

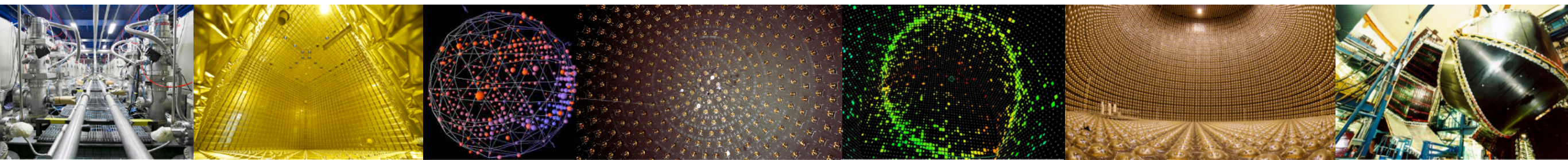
Achilles

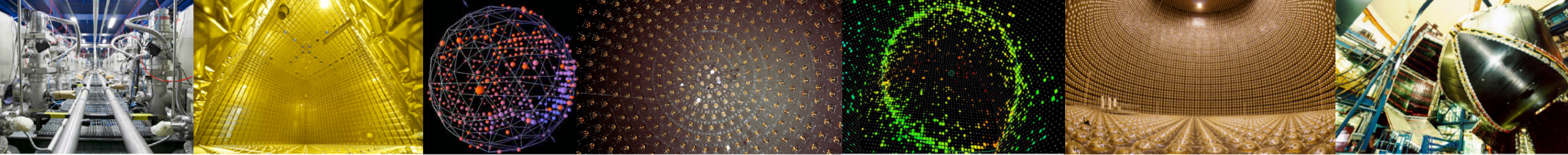
A **CHI**cago**L**and **L**epton **E**vent **S**imulator

William Jay — MIT

with Joshua Isaacson, Alessandro Lovato, Pedro Machado, Noemi Rocco,
and Luke Pickering

HEP Journal Club Seminar
University of Hawaii
3 October 2023





Based largely on:

Isaacson [WJ] et al.

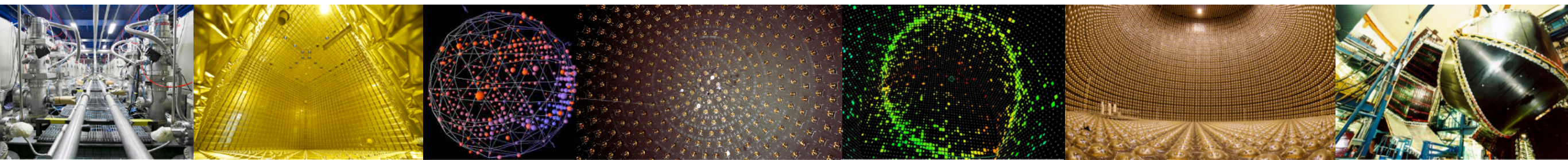
“New approach to intranuclear cascades with quantum Monte Carlo configurations”

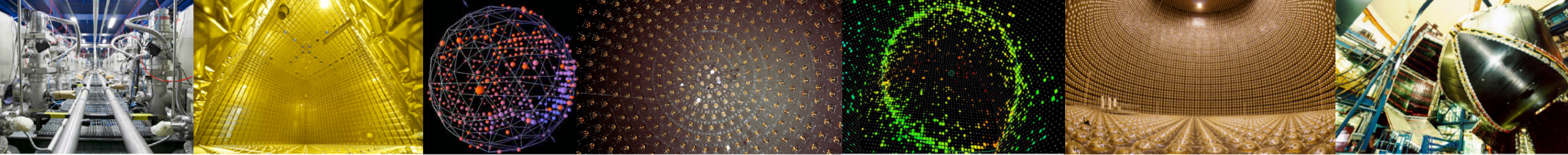
Phys.Rev.C 103 (2021) 1, 015502 [arXiv:2007.15570]

Isaacson [WJ] et al.

“Introducing a novel event generator for electron-nucleus and neutrino-nucleus scattering”

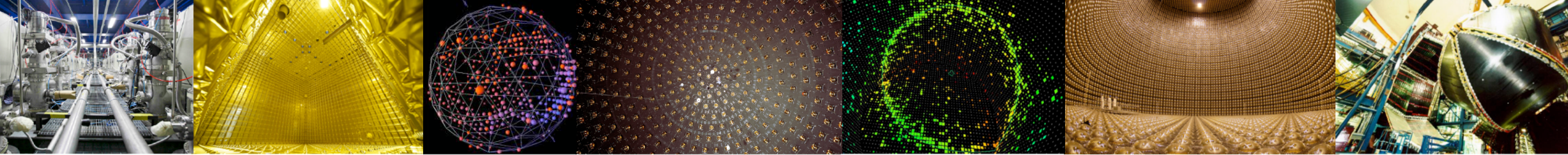
Phys.Rev.D 107 (2023) 3, 033007 [arXiv:2205.06378]



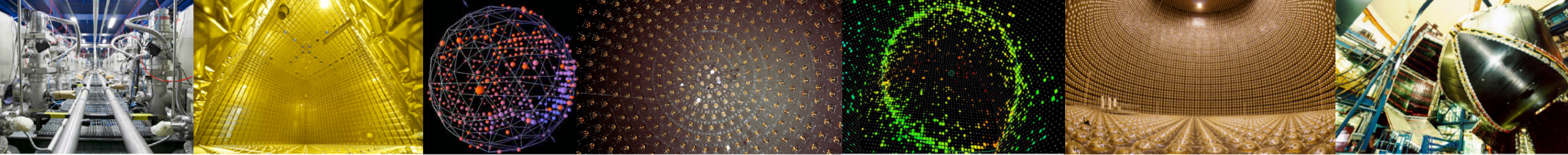


Outline

- Motivation
- Achilles overview
 - Theoretical setup
 - Implementation comments
 - Work in progress
- Recent results

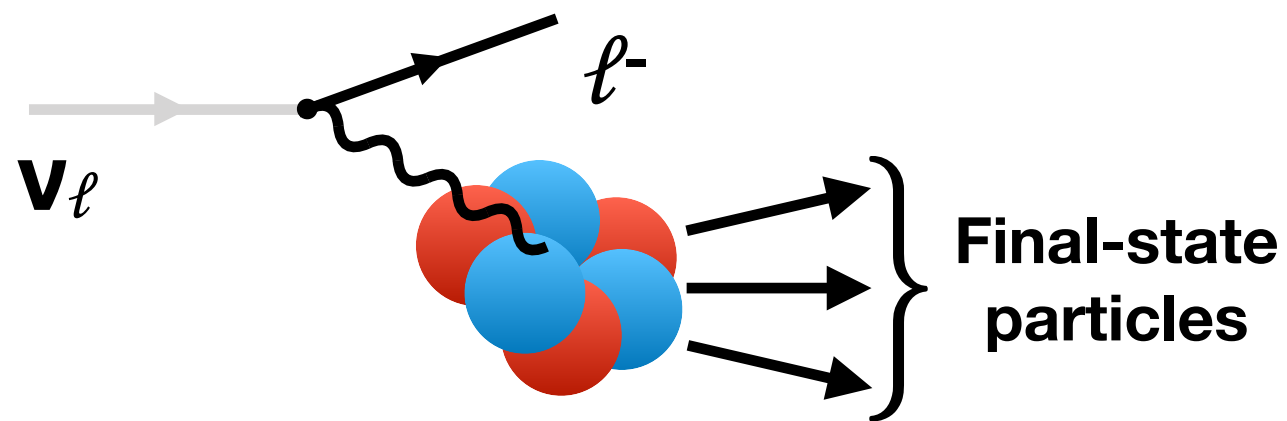


Motivation



The Challenge

Lepton Event Simulation



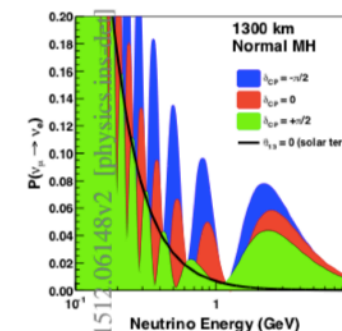
- Neutrino experiments like DUNE and T2HK herald the start of the “precision era” for neutrino experiments
- Percent-level theoretical control of neutrino-nucleus scattering cross sections is needed

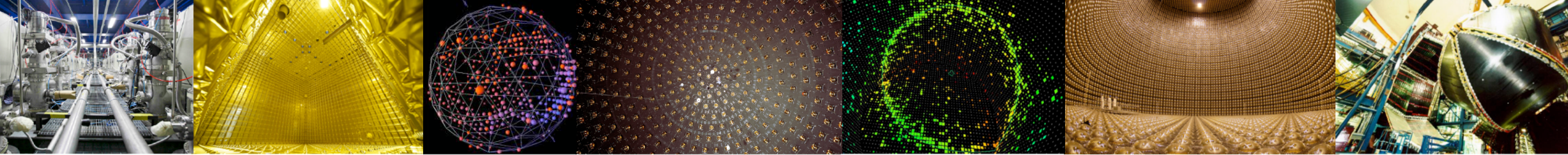
“Uncertainties exceeding 1% for signal and 5% for backgrounds may result in substantial degradation of the sensitivity to CP violation and the mass hierarchy.”

Long-Baseline Neutrino Facility (LBNF) and
Deep Underground Neutrino Experiment (DUNE)

Conceptual Design Report

Volume 2: The Physics Program for DUNE at LBNF





The Challenge

Lepton Event Simulation

Want: Mixing parameters, e.g, angle θ

$$P_{\nu_\mu \rightarrow \nu_e} \approx \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$

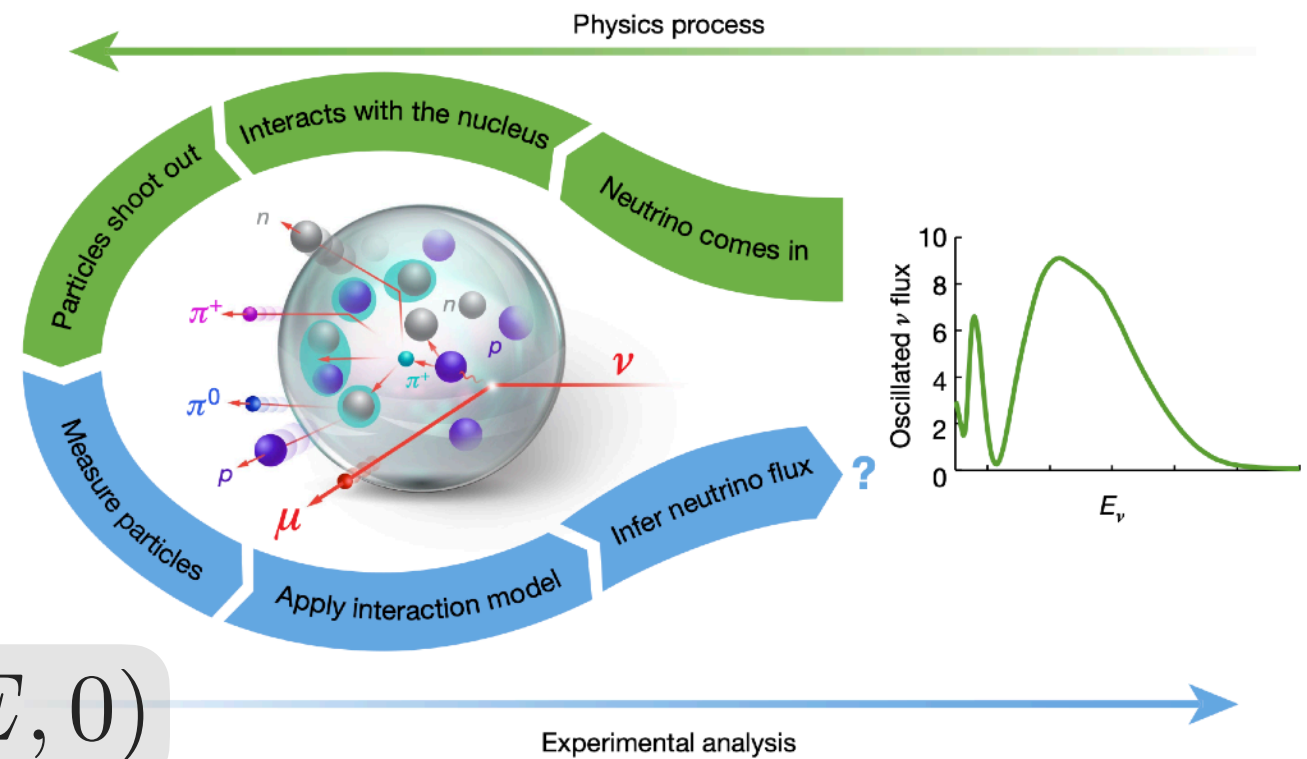
$$\Phi_e(E, L) \propto P_{\nu_\mu \rightarrow \nu_e}(E, L) \Phi_\mu(E, 0)$$

Neutrino fluxes. “Measurable.”

