Low energy e+e- cross section study (applications to (g-2), and light hadron spectroscopy)

E. Solodov

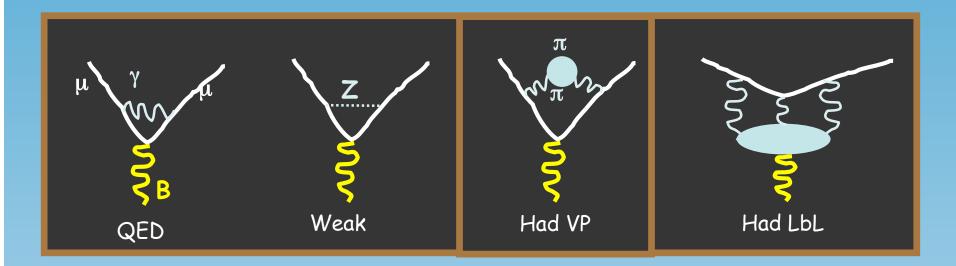
Budker Institure of Nuclear Physics (Novosibirsk, Russia) CMD-2(3) - BaBar

March, 2009

Outline

- 1. Motivation, $(g-2)_{\mu}$, some history
- 2. New results on $e^+e^- \rightarrow \pi^+\pi^-$ (2008, KLOE, BaBar)
- 3. Results on $e^+e^- \rightarrow$ hadrons, BaBar contribution
- 4. VEPP2000 project
- 5. Summary

$a_{\mu} = (g - 2)/2$ is non-zero because of virtual loops, which can be calculated very precisely

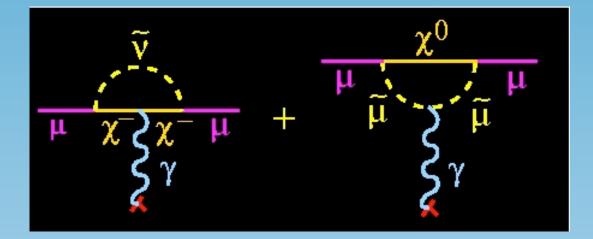


Known well

Theoretical work ongoing

Calculations can be compared with directly measured a_{μ} value performed by BNL E821 with 6.3 10⁻¹⁰ (0.54 ppm) accuracy. The difference indicates new physics.

SUSY: Muon g-2 is very sensitive through loops, which are amplified by tanβ



See full Topical Review: D. Stöckinger J.Phys. G34 (2007) R45-R92

Precise knowledge of a_{μ} will aid in discrimination between a wide variety of standard model extensions

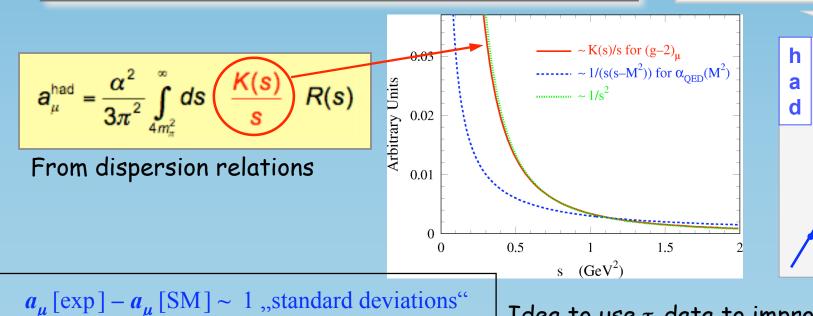
- UED models (1D) typically predict "tiny" effects – Incompatible with a Δa_{μ} of ~ 300 x 10⁻¹¹
- SUSY models there are many predict a_{μ} contributions of about the observed magnitude for Δa_{μ}
- The "Uninvented" perhaps most importantly, sets a stringent experimental constraint for any new models

SM For The Muonic $(g-2)_{\mu}$ (1995)

Contributions to the Standard Model (SM) Prediction:

$$a_{\mu} = \left(\frac{g-2}{2}\right)_{\mu} = \left(a_{\mu}^{QED}\right) + \left(a_{\mu}^{had}\right) + \left(a_{\mu}^{weak}\right)$$

