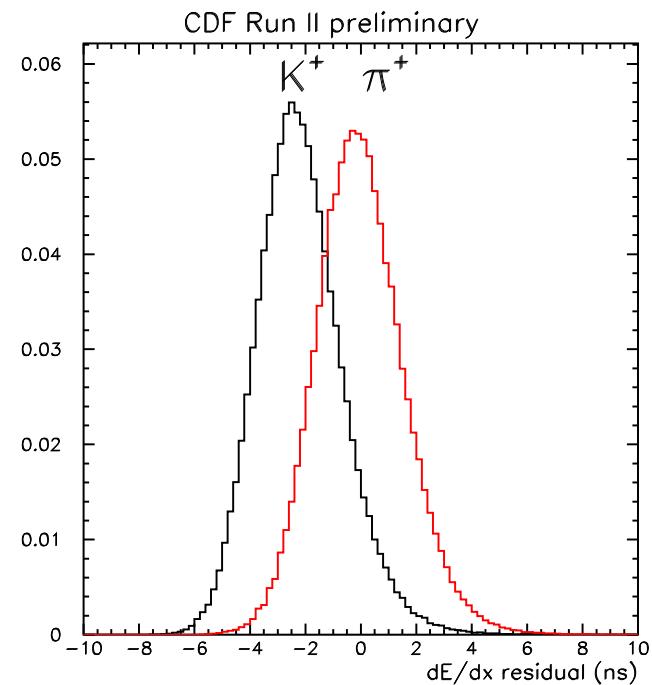
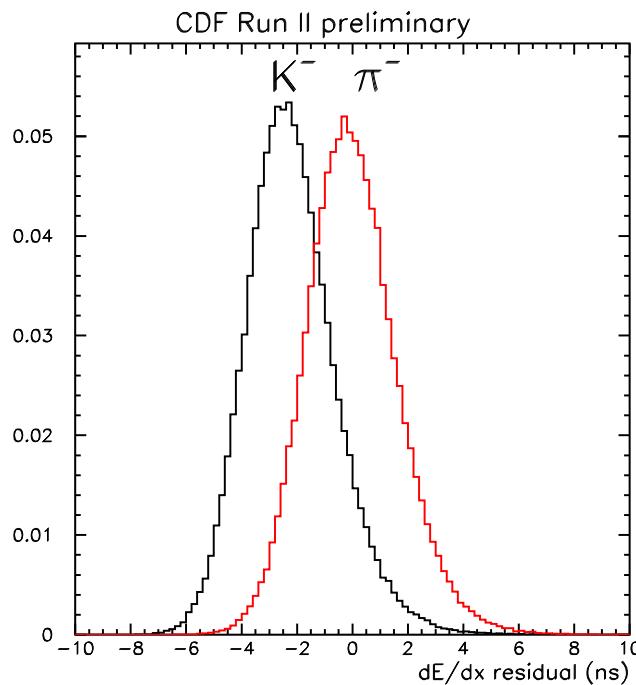


Strategy: use  $D^0\pi$  mass and PID to separate  $D^0\pi$ ,  $D^0K$  and backgrounds

## Separating $D^0K$ from $D^0\pi$ : $dE/dx$

Use  $dE/dx$  of track recoiling against  $D^0$ :

$$ID = \frac{dE/dx_{\text{meas}} - dE/dx_{\text{exp}}(\pi)}{dE/dx_{\text{exp}}(K) - dE/dx_{\text{exp}}(\pi)}$$