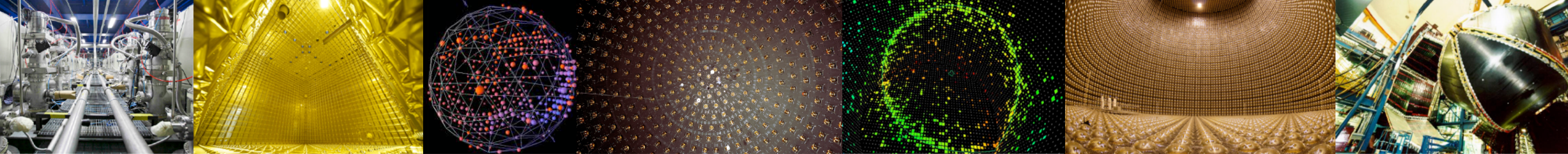
$$N_\alpha(E_{\text{rec}}, L) \propto \int dE \Phi_\alpha(E, L) \sigma(E) f_{\sigma_i}(E, E_{\text{rec}})$$

Event rate

Interaction
cross section

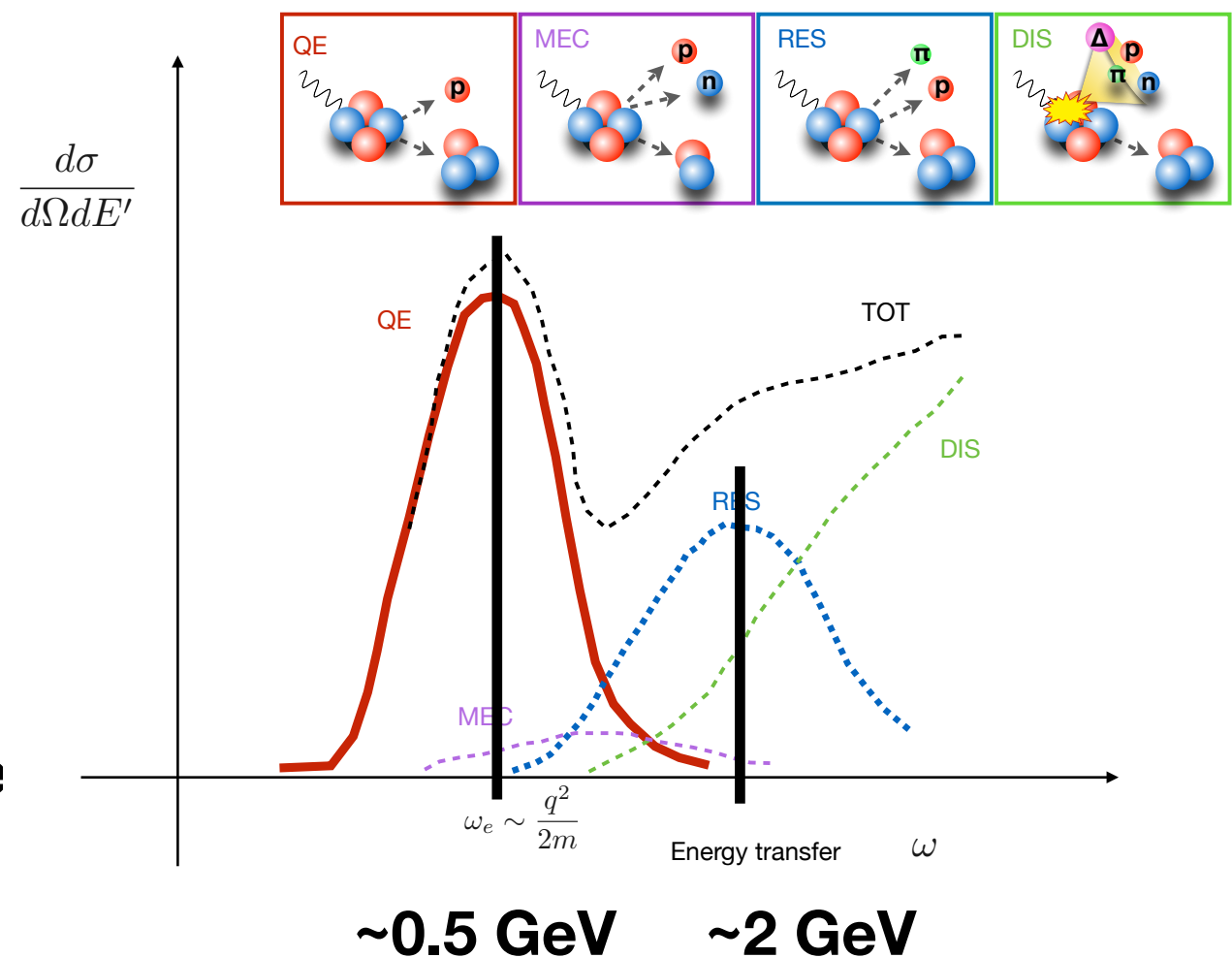
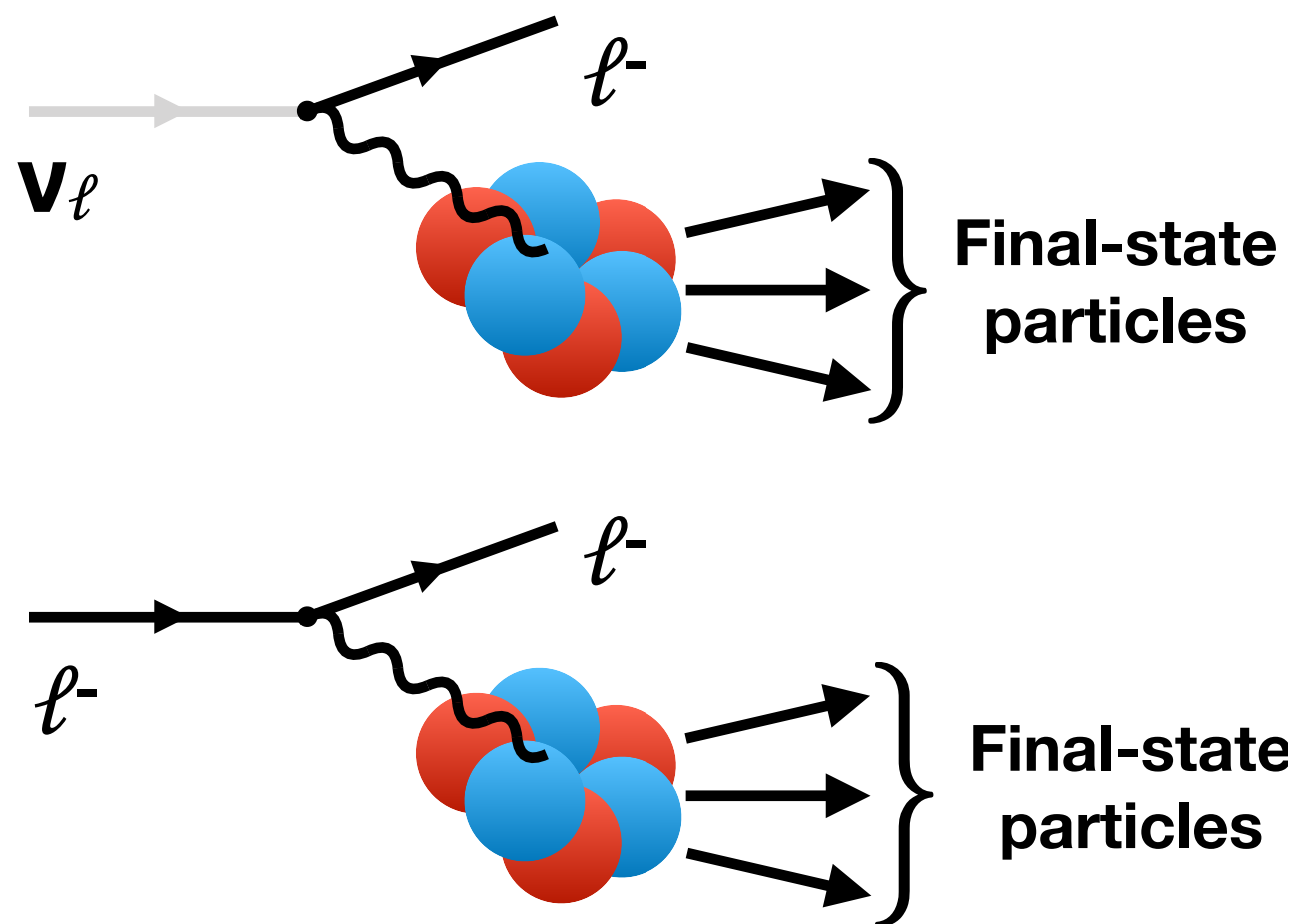


“Smearing matrix”
(Experimental + theoretical)

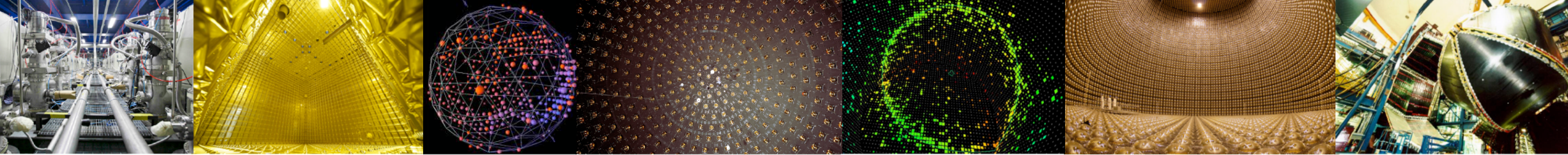


The Challenge

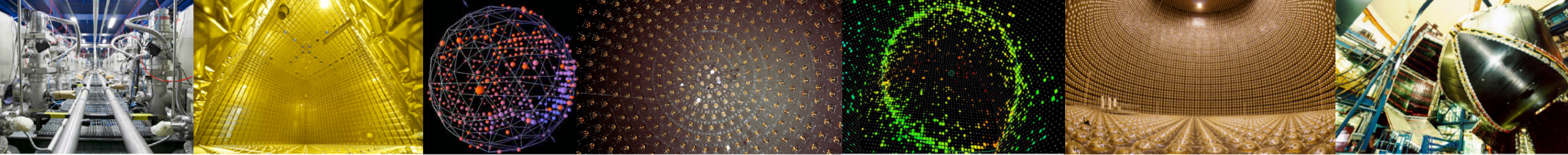
Lepton Event Simulation



Achilles is a **theory-driven event generator** aiming to be responsive to **current and upcoming experimental needs**

