

Earth and its energy budget

William F. McDonough

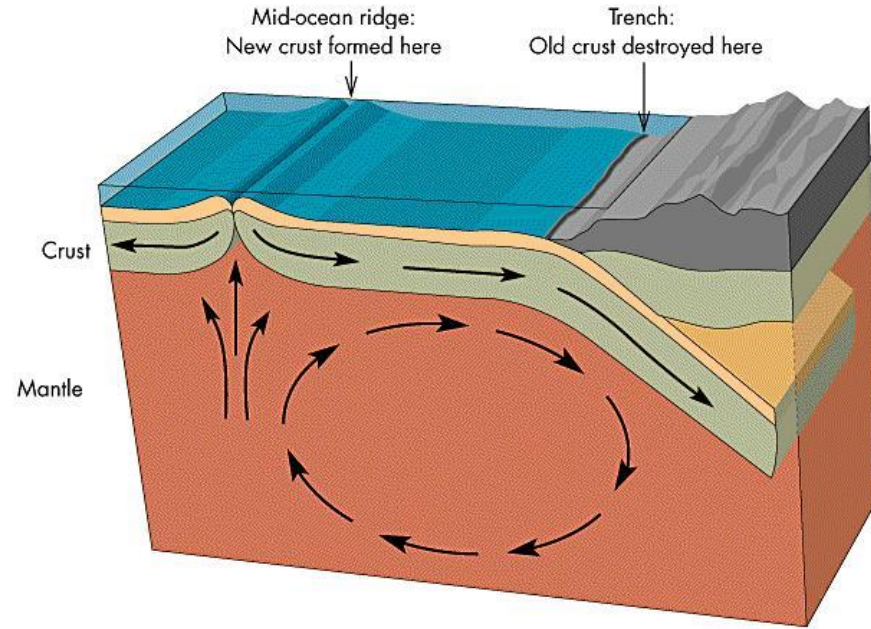
Advanced Institute for Marine Ecological Change,
Research Center of Neutrino Sciences, & Earth Sciences,
Tohoku University, Sendai, JAPAN

and

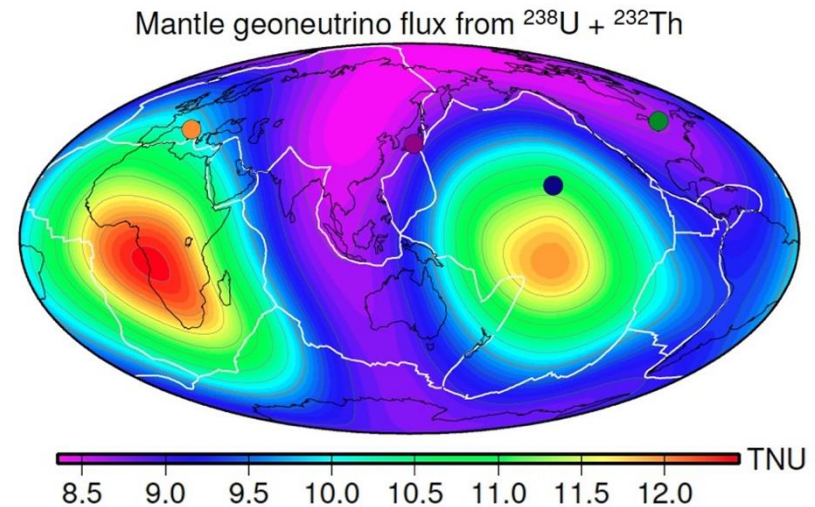
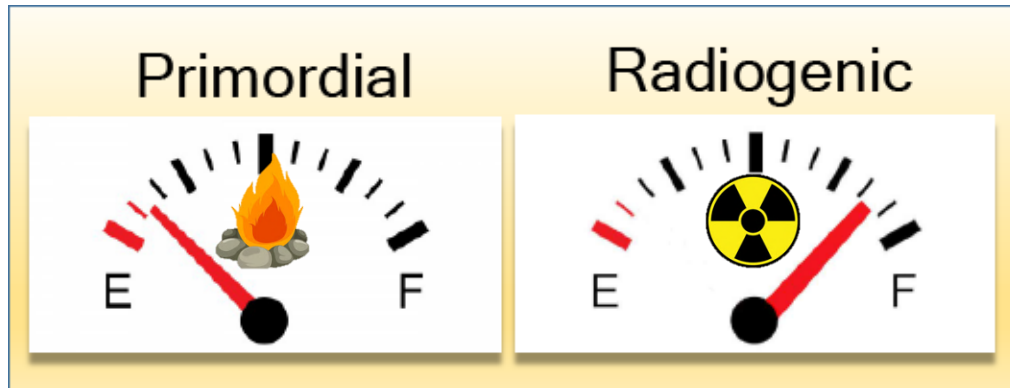
Geology, University of Maryland, College Park, MD, USA



How much fuel is left to drive Plate Tectonics?