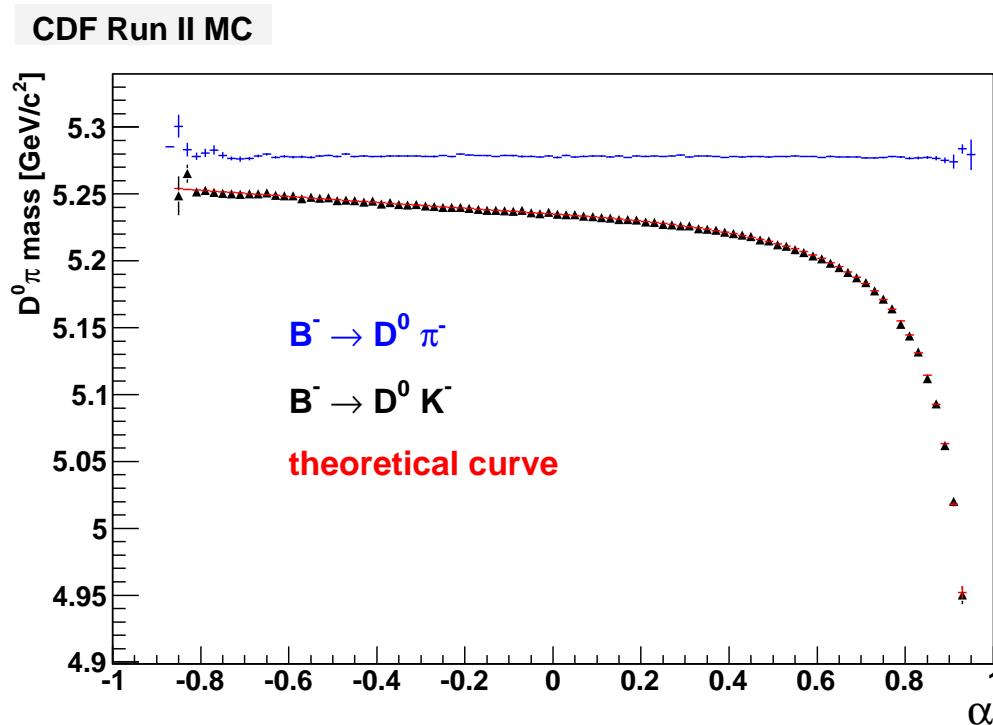


$1.5\sigma$  separation from  $dE/dx$  between  $K$  and  $\pi$

# Separating $D^0K$ from $D^0\pi$ : Kinematics

Reconstructed ( $D^0\pi$ ) mass depends on momentum imbalance:

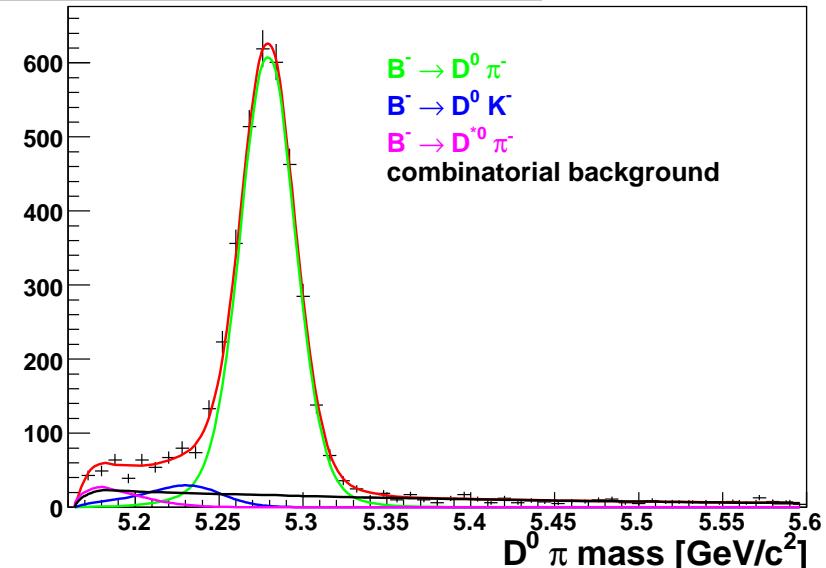
$$\alpha = \begin{cases} 1 - p_{\text{tr}}/p_{D^0} & \text{if } p_{\text{tr}} < p_{D^0} \\ -(1 - p_{D^0}/p_{\text{tr}}) & \text{if } p_{\text{tr}} \geq p_{D^0} \end{cases}$$