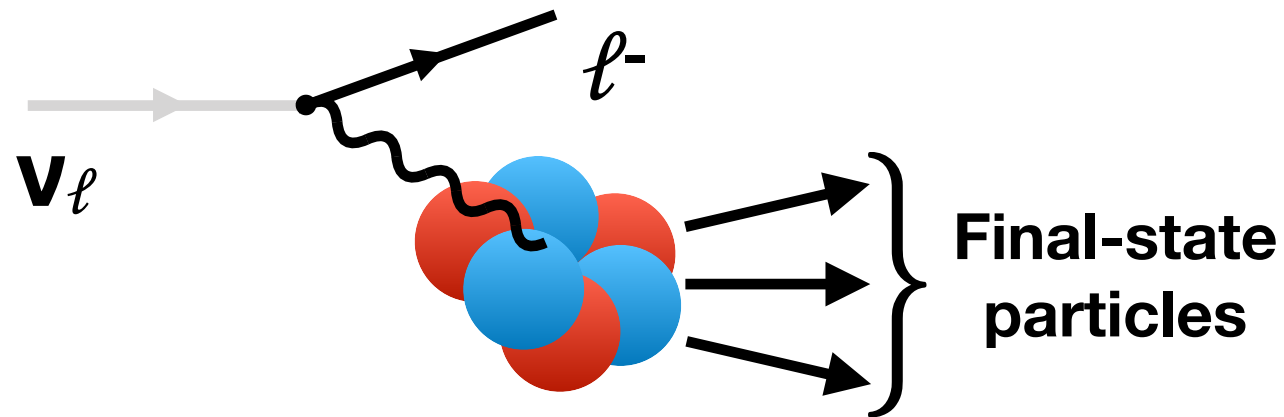


Achilles overview



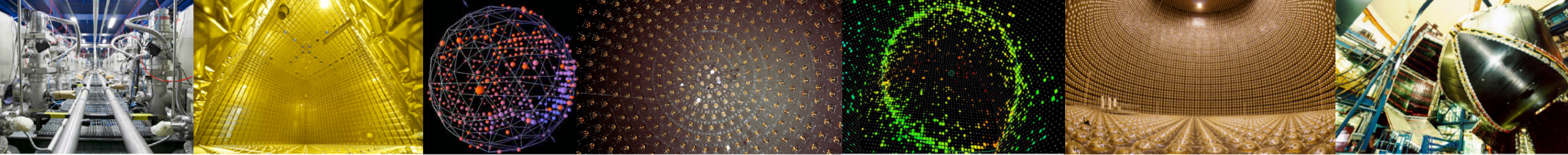
Achilles

Theory-driven: break the problem into well-defined theoretical pieces



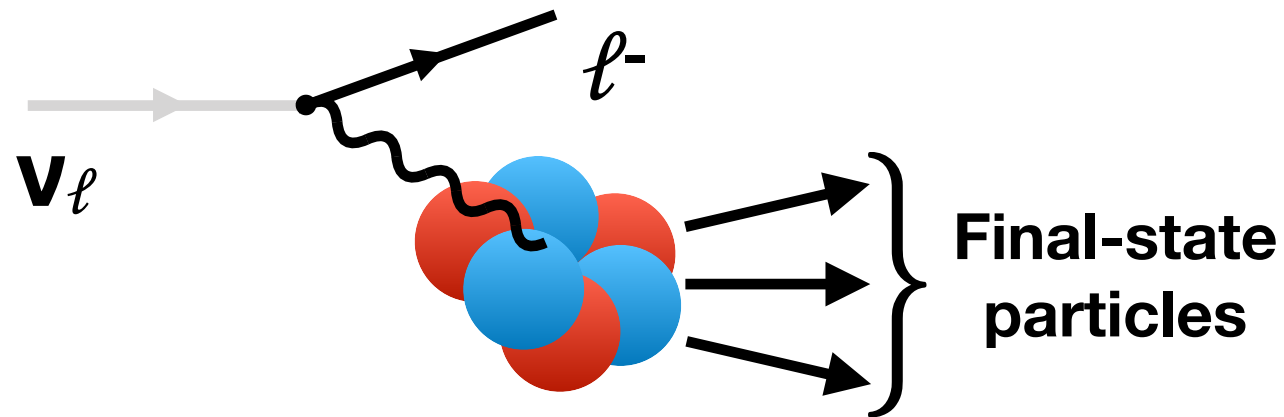
$$d\sigma = \left(\frac{1}{|v_A - v_\ell|} \frac{1}{4E_A^{\text{in}} E_\ell^{\text{in}}} \right) \times |\mathcal{M}|^2 \times \prod_f \frac{d^3 p_f}{(2\pi)^3} (2\pi)^4 \delta^4 \left(k_A + k_\ell - \sum_f p_f \right)$$

$$d\sigma = (\text{flux}) \times (\text{matrix element}) \times (\text{phase space})$$



The Matrix Element

Approx. 1: Single gauge boson exchange



$$|\mathcal{M}|^2 = L_{\mu\nu} \frac{1}{P^2} W^{\mu\nu} \rightarrow \langle \Psi_0 | J_\mu^\dagger(q) | \Psi_f \rangle \langle \Psi_f | J_\nu(q) | \Psi_0 \rangle$$

Leptonic tensor:

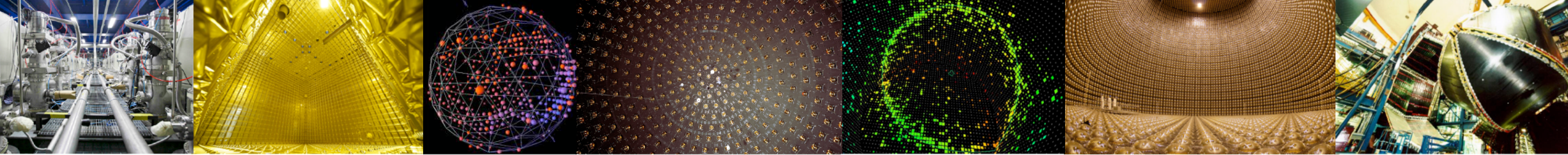
Known analytically in SM or BSM scenario

Hadronic tensor:

Complicated multi-scale object encoding all the hadronic/nuclear physics

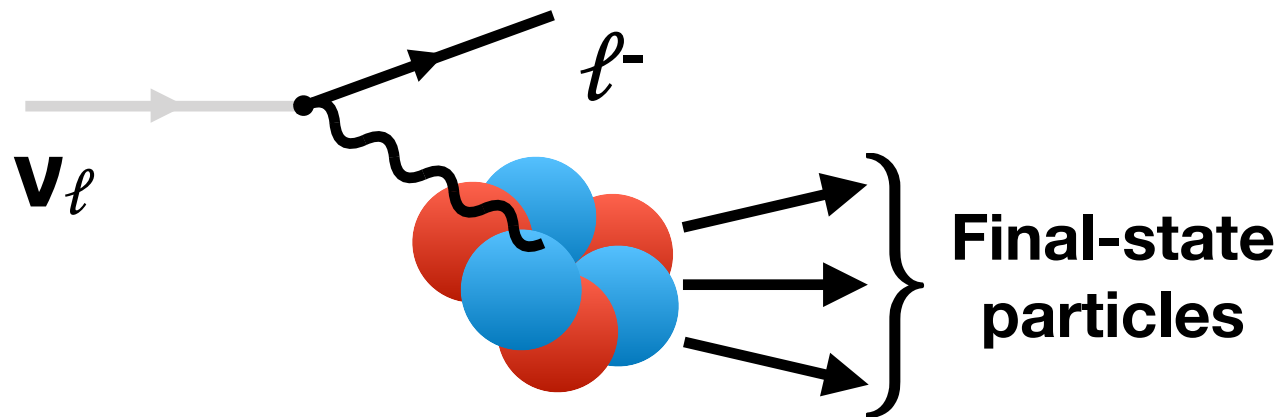
$|\Psi_0\rangle$: Initial state (say, ^{40}Ar or H_2O)

$|\Psi_f\rangle$: Final state (nuclear remnant + outgoing pions, kaons, etc...)



The Matrix Element

Approx. 2: Factorization of primary vertex



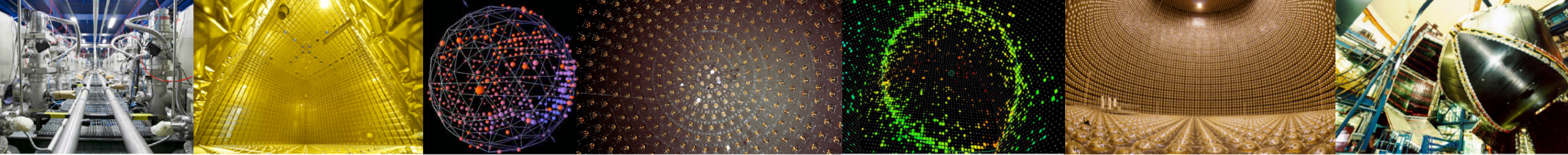
$\mathcal{V}$: Primary-interaction vertex

$\mathcal{P}$: Time evolution to produce observed final states

“Sum coherently over all possible intermediate states p' .”
-Quantum mechanics

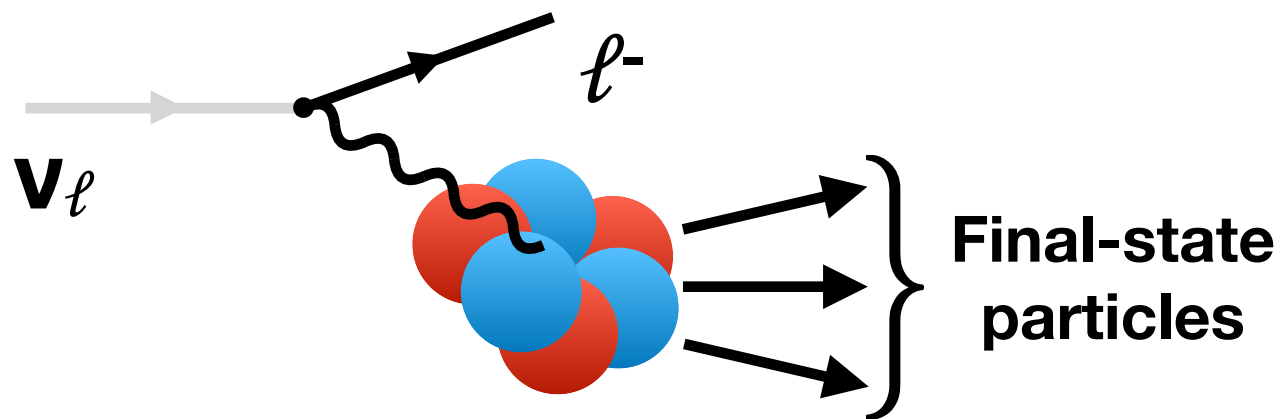
$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 = \left| \sum_{p'} \mathcal{V}(\{k\} \rightarrow \{p'\}) \times \mathcal{P}(\{p'\} \rightarrow \{p\}) \right|^2$$

**This is exact, but exponentially hard.
Factorize the problem.**



The Matrix Element

Approx. 2: Factorization of primary vertex



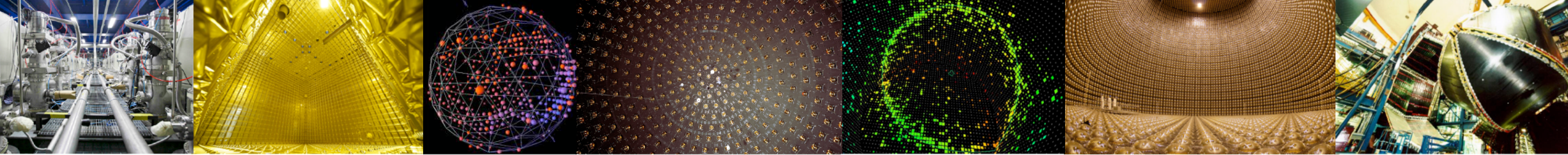
$\mathcal{V}$: Primary-interaction vertex

$\mathcal{P}$: Time evolution to produce observed final states

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

Treat the sum incoherently.
Handle constituents with theoretical care.