46±3 TW

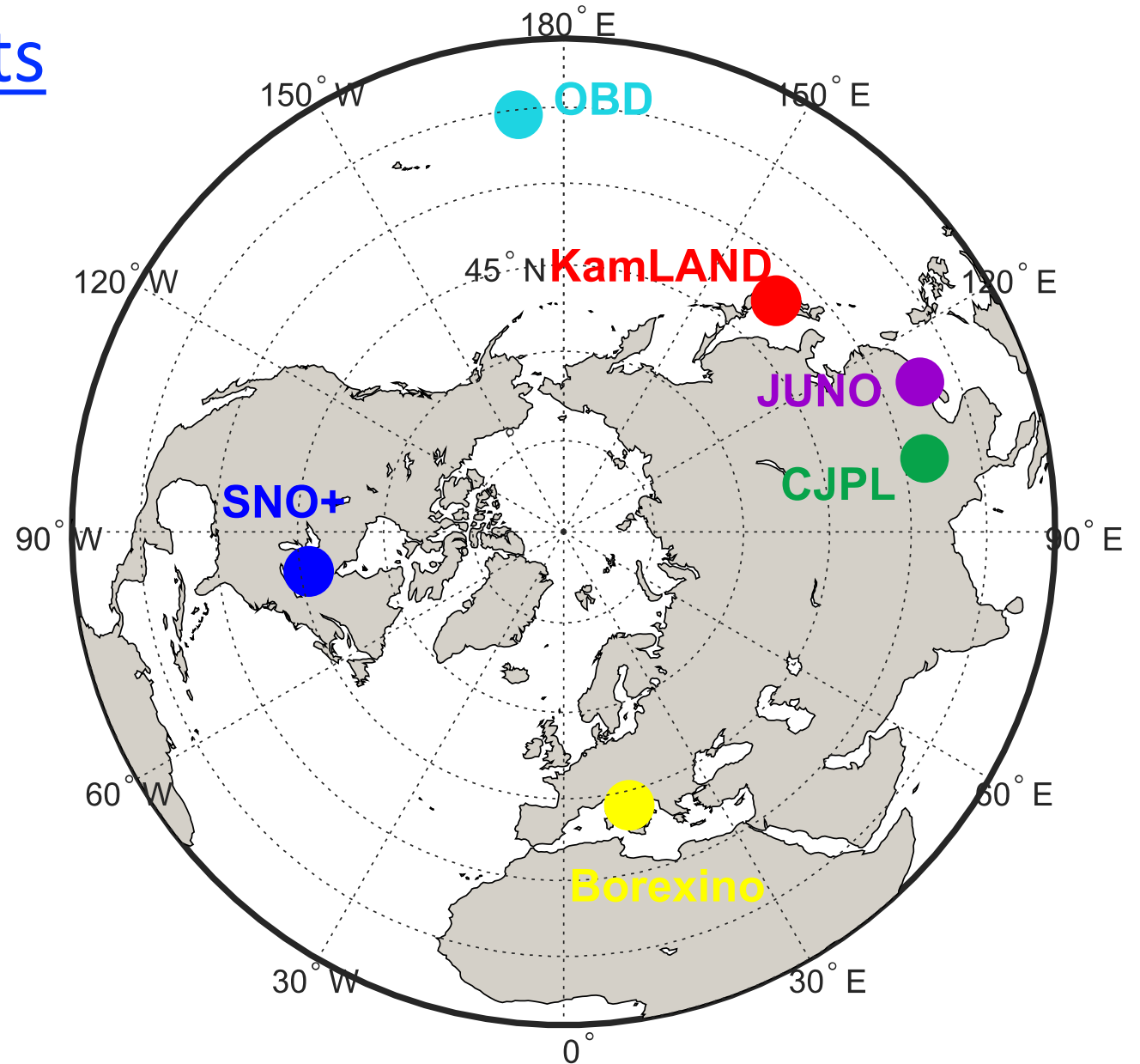


Geoneutrino experiments

KamLAND counting
Borexino finished
SNO+ counting*

JUNO filing!+,
and counting August '25
CJPL development
OBD development

* reporting in 2025



Geoneutrino Flux on Earth Surface

Activity and number of produced geoneutrinos

$$\frac{d\phi(E_\nu, \mathbf{r})}{dE_\nu} = A \frac{dn(E_\nu)}{dE_\nu} \int_{V_\oplus} d^3\mathbf{r}' \frac{a(\mathbf{r}')\rho(\mathbf{r}')P(E_\nu, |\mathbf{r} - \mathbf{r}'|)}{4\pi|\mathbf{r} - \mathbf{r}'|^2}$$