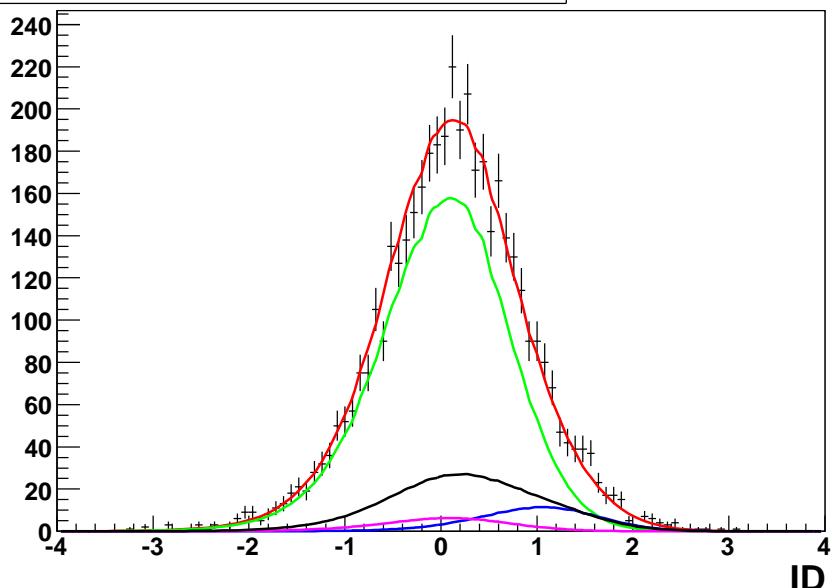
# Fit

- unbinned maximum-likelihood fit
- fit in narrow range  $[5.17, 5.6]$  GeV
- fit components:  $D^0\pi$ ,  $D^0K$ ,  $D^{*0}\pi$ , combinatorial background
- fit variables:  $m(D^0\pi)$ ,  $\alpha$ ,  $dE/dx$

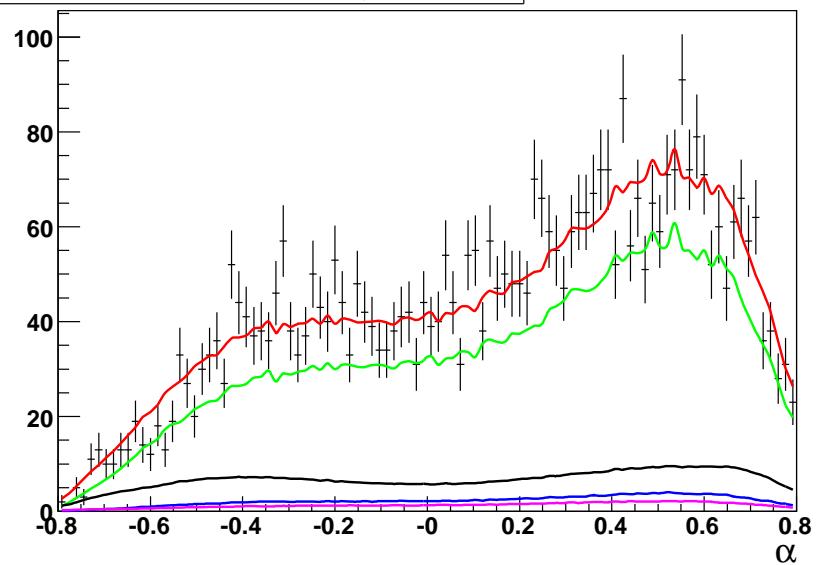
CDF Run II Preliminary  $L_{\text{int}} = 360 \text{ pb}^{-1}$



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## Systematic errors

source	error
mass resolution tails	0.0006
$B^+$ mass	0.001
$dE/dx$	0.0015
combinatorial background model	0.001
alternate $D^{*0}$ mass model	0.001
$D^{*0}$ mass-model parameters left free	0.003
MC statistics + XFT efficiency	0.002
total	0.004

largest error:  $D^{*0}$  mass pdf

# Result

CDF result on  $360 \text{ pb}^{-1}$  ( $\sim 3300 D^0\pi$  events):

$$R = \frac{\mathcal{B}(B^+ \rightarrow \overline{D}^0 K^+)}{\mathcal{B}(B^+ \rightarrow \overline{D}^0 \pi^+)} = (6.5 \pm 0.7(\text{stat}) \pm 0.4(\text{syst})) \times 10^{-2}$$

Also measured by BaBar<sup>6</sup>, CLEO<sup>7</sup> and Belle:<sup>8</sup>

experiment	measurement ( $10^{-2}$ )	$D^0\pi$	sample size
BaBar	$8.31 \pm 0.35 \pm 0.20$	$\sim 10000$	$(61.0 \times 10^6 B\overline{B})$
CLEO	$9.9^{+1.4+0.7}_{-1.2-0.6}$	$\sim 500$	$(15.3 \text{ fb}^{-1})$
Belle	$7.7 \pm 0.5 \pm 0.6$	$\sim 6000$	$(85.4 \times 10^6 B\overline{B})$