1995 ເ	Source	$\sigma(a_{\mu})$	Reference		
Situation	QED	$\sim 0.3 \times 10^{-10}$	[Schwinger '48 & others]		Dominant uncertainty from lowest order hadronic piece.
The Sit	Hadrons	\sim (15 \oplus 4) × 10 ⁻¹⁰	[Eidelman-Jegerlehner '95 & others]		Cannot be calculated from QCD ("first principles") – but: we can use experiment (!)
	Z, W exchange	$\sim 0.4 \times 10^{-10}$	[Czarnecki et al. '95 & others]		



Idea to use τ -data to improve accuracy

U

had

R, the definition

R(s) is defined as:

$$R(s) = \frac{\sigma^{(0)}(e^+e^- \rightarrow \gamma^* \rightarrow hadrons)}{\sigma^{(0)}(e^+e^- \rightarrow \mu^+\mu^-)}$$

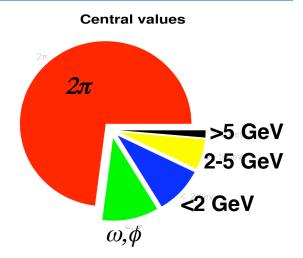
R(s) is one of the most fundamental quantities in high energy physics:

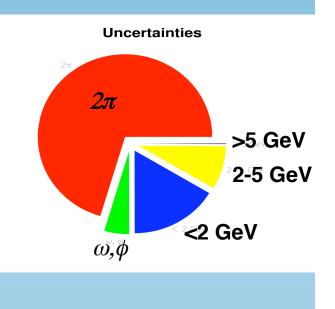
 its global structure reflects number of quarks and their colors; used for QCD tests and as a source of QCD parameters

• plays special role in precision measurements:

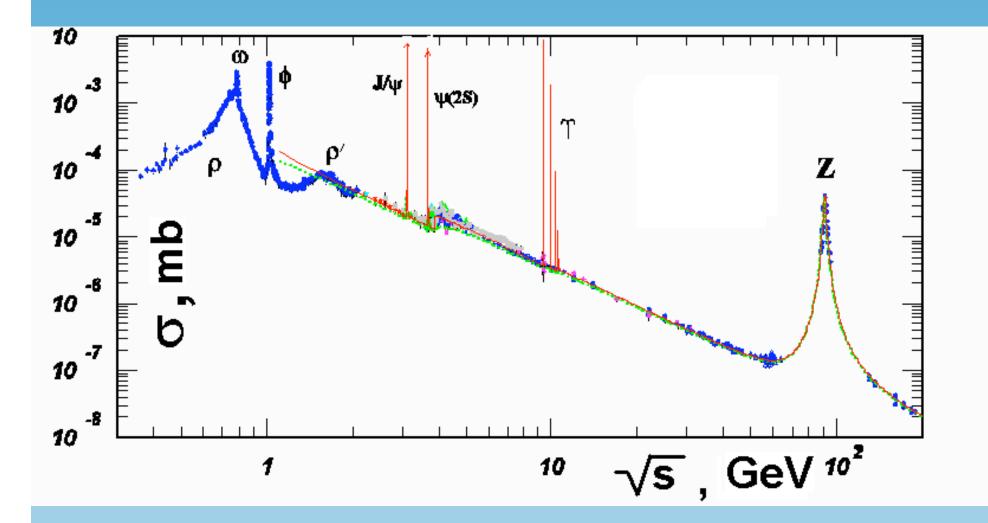
$$\alpha_{\mu}^{had}(l.o.) = \left(\frac{\alpha m_{\mu}}{3\pi}\right)^2 \int_{4m_{\pi}^2}^{\infty} ds \frac{K(s)}{s^2} R(s)$$
$$\Delta \alpha_{had}(M_Z^2) = -\frac{\alpha(0)M_Z^2}{3\pi} \operatorname{Re} \int_{4m_{\pi}^2}^{\infty} ds \frac{R(s)}{s(s-M_Z^2) - i\varepsilon}$$