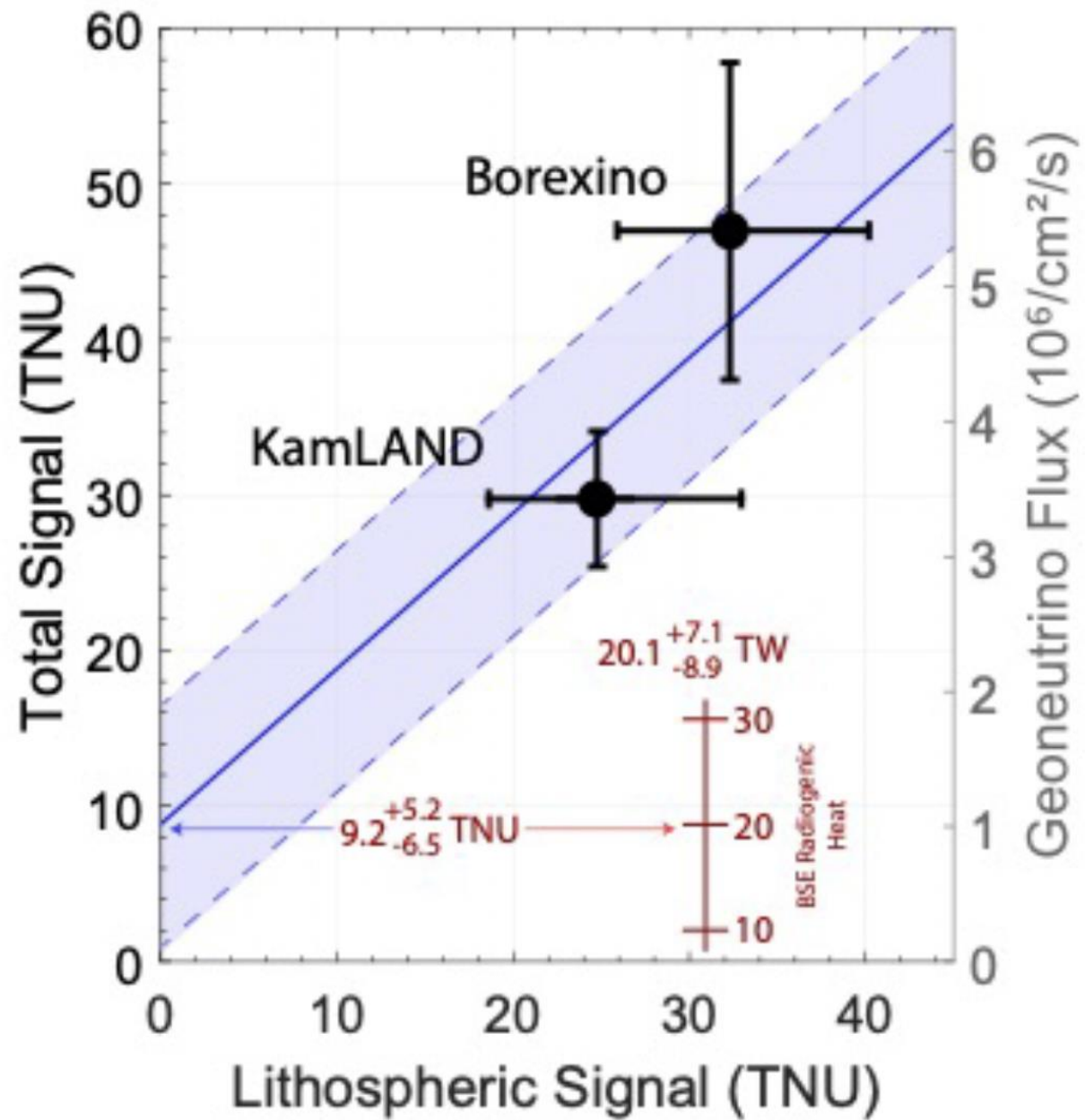
Volume of source unit

Abundance and density of the source unit

Survival probability function

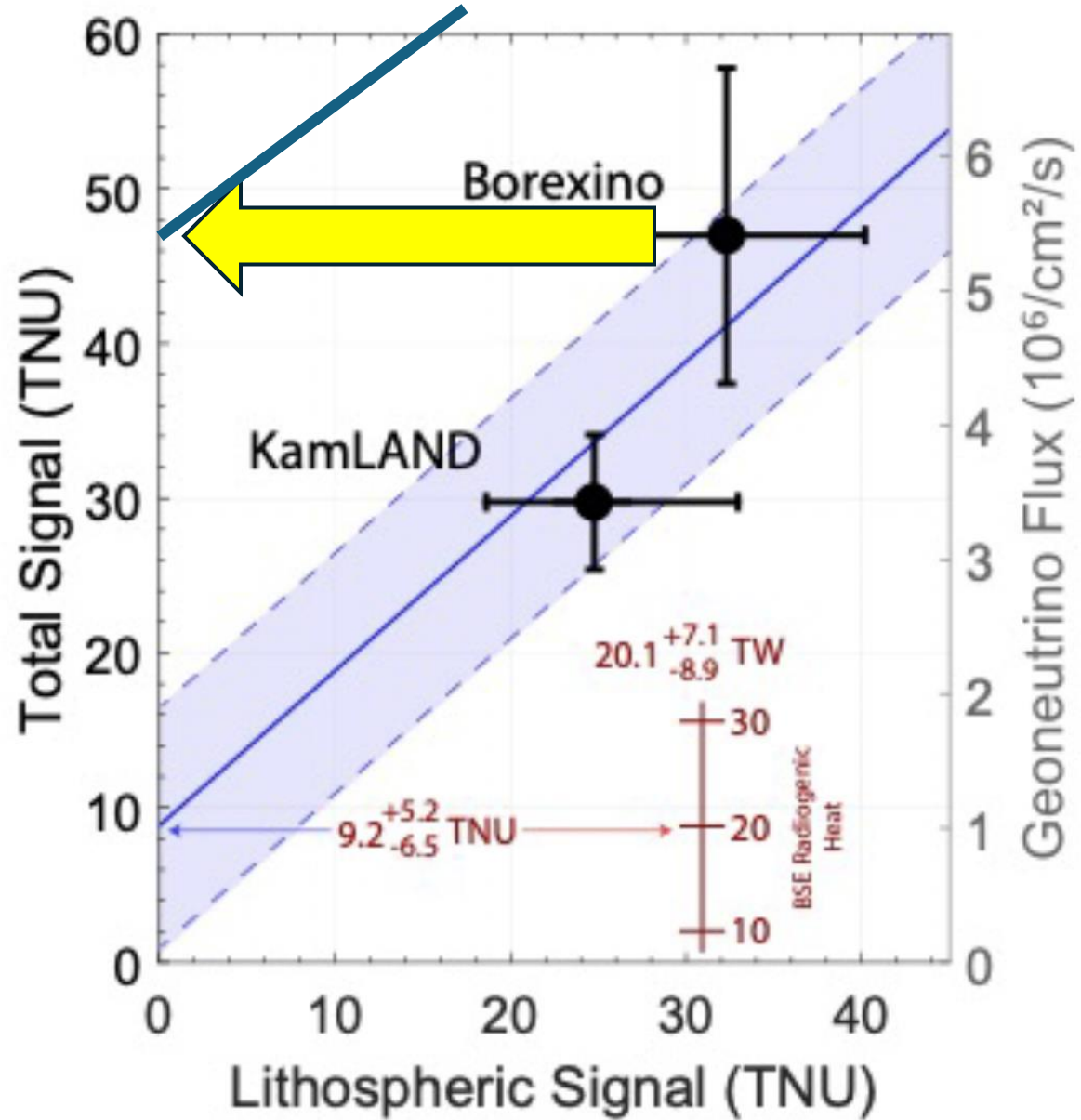
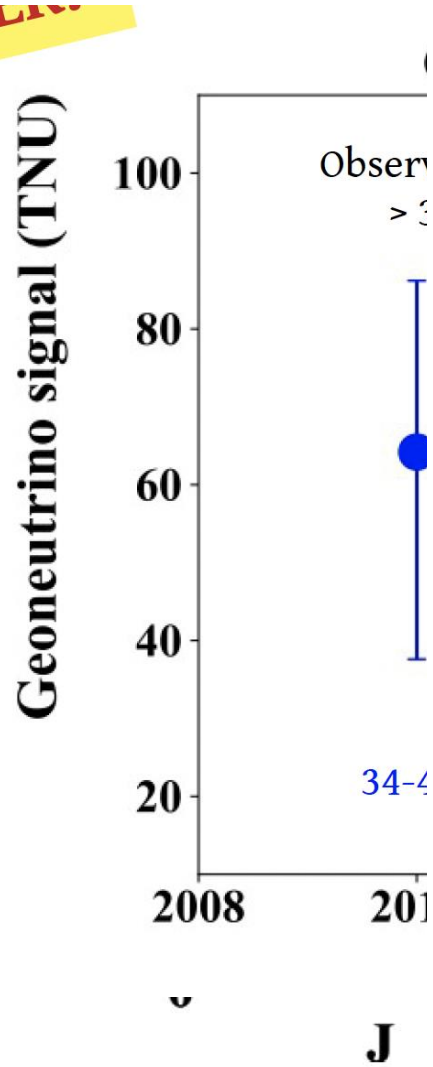
Distance between source unit and detector

Earth structure (ρ and L) and **chemical composition** (a)



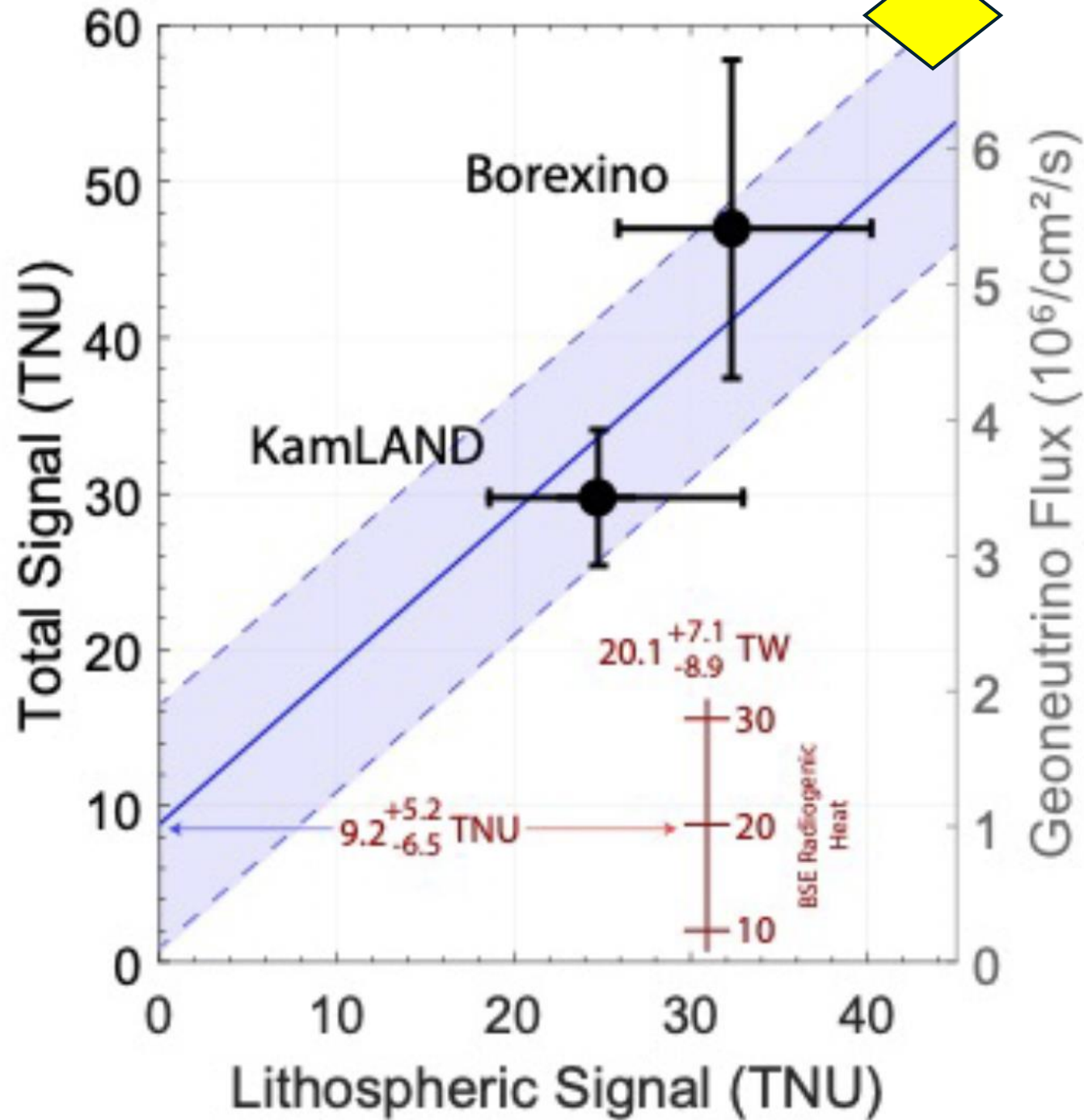
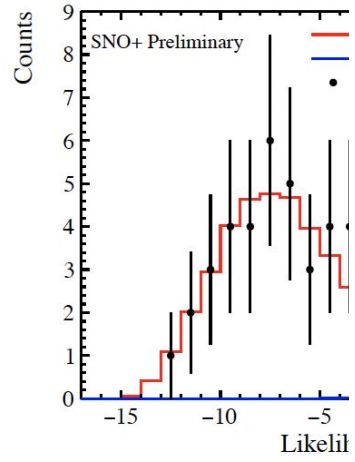
2019