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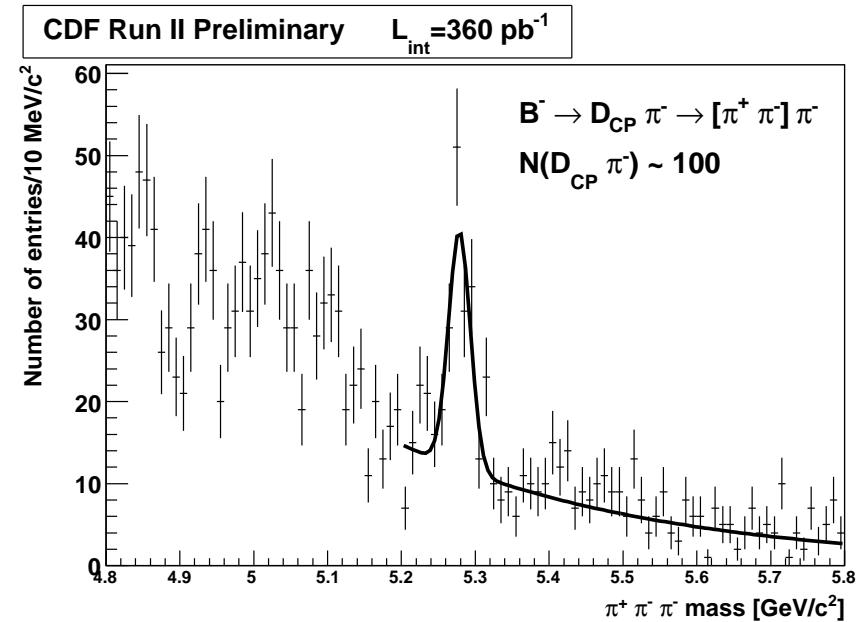
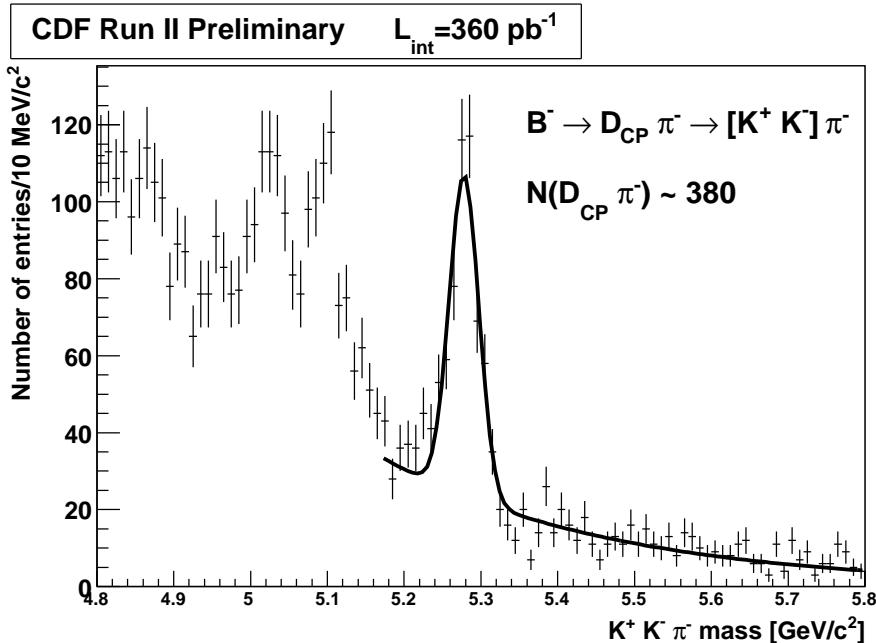
<sup>6</sup>B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. Lett. **92**, 202002 (2004) [arXiv:hep-ex/0311032].

<sup>7</sup>A. Bornheim *et al.* [CLEO Collaboration], Phys. Rev. D **68**, 052002 (2003) [arXiv:hep-ex/0302026].

<sup>8</sup>S. K. Swain *et al.* [Belle Collaboration], Phys. Rev. D **68**, 051101 (2003) [arXiv:hep-ex/0304032].