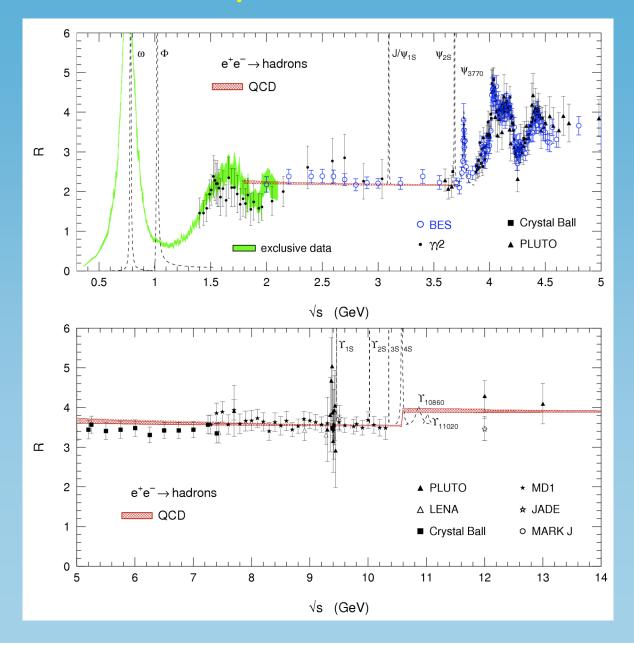




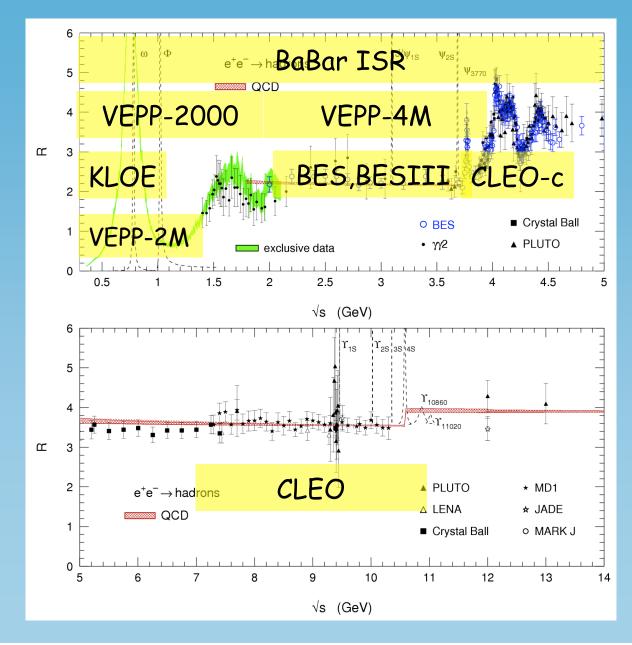
Cross section e⁺e[−] → hadrons



R from experiment and QCD



Current/Future activities in R



New calculations in 2006

New data are available from VEPP-2M - published!

 π + π - from CMD-2

- 96' data 350-520 MeV syst err = 0.7%
- 97' data 1030-1380 MeV 0.6-0.8%
- 98' data 600-980 MeV

 1.2-4.2%
 9 10⁵ evts
- good agreement with published 94-95' CMD-2 data and SND
- more data from CMD-2 and SND for other hadronic channels