(For LHC crowd: similar to dressing hard-scattering cross sections with parton showers)

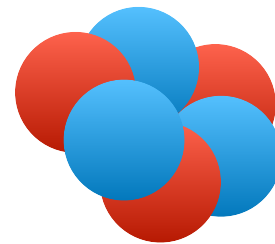


The Primary-interaction vertex

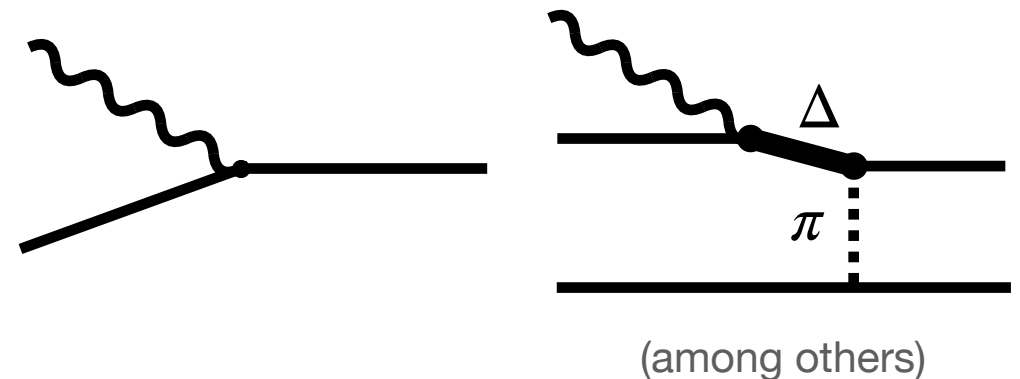
Approx. 3: Choose DOF, Factorization Scheme

- Take nucleons as initial-state DOF
- Take electroweak currents from nuclear EFT:

$$J^\mu(q) = \sum_i j_i^\mu(q) + \sum_{i<j} j_{ij}^\mu(q) + \dots$$



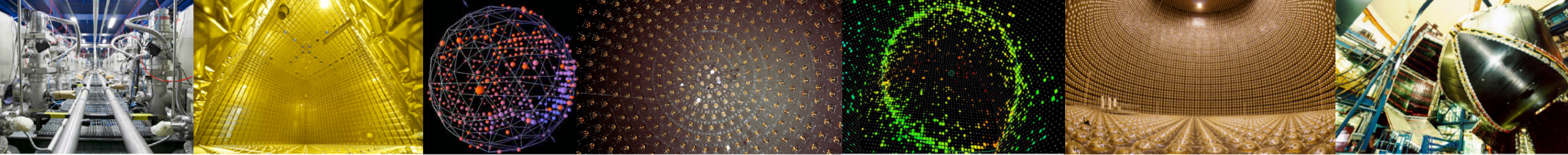
Spatial distribution from nuclear many-body theory: QMC. Quasi-exact.



- Choose a factorization scheme: the *impulse approximation*:

$$|\Psi_f\rangle = |\mathbf{p}\rangle \otimes |\Psi_f^{A-1}\rangle$$

“For momentum transfer $|\mathbf{q}| \gtrsim 400 \text{ MeV}$, external probes resolve individual nucleons.”

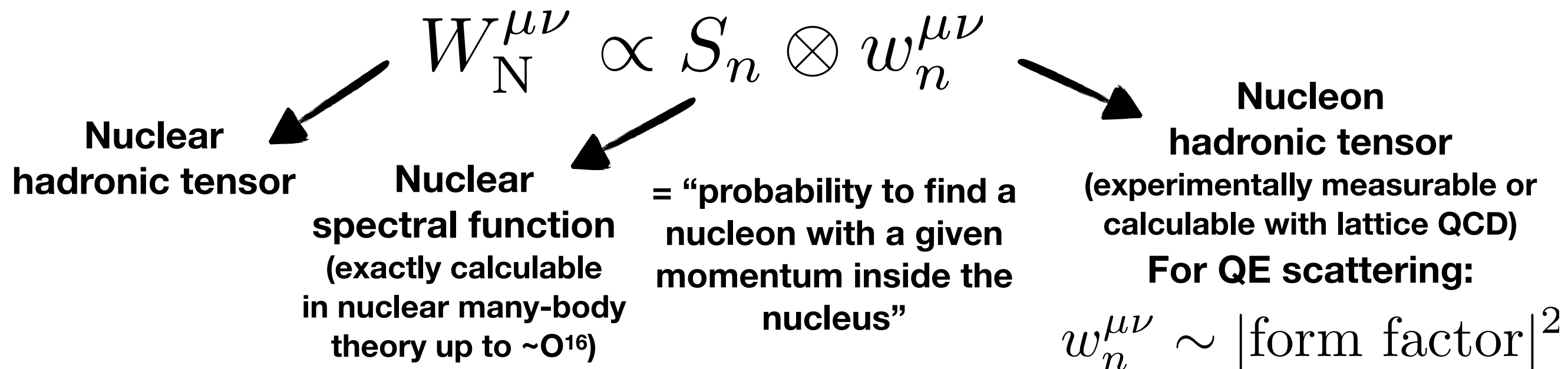


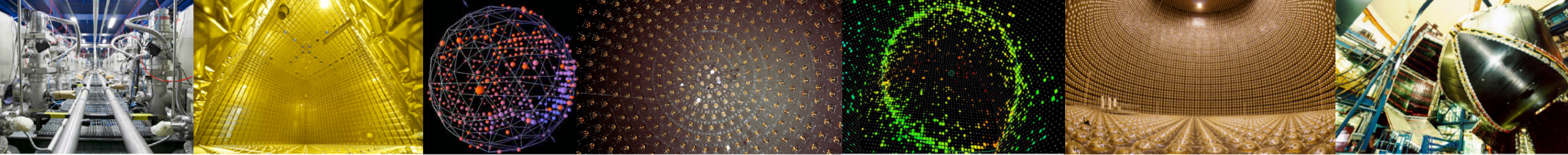
The Primary-interaction vertex

Approx. 3: Choose DOF, Factorization Scheme

$$W_N^{\mu\nu} = \langle \Psi_0 | J^{\mu\dagger}(q) | \Psi_f \rangle \langle \Psi_f | J^\nu(q) | \Psi_0 \rangle$$

With the *impulse approximation* $|\Psi_f\rangle = |\mathbf{p}\rangle \otimes |\Psi_f^{A-1}\rangle$,



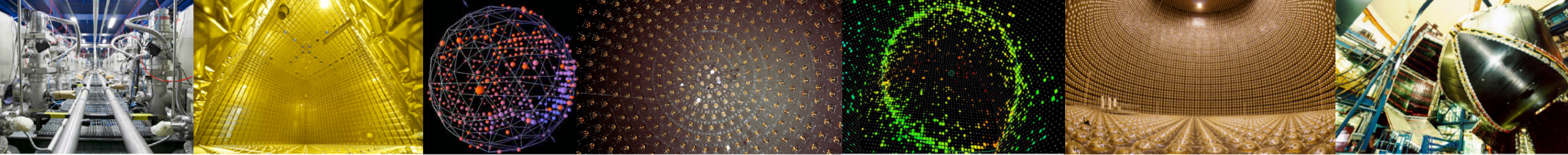


Subsequent time evolution

Approx. 4: Intranuclear cascade

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$





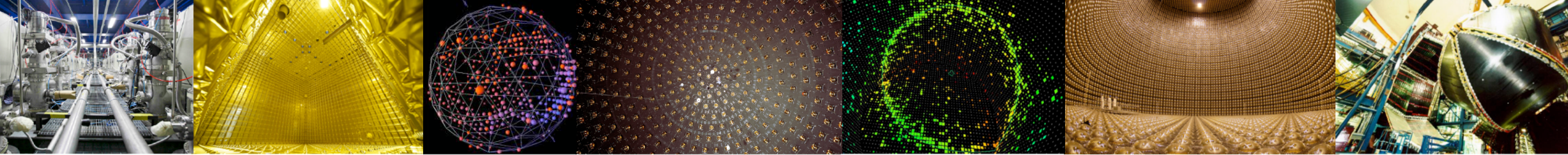
Subsequent time evolution

Approx. 4: Intranuclear cascade

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

- *Intranuclear Cascade (INC)*
 - Scatter nucleons quantum mechanically
 - Propagate nucleons classically, with in-medium corrections

(Neglect interference between successive scattering events in propagation)

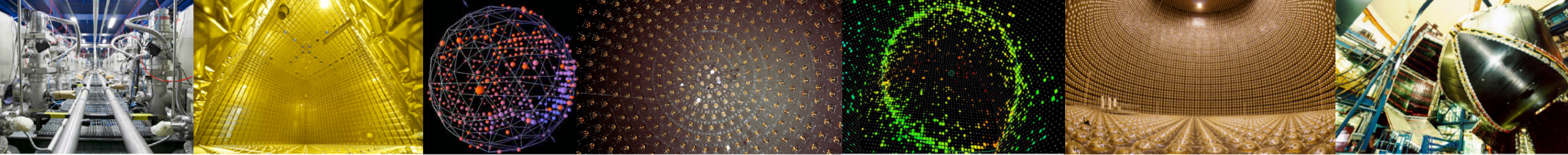


Subsequent time evolution

Approx. 3: Intranuclear cascade

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

- The initial configuration of nucleons is taken from:
 - Spatial distribution: quantum Monte Carlo, retaining correlations
 - Momenta: local Fermi gas model



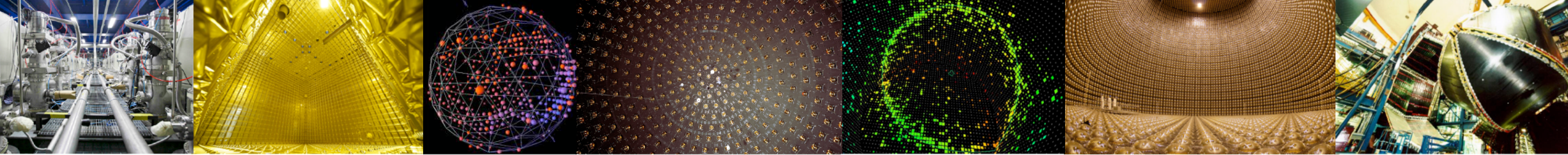
Subsequent time evolution

Approx. 3: Intranuclear cascade

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

The quantum mechanical scattering model:

- Utilizes measured NN cross sections, e.g., from SAID database with GEANT4 or NASA parameterization
- Scatters probabilistically according to the impact parameter: $P(b) = \exp(-\pi b^2/\sigma)$
 - ☑ $\lambda^{-1} = \rho\sigma$ for the mean free path λ
 - ☑ Total probability integrates to the cross section σ
- Incorporates Pauli blocking and formation zone to constrain possible scatterings



Subsequent time evolution

Approx. 3: Intranuclear cascade

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

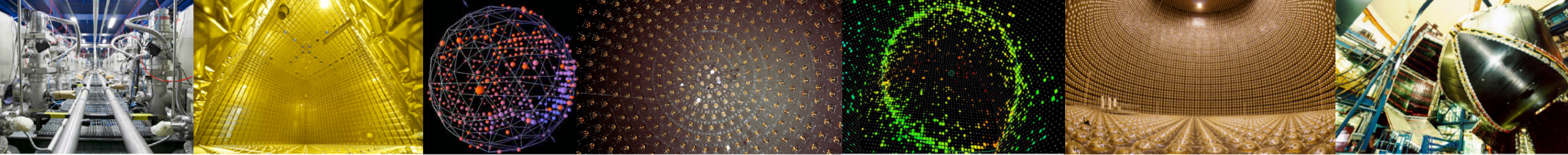
Classical propagation in the background nucleus creates an effective optical potential which induces two effects:

1. Short-distance: $\frac{d\sigma}{d\Omega} \longrightarrow \left(\frac{d\sigma}{d\Omega} \right)_{\text{in medium}}$

(In-medium corrections to NN interactions)

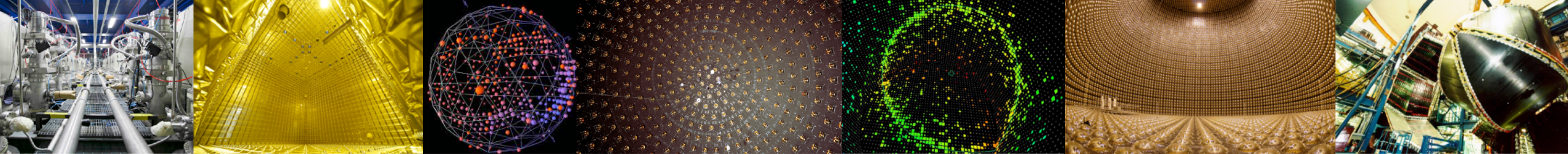
2. Long-distance: $\dot{\mathbf{p}} = -\partial_{\mathbf{q}} H \quad \dot{\mathbf{q}} = +\partial_{\mathbf{p}} H$