Geoneu



The S

- observing channel
- second
- prelim. g



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V. A. MOZART

t time this

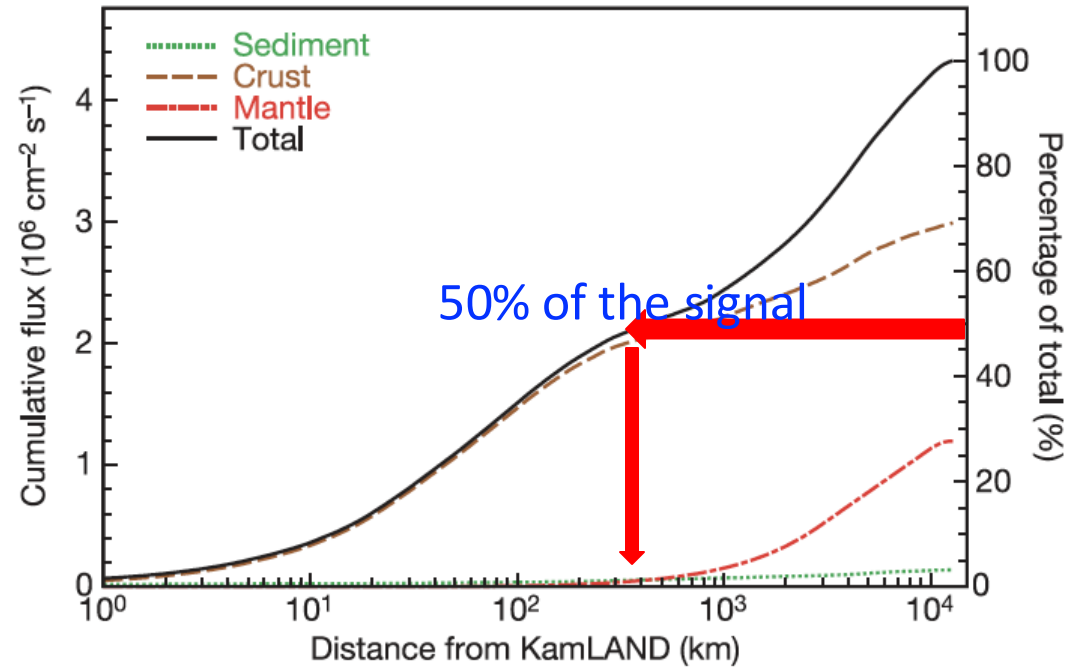
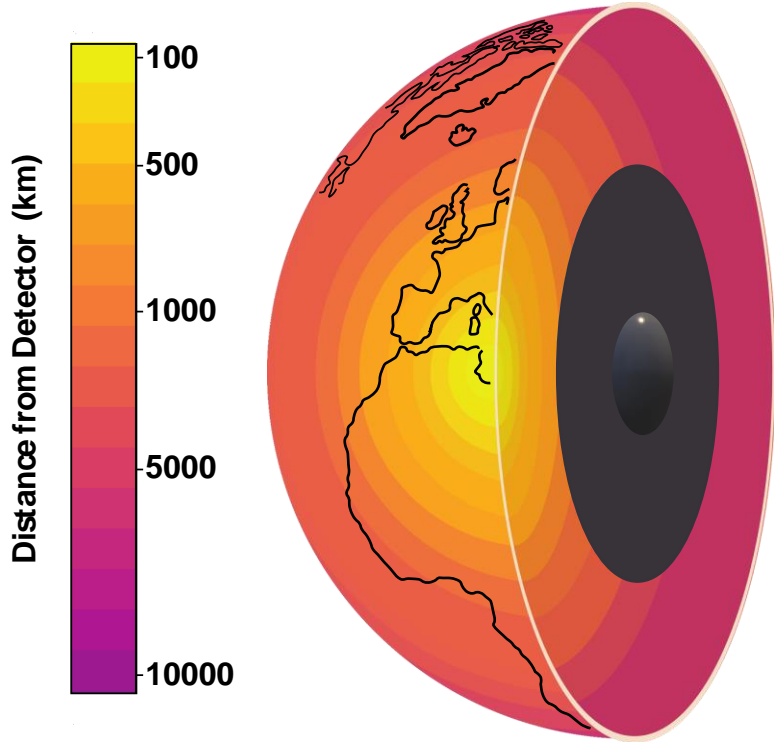
s soon)

Data
reactor- $\bar{\nu}$
-n
geo- $\bar{\nu}$
other

Small plot showing detected energy (MeV) on the x-axis (6 to 7) with data points and a fit curve.

$$S_{total} = S_{lithosphere} + S_{mantle} + S_{core}$$

$$S_{lithosphere} = S_{Near\ Field\ Lithosphere} + S_{Far\ Field\ Lithosphere}$$



$$S_{total} \propto \int_{V_{\oplus}} \frac{\alpha[U] + \beta[Th]}{r^2}$$



“... Borexino estimate of the total radiogenic heat of the Earth is $38.2^{+13.6}_{-12.7}$ TW...” Borexino collaboration (2020, PRD)

Quantifying Earth's radiogenic heat budget

Laura G. Sammon^{a,*}, William F. McDonough^{a,b}

[Earth and Planetary Science Letters 593 \(2022\) 117684](#)

Italian surface rocks

Names of volcanoes
ages (Myrs)