# Outlook: $B^+ \rightarrow D_{CP}^0 K^+$

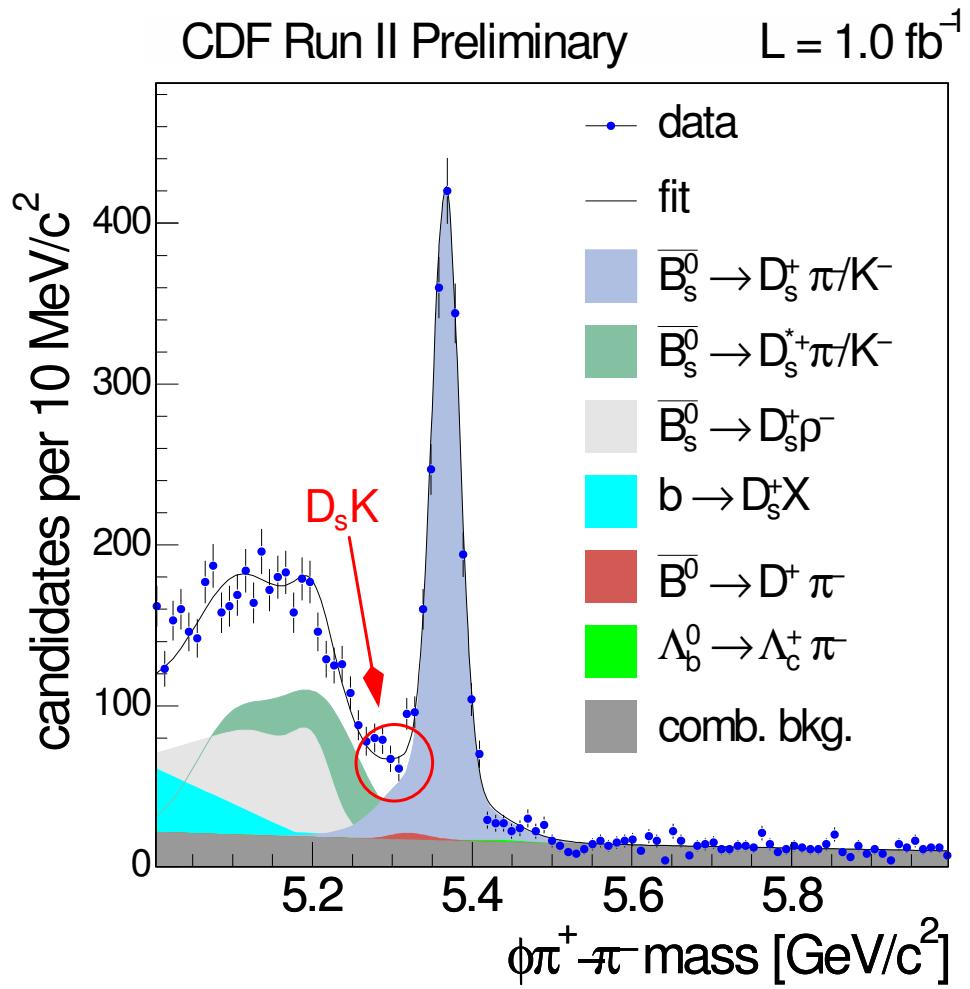
Statistics in  $360 \text{ pb}^{-1}$ :  $3300 D^0 \pi$ ,  $500 D_{CP+}^0 \pi$



Analysis in progress on  $1 \text{ fb}^{-1}$ :

- $\times 3$  statistics
- template mass pdfs
- wider fit range
- improved BG model

## Outlook: $\mathcal{B}(B_s^0 \rightarrow D_s K)/\mathcal{B}(B_s^0 \rightarrow D_s \pi)$



- $\mathcal{B}(B_s \rightarrow D_s K)/\mathcal{B}(B_s \rightarrow D_s \pi)$  measurement in progress
- first measurement of this ratio; potentially large interference
- this measurement will decide how much data is required for time-dependent, flavor-tagged  $B_s^0 \rightarrow D_s^\pm K^\mp$  analysis

## In summary

CDF has measured  $R$  in  $360 \text{ pb}^{-1}$ :

$$R = \frac{\mathcal{B}(B^+ \rightarrow \overline{D}^0 K^+)}{\mathcal{B}(B^+ \rightarrow \overline{D}^0 \pi^+)} = (6.5 \pm 0.7(\text{stat}) \pm 0.4(\text{syst})) \times 10^{-2}$$