(Classical evolution in background potential)



Achilles overview

(A few recent developments)



Isaacson et al.
PRD 105 (2022) 9, 096006
[arXiv:2110.15319]

Achilles — Recent updates

Factorization of leptonic and hadronic tensors

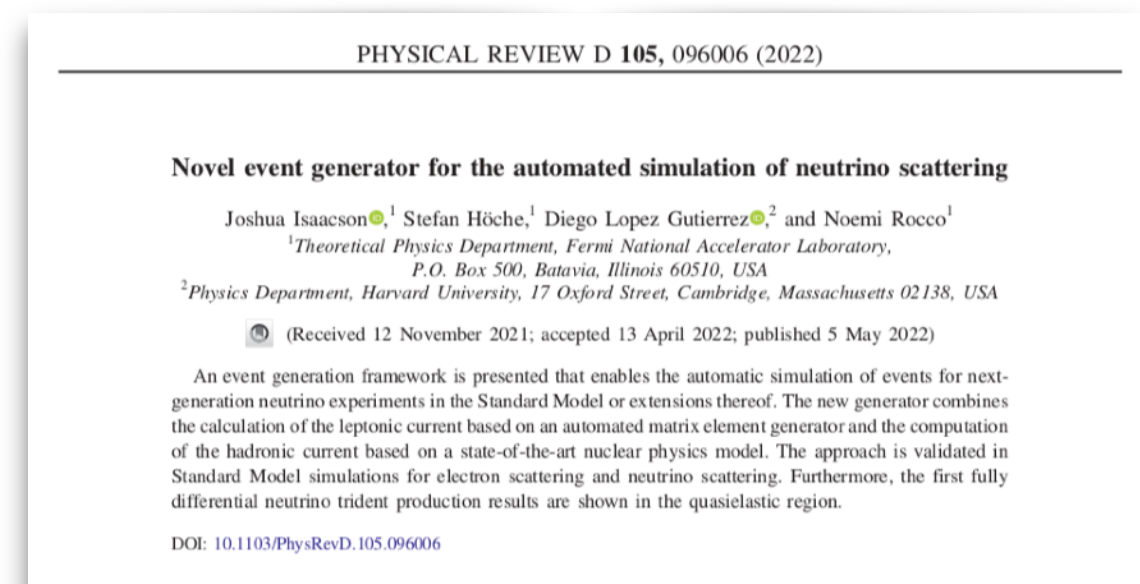
- Automated specification of leptonic tensor (including BSM possibilities)
- Key involvement: Diego Lopez Gutierrez [Undergrad @ Macalester → PhD @ Wash. U. St Louis]
- Uses tools developed by LHC event generation community: Sherpa, Comix, FeynRules, UFO files

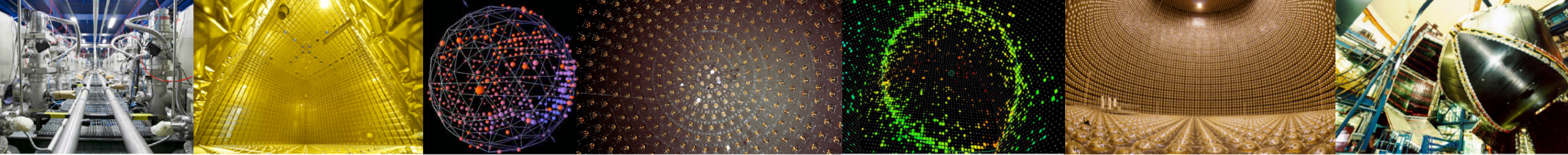
$$|\mathcal{M}|^2 = L_{\mu\nu} W^{\mu\nu} \frac{1}{P^2}$$

Diagram illustrating the factorization of the squared matrix element $|\mathcal{M}|^2$ into a leptonic tensor $L_{\mu\nu}$ and a hadronic tensor $H_{\mu\nu}$.

The leptonic tensor $L_{\mu\nu}$ is associated with the **Calculable QED/EW/BSM physics**, represented by a diagram of a lepton line (electron or muon) interacting via a photon or W/Z boson.

The hadronic tensor $H_{\mu\nu}$ is associated with the **Nuclear/hadronic physics of initial interaction and subsequent evolution**, represented by a diagram of a nucleon (proton or neutron) interacting via a photon or W/Z boson.

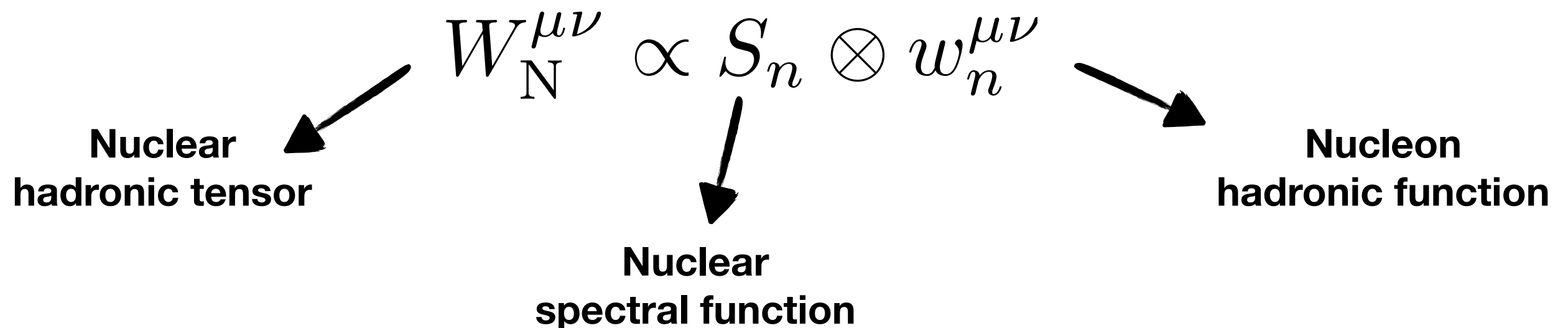


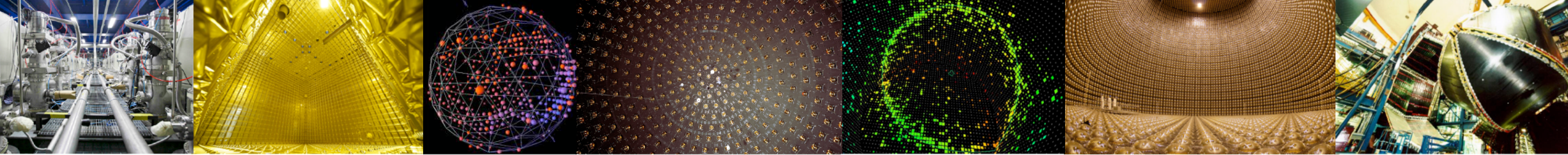


Achilles — Recent updates

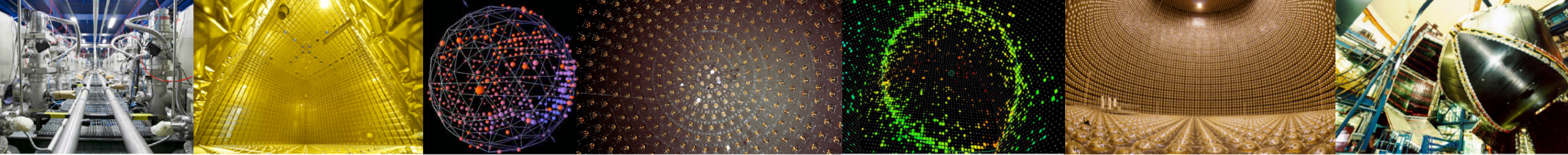
New API for nuclear models

- We have new API/extendible interface for nuclear models
- The API supports models implemented in Fortran or CPP. Extension to models in python is straightforward if there is community interest
- Allows, e.g., for different nuclear spectral functions [Also more general]





Recent results



Achilles: Comparison to experiment

PRD 107 (2023) 3, 033007 [arXiv:2205.06378]

Inclusive e-C
hadronic cross
section

$$\frac{d\sigma}{d\Omega d\omega}$$

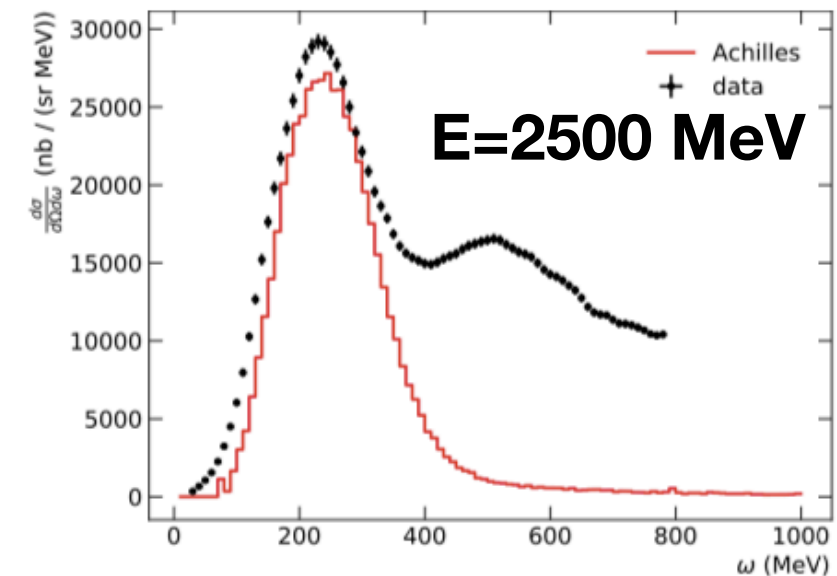
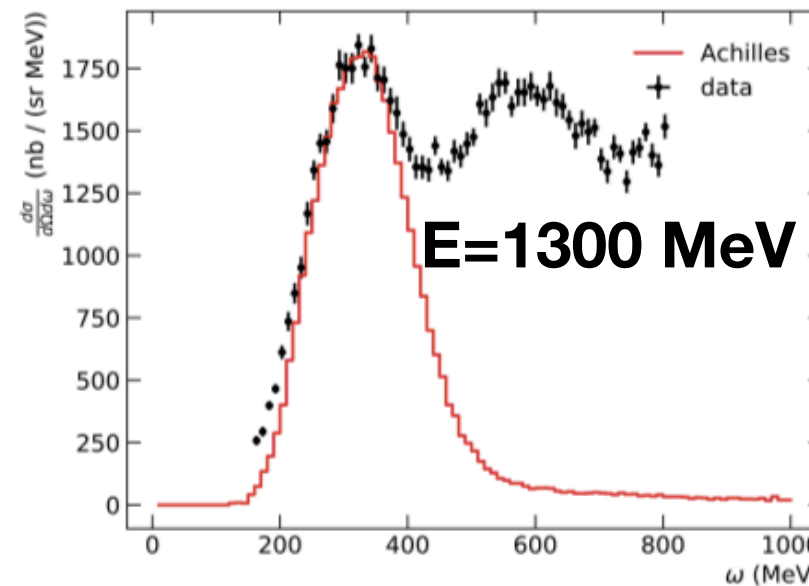
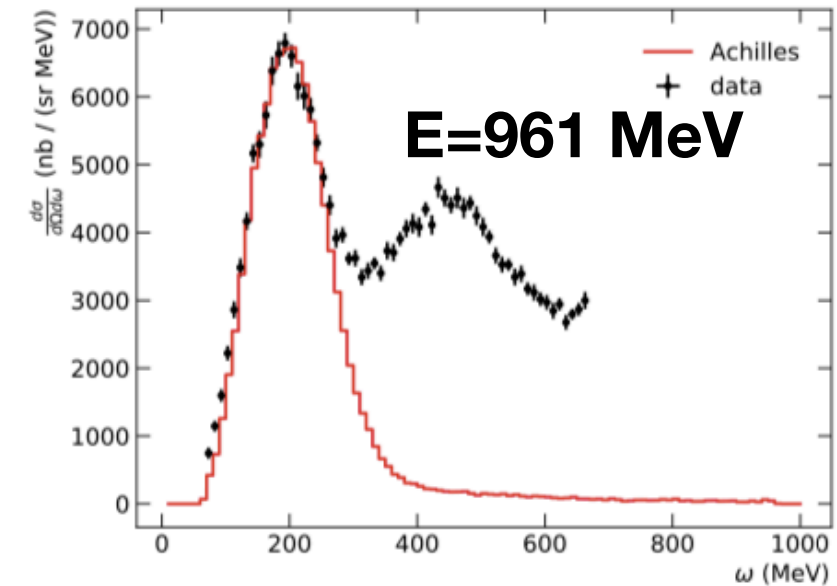
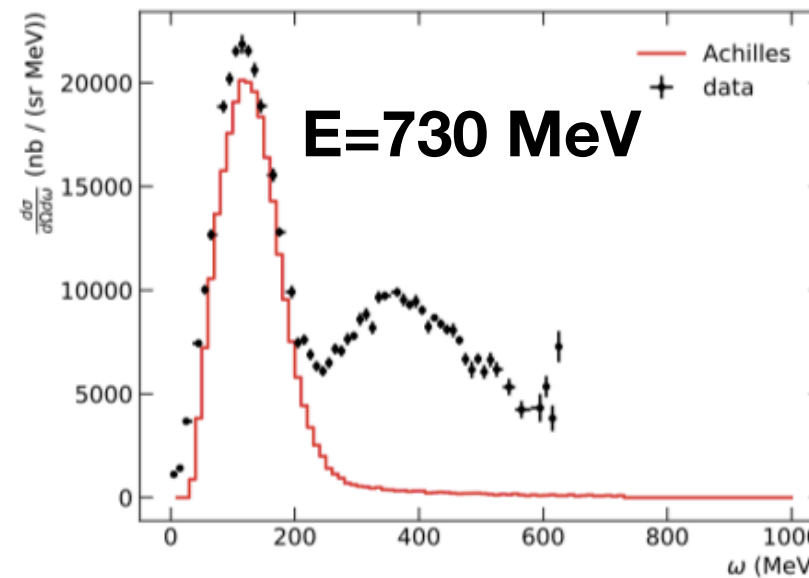
Fixed outgoing
electron angle
 $\theta=37^\circ$ to match
experimental
settings