Median Concentration
(ppm) count

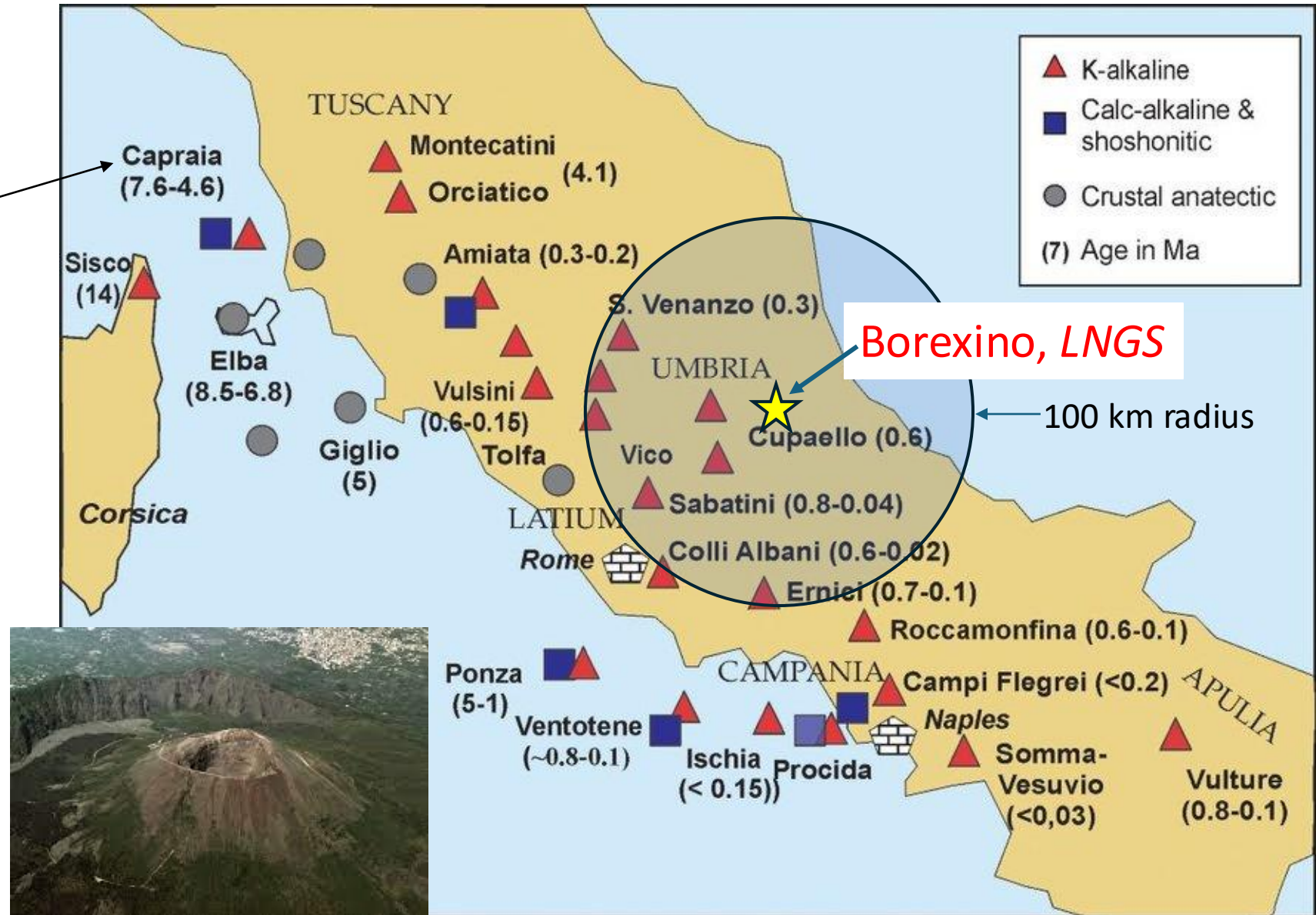
Th 35.0 2808
U 8.5 1854

Avg. upper crust: Th 10.5 ppm
U 2.7 ppm

Th/U values count

Th/U 4.1 ± 3.4 1845
Kappa 4.2 ± 3.5 1845
Kappa_{pb} 4.06 ± 0.07 386

It is important to do the geology!

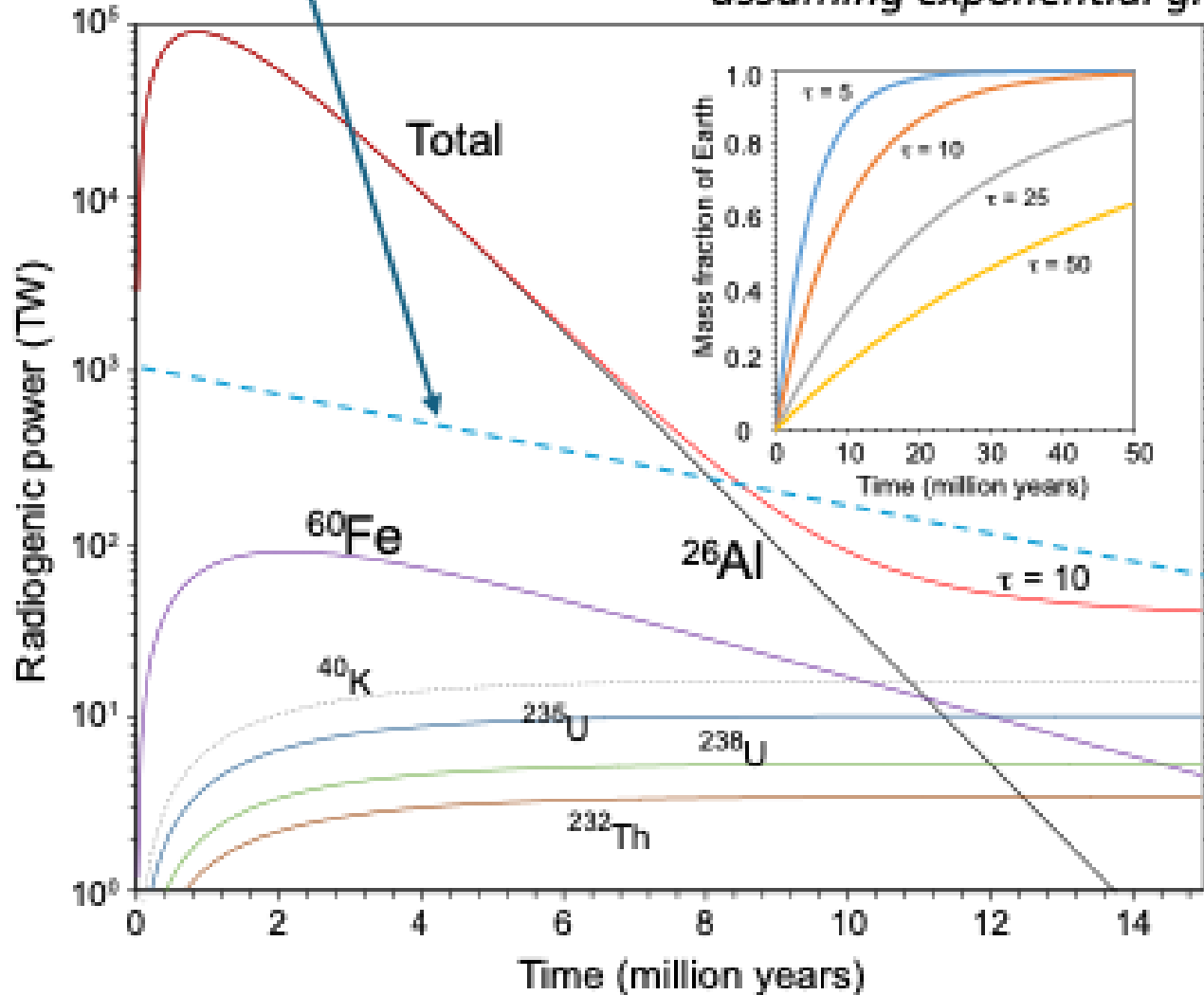


Agostini et al., (2020; Phys Rev D) reported no surface igneous rocks in the region!!!

Simple primordial accretion energy curve

$$M_{(t)}/M_{\text{final}} = 1 - \exp(-t/\tau)$$

assuming exponential growth



assumes

Earth's $\tau_{\text{accretion}} = 10$ million years

first 15 million years

Model reported in McDonough et al 2020

Thermal evolution of the Earth

Current condition

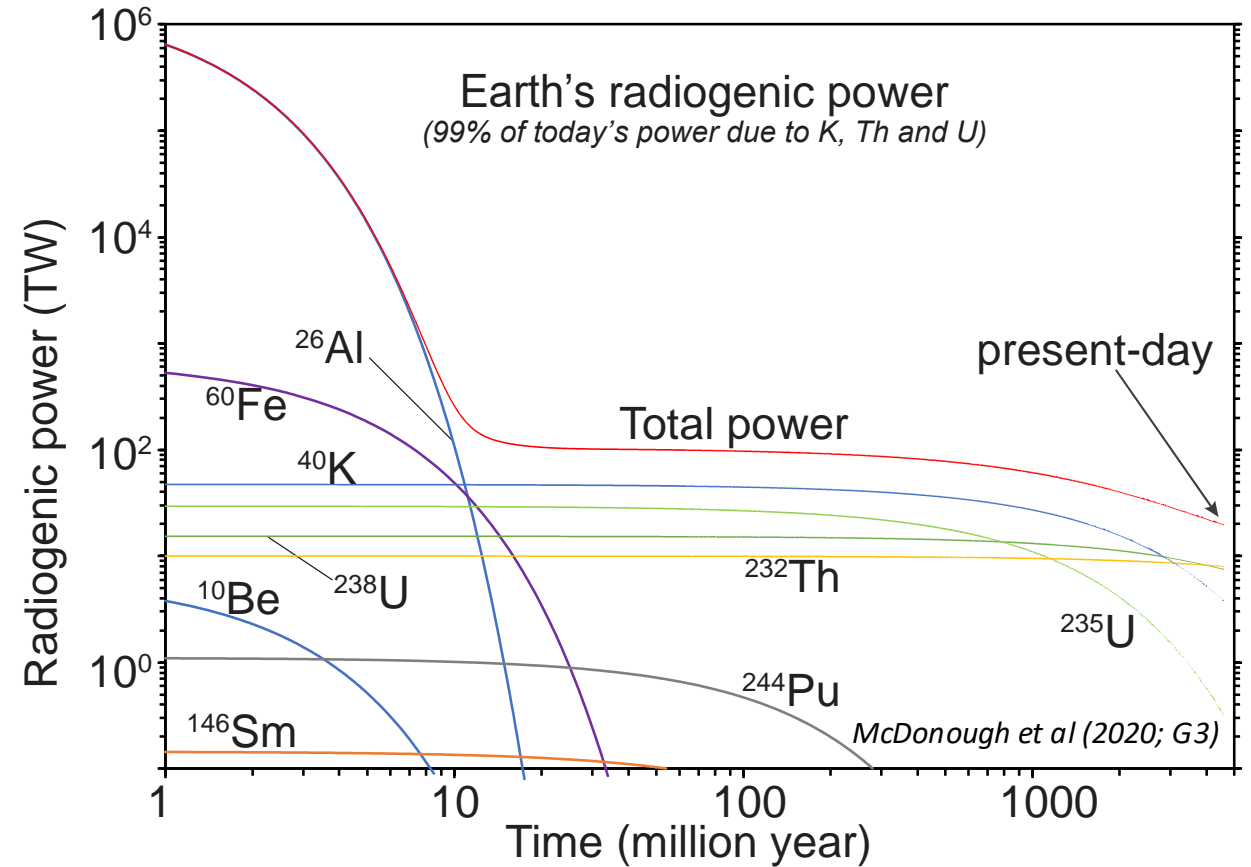
Earth's heat flux	TW
<i>total</i> $Q_{surface\ flux}$	46
<i>core</i> $Q_{cooling}$	13
<i>mantle</i> $Q_{cooling}$	13
<i>mantle</i> $Q_{radiogenic\ heating}$	13*
<i>crust</i> $Q_{radiogenic\ heating}$	7*