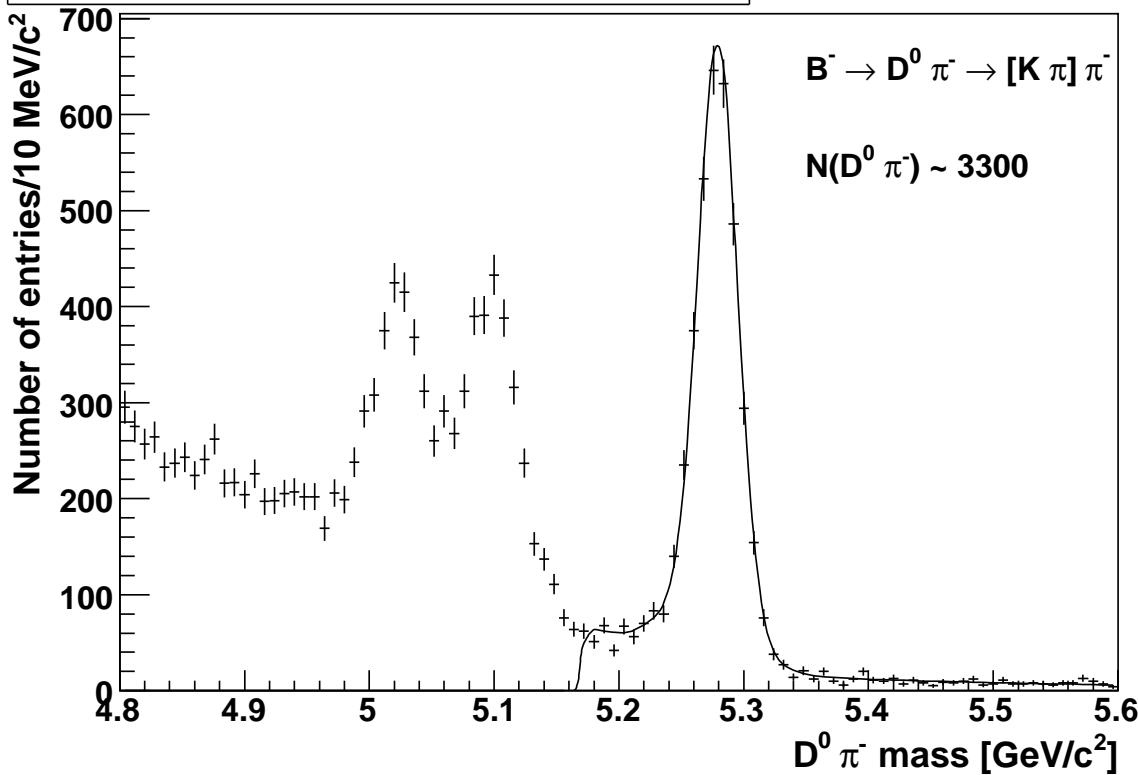
Future steps in Cabibbo-suppressed program at CDF:

- $R$  measurement in  $1 \text{ fb}^{-1}$  in progress
- $A_{CP+}$  and  $R_{CP+}$  are next
- $\mathcal{B}(B_s \rightarrow D_s K)/\mathcal{B}(B_s \rightarrow D_s \pi)$  is also in the pipeline

**Bonus slides**

# Sample selection

CDF Run II Preliminary     $L_{\text{int}} = 360 \text{ pb}^{-1}$



- $\chi^2_{\text{3D}}(B) < 15$
- $\text{iso} > 0.5$
- $L_{xy}(B)/\sigma_{L_{xy}}(B) > 8$
- $L_{xy}(B \rightarrow D) > 150 \mu\text{m}$
- $|d_0(B)| < 80 \mu\text{m}$
- $\Delta R < 2$
- $p_{\text{T}}(\pi_B) > 2.0 \text{ GeV}$
- $\pi_B$  is trigger track

Remove prompt physics and combinatorial background

# Fit

fit in narrow range [5.17, 5.6] GeV

fit components:  $D^0\pi$ ,  $D^0K$ ,  $D^{*0}\pi$ , combinatorial background

fit variables:  $m$ ,  $\alpha$ ,  $p_{\text{tot}}$ ,  $dE/dx$

$$\log \mathcal{L} = \sum_i^{N_{\text{events}}} ((1 - b)(f_\pi F_\pi(\boldsymbol{\theta}_i) + (1 - f_\pi)F_K(\boldsymbol{\theta}_i)) + \\ b(f_{D^*}B_{D^*}(\boldsymbol{\theta}_i) + (1 - f_{D^*})B_{\text{comb}}(\boldsymbol{\theta}_i))), \quad \boldsymbol{\theta} = (\alpha, p_{\text{tot}}, m_{D^0\pi}, ID)$$

$$F_j(\alpha, p_{\text{tot}}, m_{D^0\pi}, ID) = G(m_{D^0\pi} - M(\alpha, p_{\text{tot}}))P(\alpha, p_{\text{tot}})P(ID)$$

$$B_j(\alpha, p_{\text{tot}}, m_{D^0\pi}, ID) = B(m_{D^0\pi})P(\alpha, p_{\text{tot}})P(ID)$$

$P(\alpha, p_{\text{tot}})$  from MC for  $B$ -physics components, from high-sideband negative- $L_{xy}$   
 $B^+$  for combinatorial