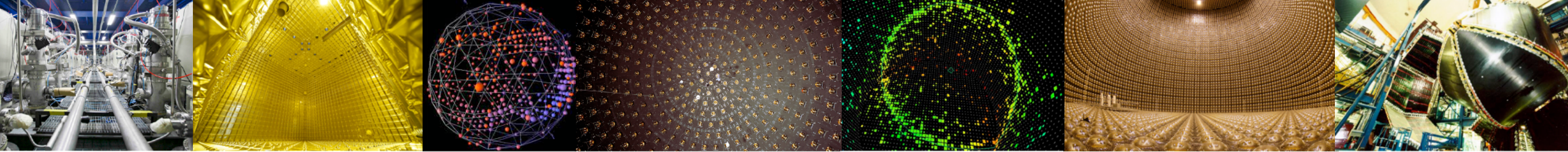
Differential in
outgoing electron
energy ω

Beyond firsts peak: Neglected MEC and resonance contributions

Good agreement = Validation of initial model for QE interaction

J. S. O'Connell *et al.*, *Phys. Rev. C* **35**, 1063 (1987).
R. M. Sealock *et al.*, *Phys. Rev. Lett.* **62**, 1350 (1989).
D. Zeller, Investigation of the structure of the C-12 nucleus
by high-energy electron scattering, Other thesis, Karlsruhe
University, 1973.





Achilles: Comparison to experiment

CLAS and e4v collaborations
Nature 599 (2021) 7886, 565-570

PRD 107 (2023) 3, 033007 [arXiv:2205.06378]

- Inclusive e-C hadronic cross section
- Analysis by e4v to mimic kinematic setup for QE vA scattering

$$E_{QE} = \frac{2m_N\epsilon + 2m_N E_\ell - m_\ell^2}{2(m_N - E_\ell + p_\ell \cos \theta_\ell)}$$

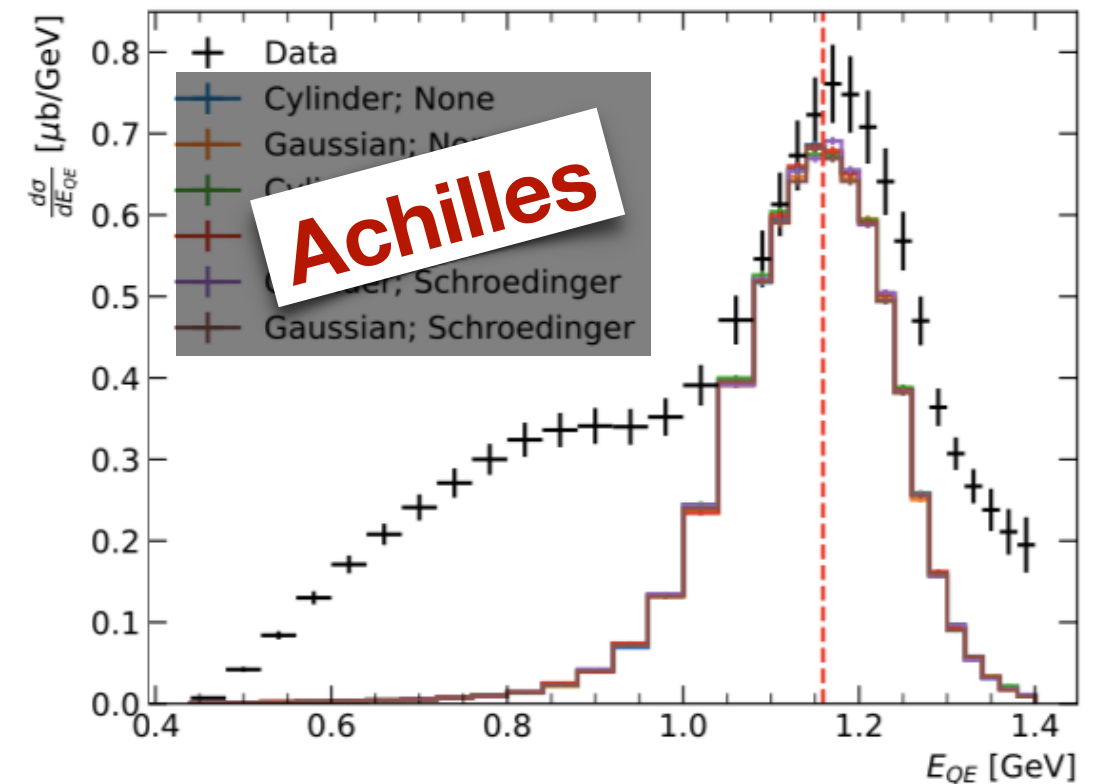
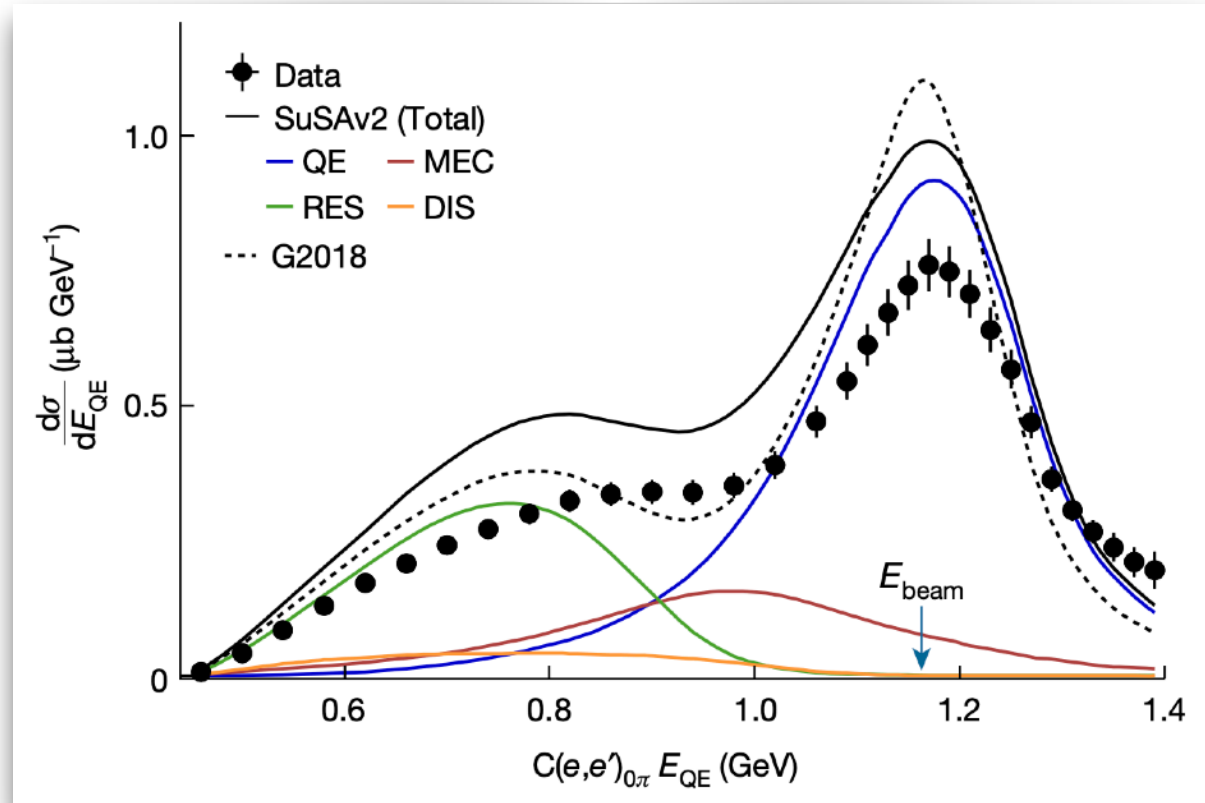
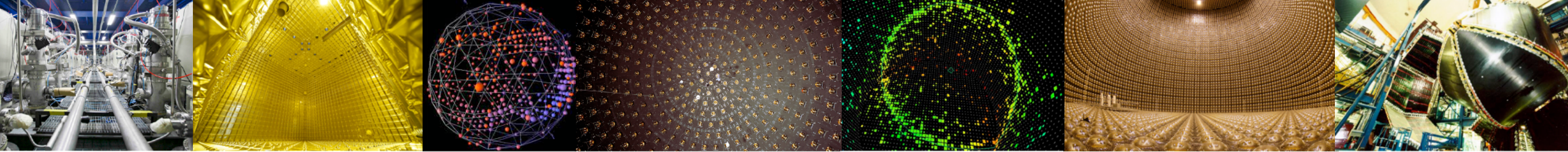


FIG. 4: Comparison of the quasielastic energy reconstructed for an electron beam of 1159 MeV. Data is taken from Ref. [69]. The definition of E_{QE} can be found in Eq. 31. The red dashed vertical line marks the true beam energy.