*assuming McDonough and Sun (1995, CG) Earth model

$$M_{(t)}/M_{final} = 1 - \exp(-t/\tau)$$

assuming exponential growth

Earth's τ age = 10 Ma



SUMMARY

Earth's radiogenic (K, Th & U) power *(assuming Th/U=3.9; K/U = 14,000)*

21_{-8}^{+7} TW - Borexino 20_{-7}^{+6} TW – KamLAND

: 20_{-9}^{+7} TW, 20.5 ppb U, 77 ppb Th, & 2.7 x CI abundances

-- Future is bright—

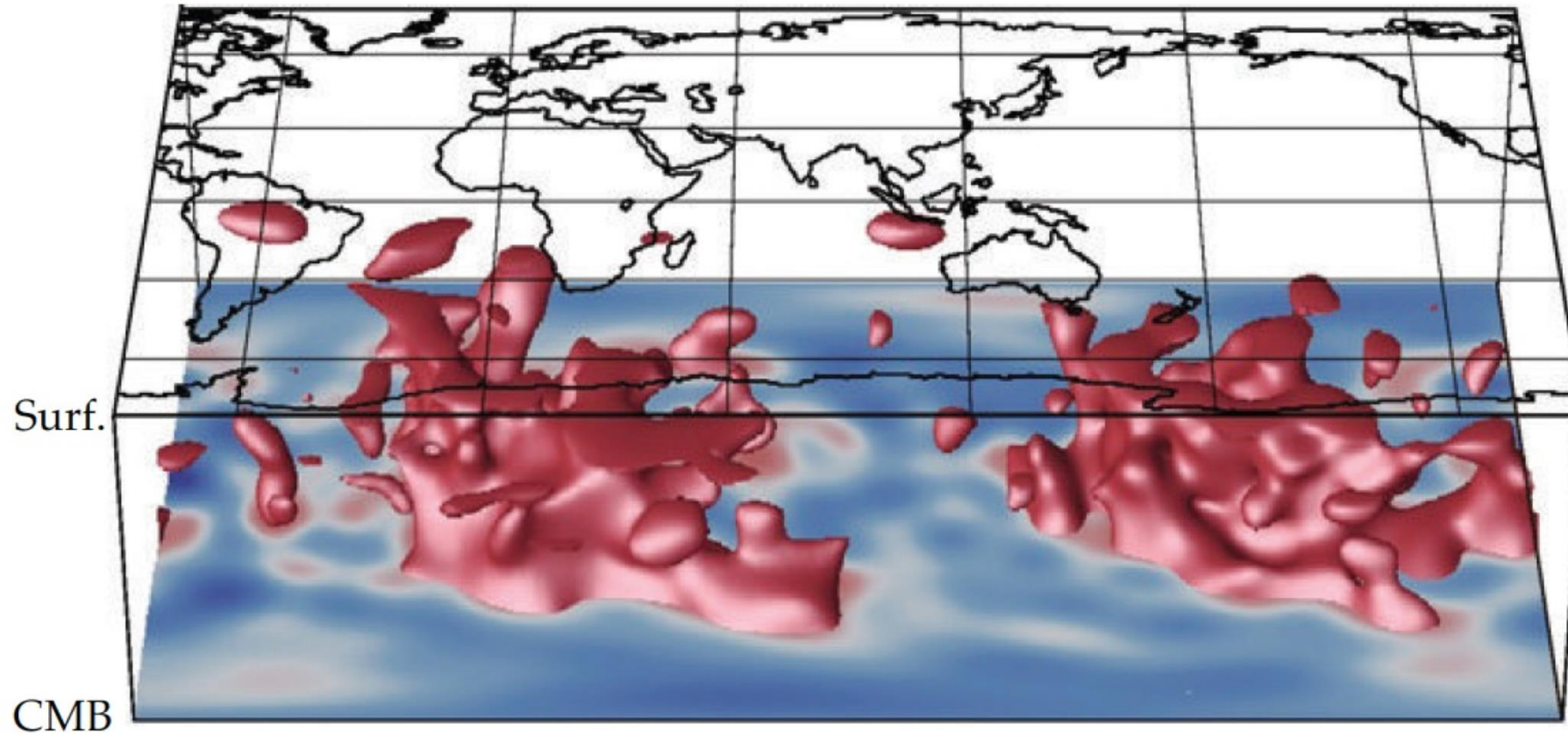
On-line and next generation [GEO-NEUTRINO](#) experiments:

- **SNO+** online since late 2022, ☺ expects to report 2025
- **JUNO**: 2025, enormous detector & big background...
- **CJPL**: 2030(?), superb experiment, great for crust & mantle
- **OBD**: looks only at the mantle

What's hidden in the mantle?

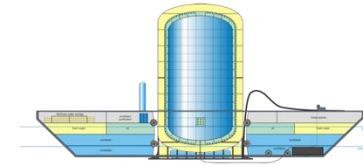
Can we image it with geonus?