- Low E_{QE} : MEC and resonance contributions
- High E_{QE} : interference effects (neglected)



Achilles: Comparison to experiment

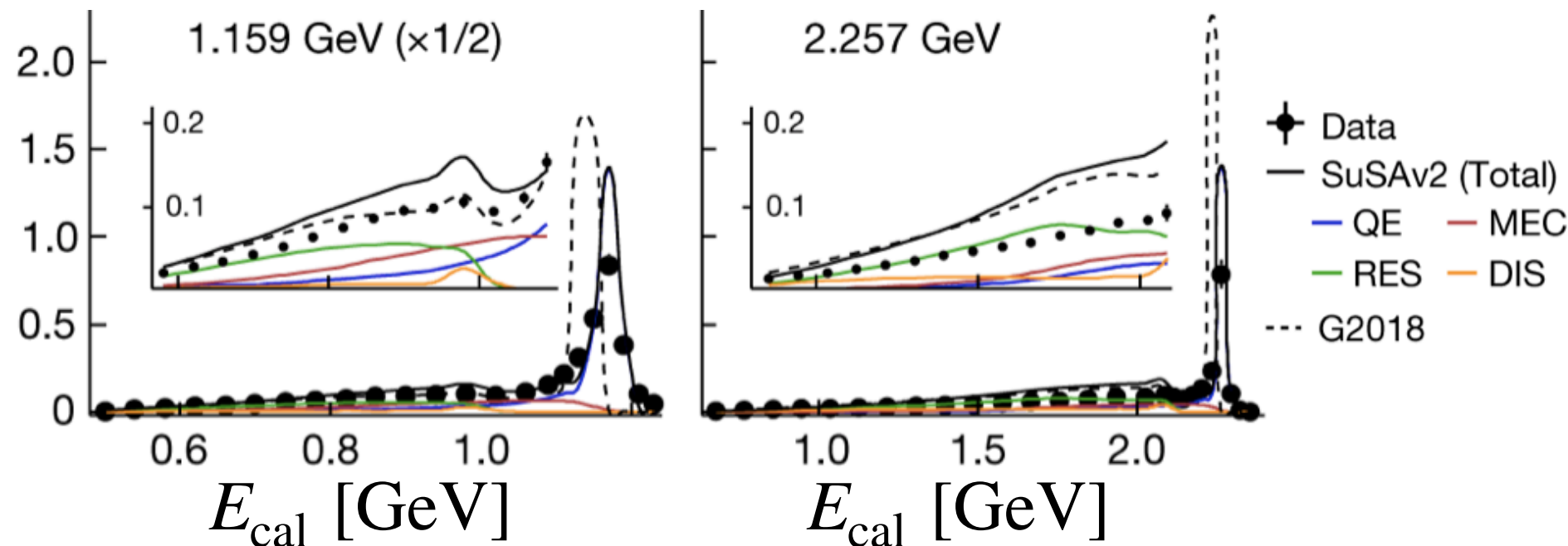
CLAS and e4v collaborations
Nature 599 (2021) 7886, 565-570

PRD 107 (2023) 3, 033007 [arXiv:2205.06378]

E_{cal} = “Calorimetric energy” = “sum of final-state energies”

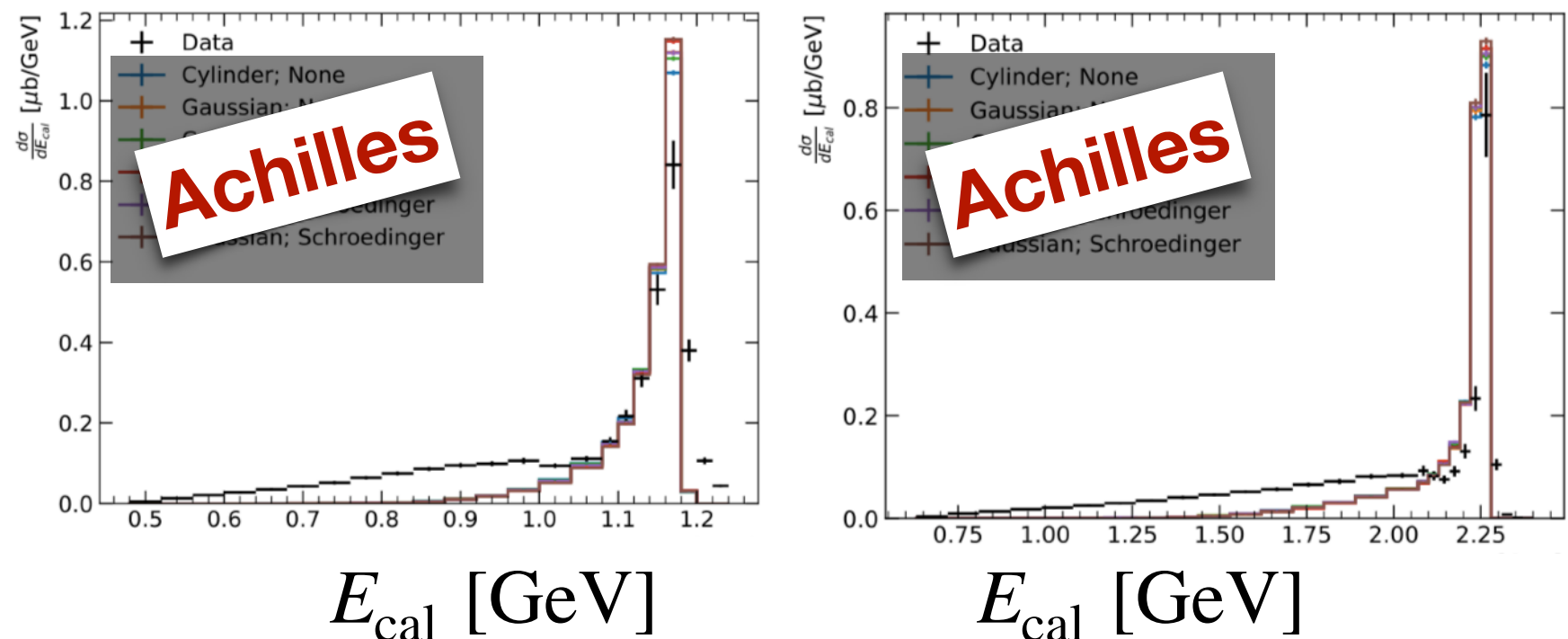
Data + simulation
from e4v paper

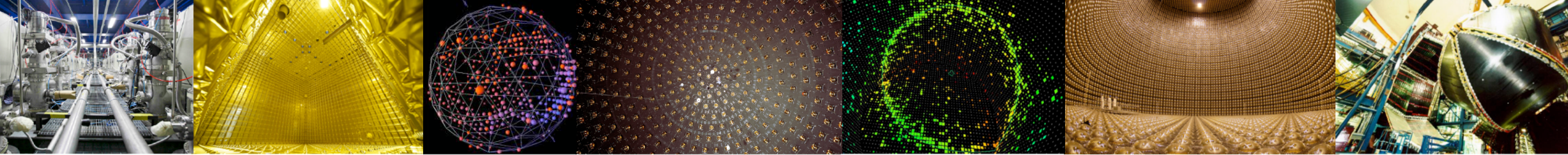
$$\frac{d\sigma}{dE_{\text{cal}}}$$



Same e4v data
vs Achilles

$$\frac{d\sigma}{dE_{\text{cal}}}$$





Achilles: Recent Results

Isaacson et al.
[arXiv:2303.08104]

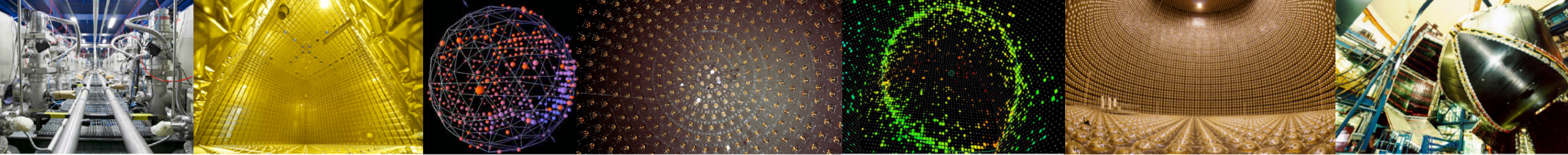
Application: Correlated decays in neutrino experiments

Motivation: ν_τ is perhaps the least understood elementary particle

- DUNE: $O(\text{few hundred})$ ν_τ events per year $\rightarrow$ Accurate theoretical predictions critical
- Outgoing/decaying τ is polarized $\rightarrow$ Induces correlations in final-state particles
- Standard Model predicts:
 - τ polarization perpendicular to the lepton-scattering plane *vanishes*
 - τ polarization components within the lepton-scattering plane do not vanish
- Other generators have often treated ν_τ interactions as for $\nu_e, \nu_\mu \rightarrow$ “outgoing τ as LH only”

Results

- First fully differential predictions for ν_τ scattering at DUNE energies, including all spin correlations and all τ decay channels
- Calculated using generic interface between Achilles and Sherpa
- Correlations between production and decay are *automatically* maintained



Achilles: Recent Results

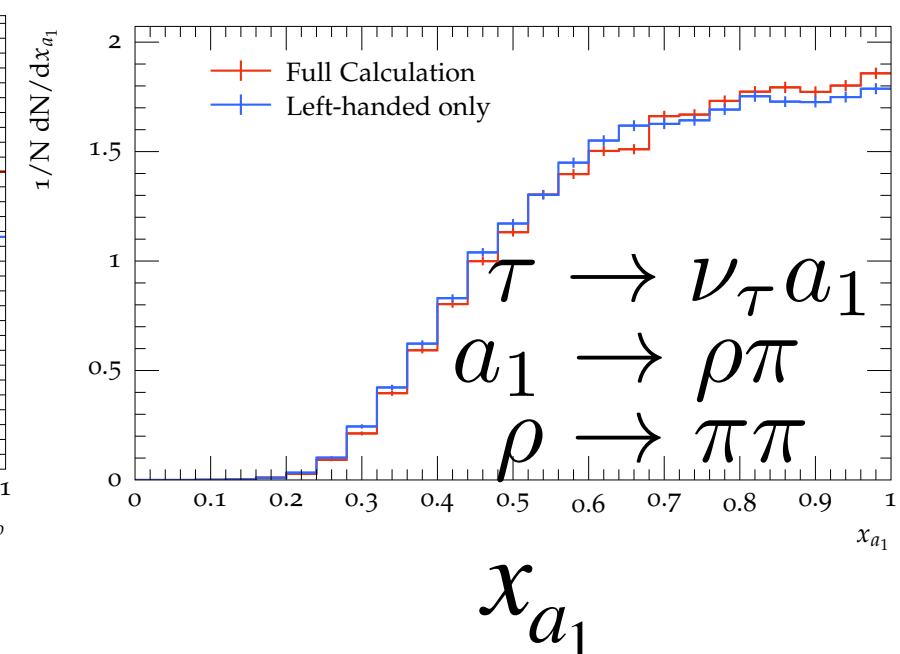
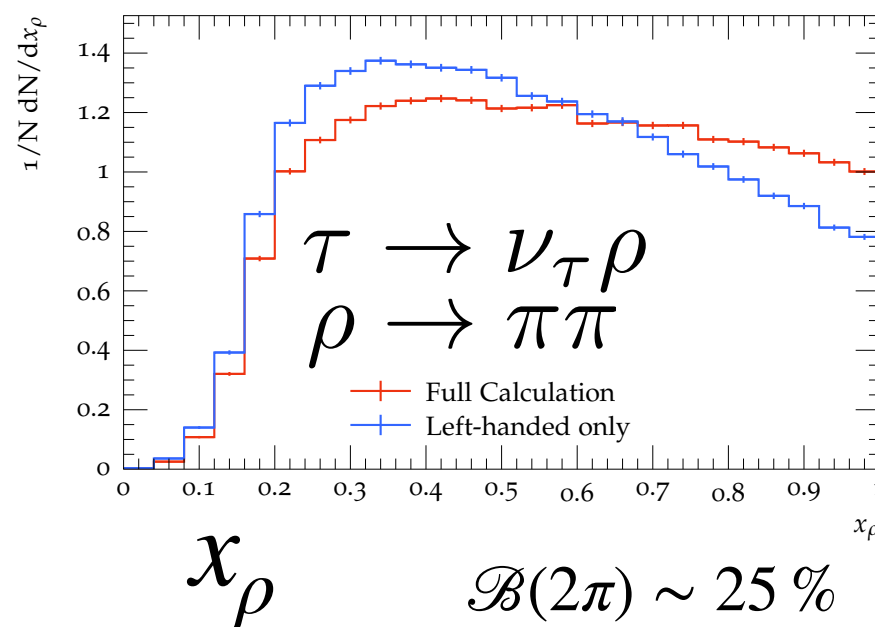
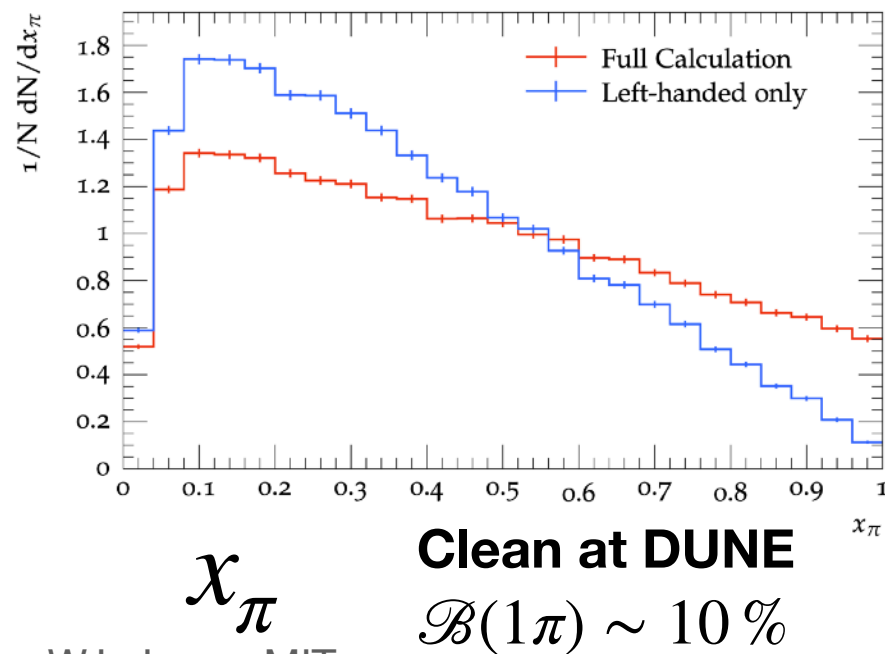
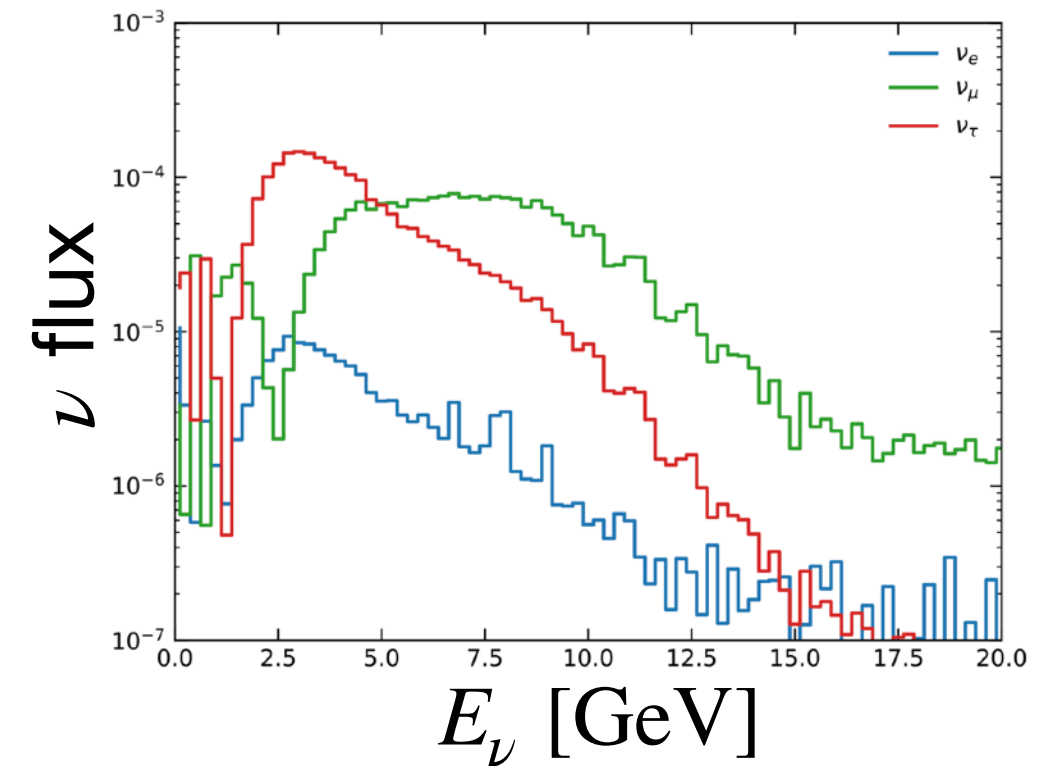
J. Isaacson et al.
[arXiv:2303.08104]

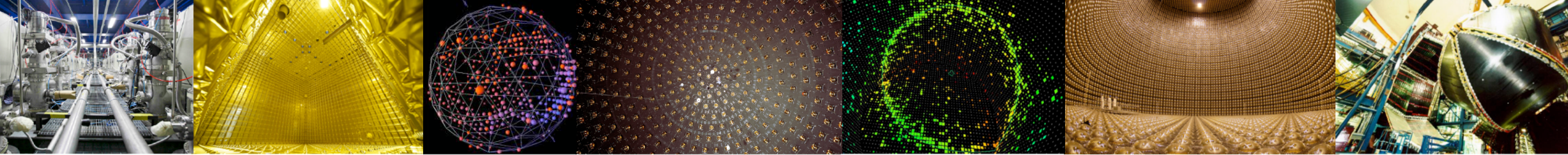
Application: Correlated decays in neutrino experiments

Momentum Fraction Distributions

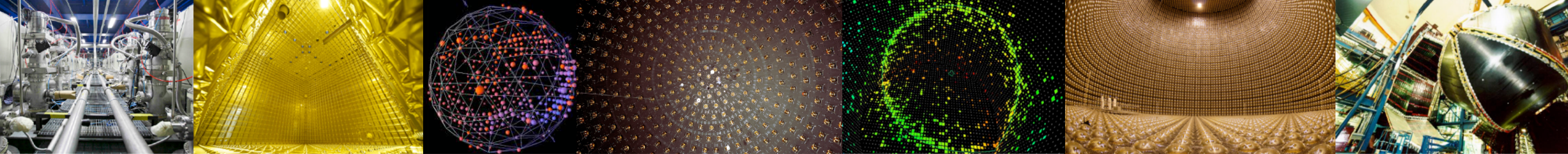
- Benchmarking done against analytic results in collinear ($p_\tau \rightarrow \infty$) limit, monochromatic beams
- Final results calculated using realistic DUNE fluxes

$$\frac{1}{N} \frac{dN}{dx_i} \rightarrow \text{Momentum fraction } x_i = E_i/E_\tau$$





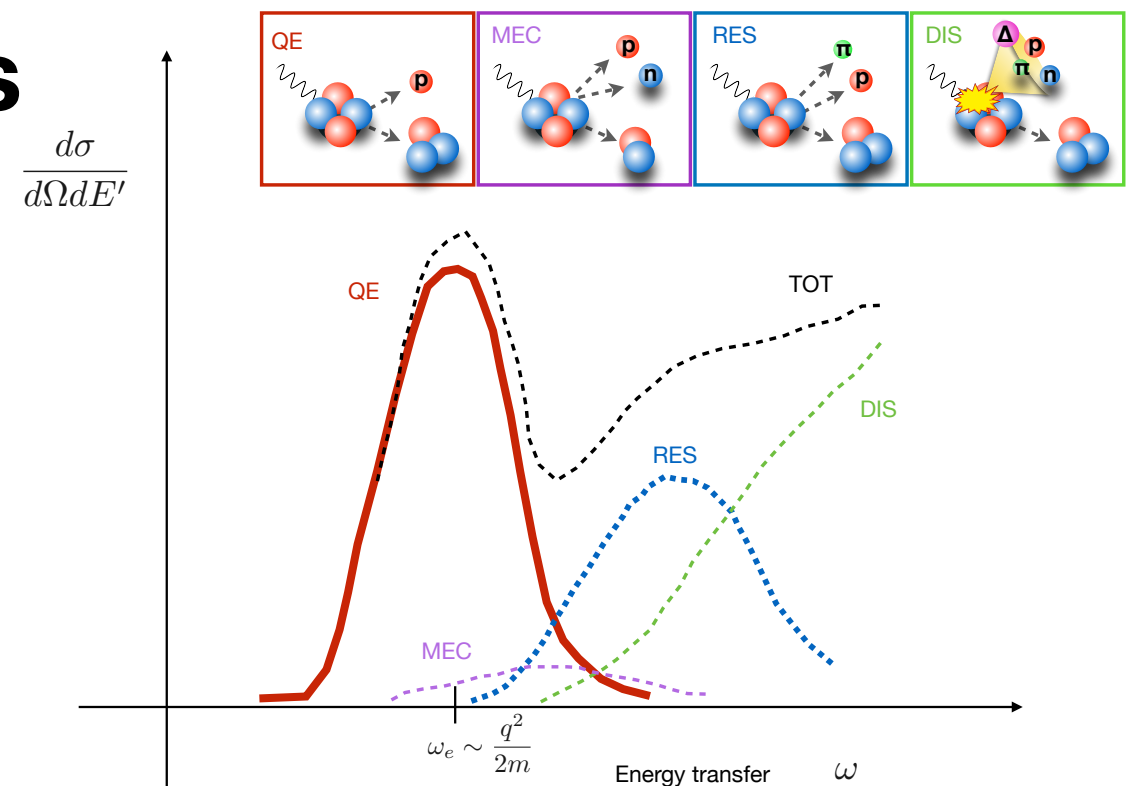
Conclusions



Achilles — What's next?

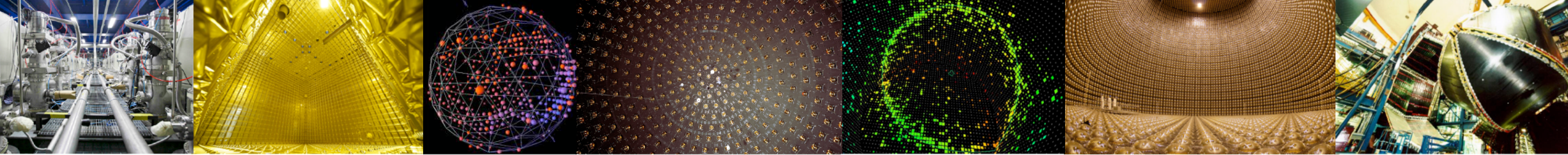
More production processes

- Existing generator: QE scattering only
- Near-term goals: particle production (+decay) at the initial interaction and cascade
- Initial “hard interaction”
 - **Meson-exchange currents** in the spectral function formalism
 - **Resonant scattering** in the dynamical coupled channel formalism
 - Longer term: consistent treatment of DIS



- Cascade
 - **Pion production**
 - **Propagation/decay of Δ**
$$NN \rightarrow N\Delta \rightarrow NN\pi$$

(Can take from data. Lattice calculations will always help.)



Achilles — Summary

- **Our Goal/Credo: Achilles aspires to be a theory-driven event generator, with consistent treatment of known theoretical uncertainties**
- **Observations:**
 - Robustly quantifying systematic errors is generally a tough problem
 - Once chosen, correctly propagating systematics errors is comparatively easy
 - For uncertainties in the “hard interaction” the theoretical uncertainty amounts to an uncertainty in the overall event weight, which is straightforward to propagate
 - Theoretical uncertainties should be incorporated by event generators
- **Achilles employs a modular design to factorize physically different processes:**
 - Leptonic vs hadronic tensors,
 - Nuclear vs hadronic physics
 - “Hard interaction” vs intranuclear cascade
- Achilles currently supports quasi-elastic scattering (e.g., spectral function formalism)
- In the near term ($\approx$ year), we expect to implement MEC and resonant production mechanisms and particle production/decay in the intranuclear cascade