Seismically slow “red” regions in the deep mantle

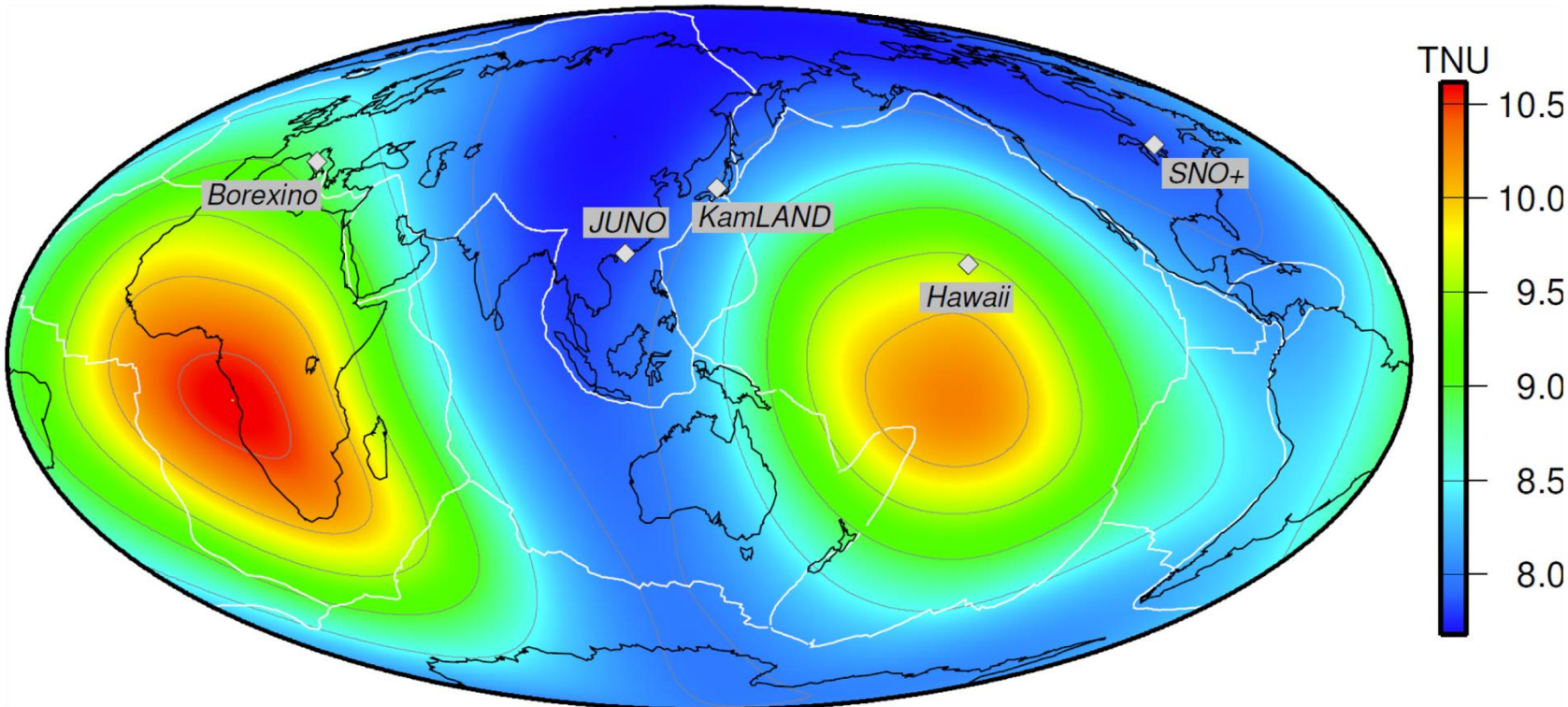


From Alan McNamara after Ritsema et al (Science, 1999)

Testing Earth Models



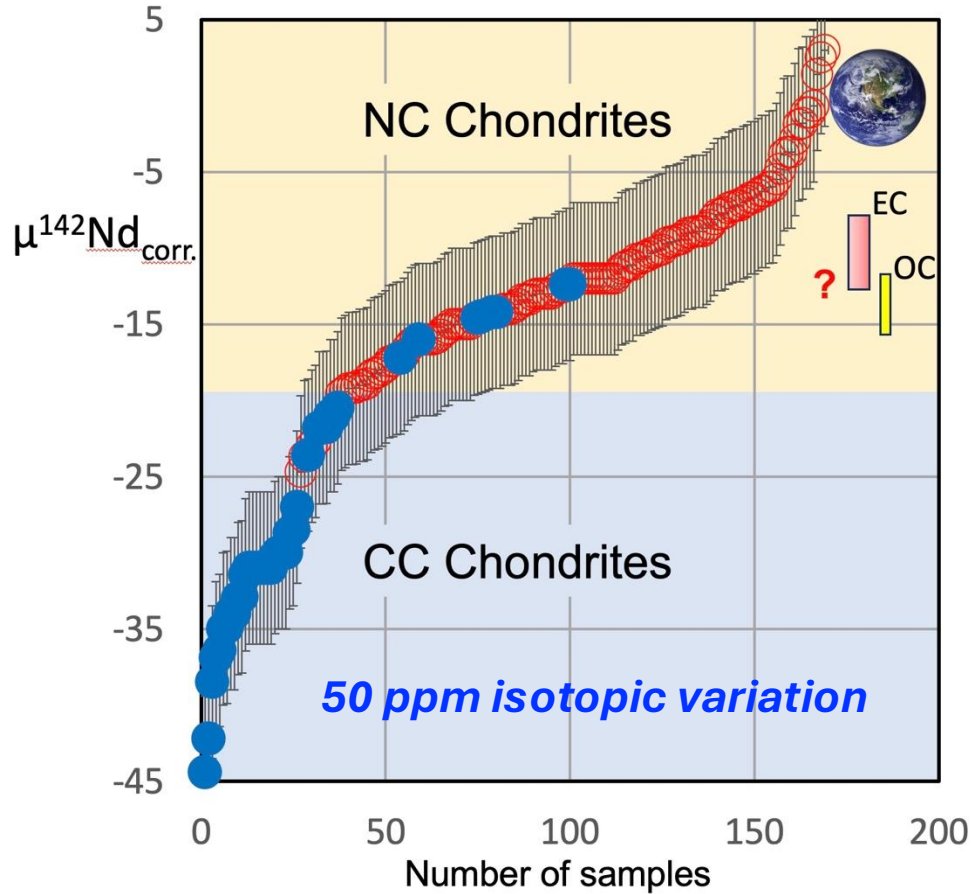
Mantle geoneutrino flux (^{238}U & ^{232}Th)



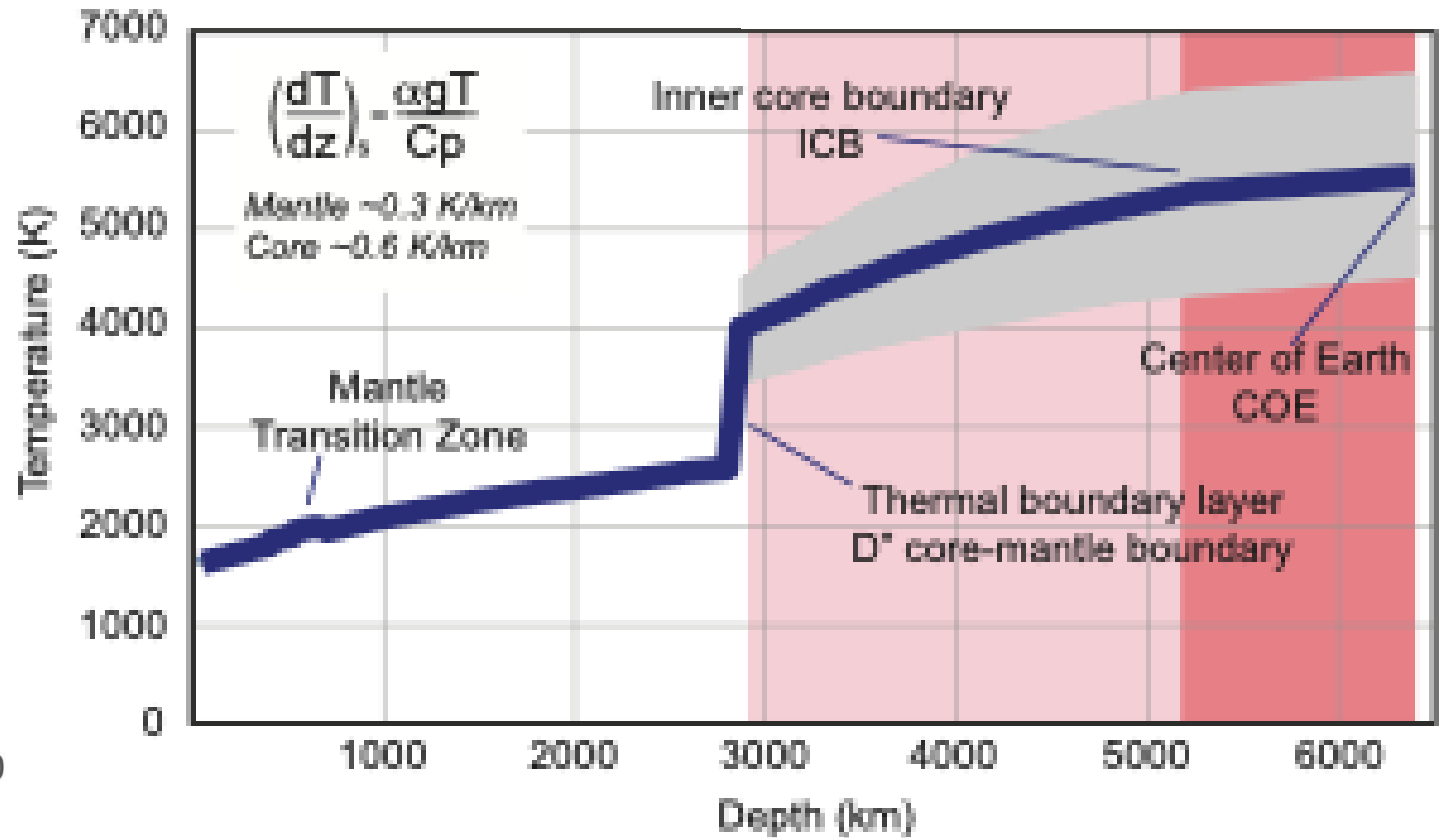
Šrámek et al (2013) *EPSL*, 361: 356–366, [10.1016/j.epsl.2012.11.001](https://doi.org/10.1016/j.epsl.2012.11.001)

Heat budget

Neutrino data constrains the sources of radiogenic energy



Can we measure temperature at depth in the Earth?

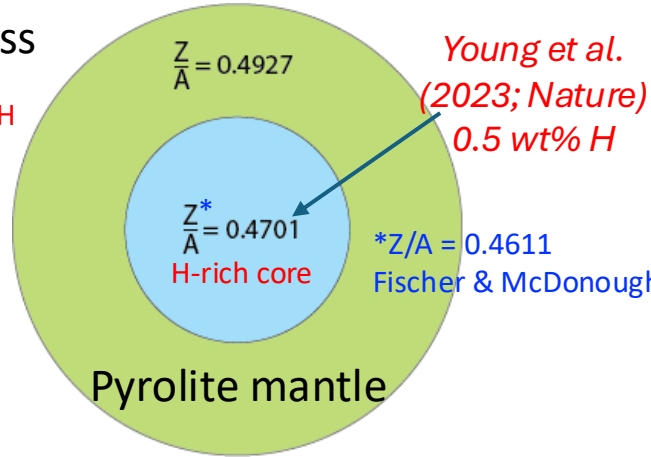
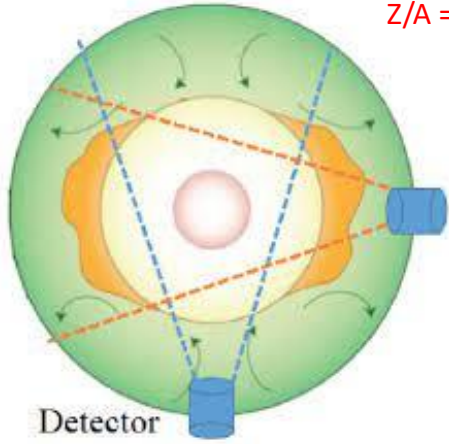


Electron density:

testing the H content of the Earth

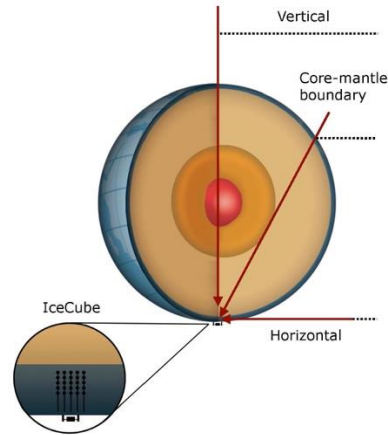
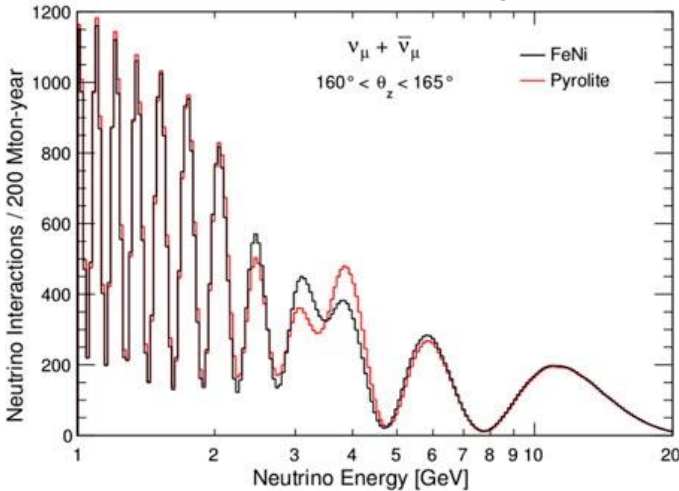
Z = proton#, A = atomic mass

Z/A = 1 for H
Z/A = 0.5



Neutrino oscillation studies

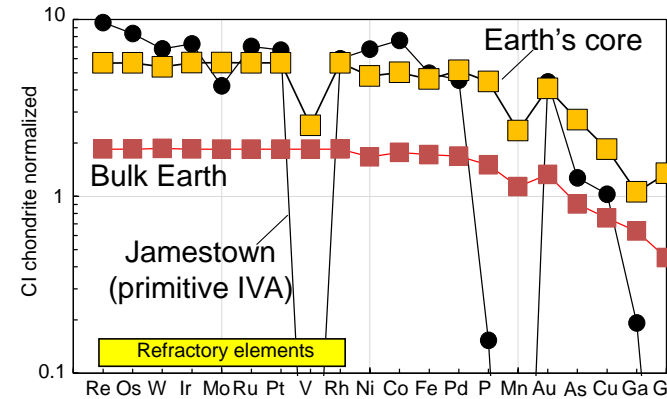
B 2-8 GeV oscillation spectrum



Earth's core

- Radius: 3483 ± 5 km
- Inner core radius: 1220 ± 10 km
- Mass: 1.93×10^{24} kg
- CMB heat flux $60-110$ mW/m²
- CMB heat flux 13 ± 3 TW
- Ellipticity @ CMB 2.5×10^{-3}
- Core surface topography < 3 km

Fischer & McDonough, 2025



	* wt%	at %
Fe	85	80
O	1.0	3.3
Si	3.5	6.5
S	3.3	5.5
Ni	5.2	4.6
Co, Cr, P...	1.5	0.02



The Geoneutrino **Surface Flux** Calculator

GEONU is a user-friendly, MATLAB live script for modeling data from geoneutrino experiments; it is used to generate a global prediction for the amount of radioactive power in the mantle.

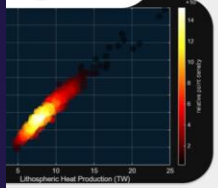
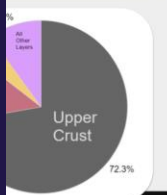
GEONU uses existing global crust models and is equipped with full descriptions of each coding statement. Users may select from a series of predefined inputs, or define their own!

GEONU boasts a flexible experience where non-specialists can learn step-by-step and experts have full access to customize their model!



face

Modeling data from global prediction for the mantle.



Example output figures of contribution from each model and flux vs. heat production (bottom).

<https://github.com/LSKgeo/GEONU>

Conclusions

Neutrino geophysics provide the following insights:

- Define the compositional model of the **bulk Earth** (e.g., U=15 and Th=55 ppb; Ca = 1.63 wt%, Al = 1.55 wt%)
- Constrain Earth's thermal evolution
- Confirm planet's chondritic ratio of refractory elements (e.g., $(\text{Th}/\text{U})_{\text{molar}} = 3.88$) and proportion 2.7* Cl