multihadron cross sections from BaBar

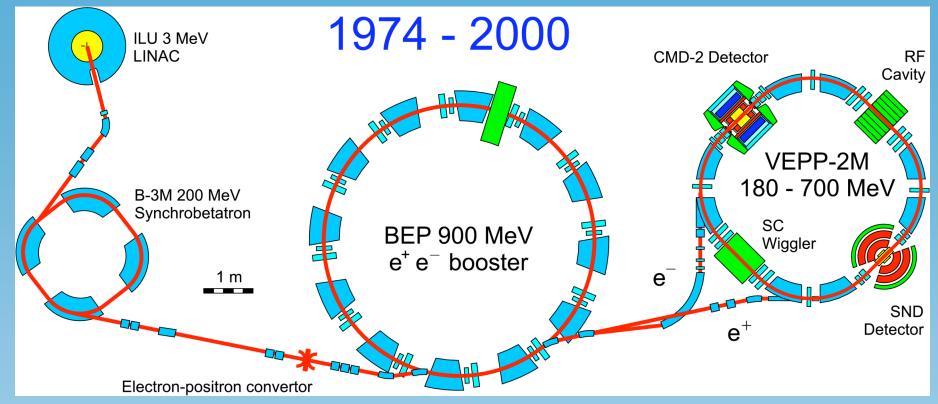
new data significantly improves accuracy of a^{had}

smaller systematic error

consistent treatment of radiative corrections

 \Rightarrow much smaller syst error on rad.corr.

Measurement of R in Novosibirsk

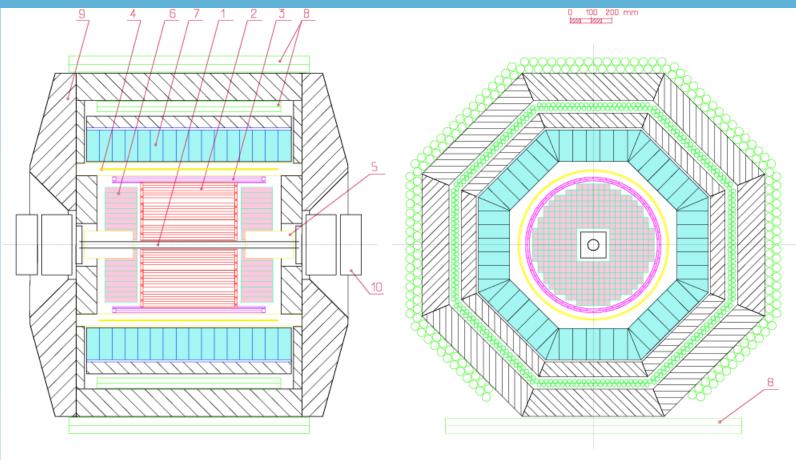


- VEPP-2M collider: 0.36-1.4 GeV in c.m., L≈3•10³⁰ 1/cm²s at 1 GeV
- Detectors CMD-2 and SND: ≈ 60 pb⁻¹ collected in 1993-2000
- All major hadronic modes are measured:

e+e- $\rightarrow 2\pi$, 3π , 4π , KK, .. e+e- $\rightarrow \rho$, ω , ϕ

Still a lot of data to analyze !

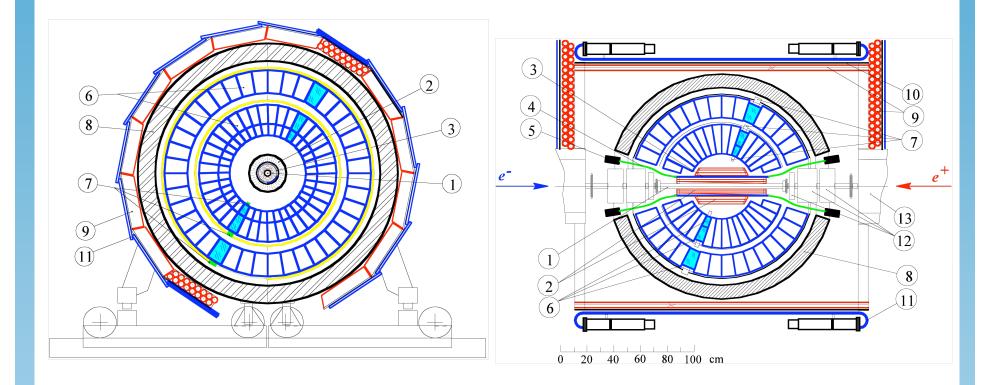




- 1 vacuum chamber
- 2 drift chamber
- 3 Z-chamber
- 4 main solenoid

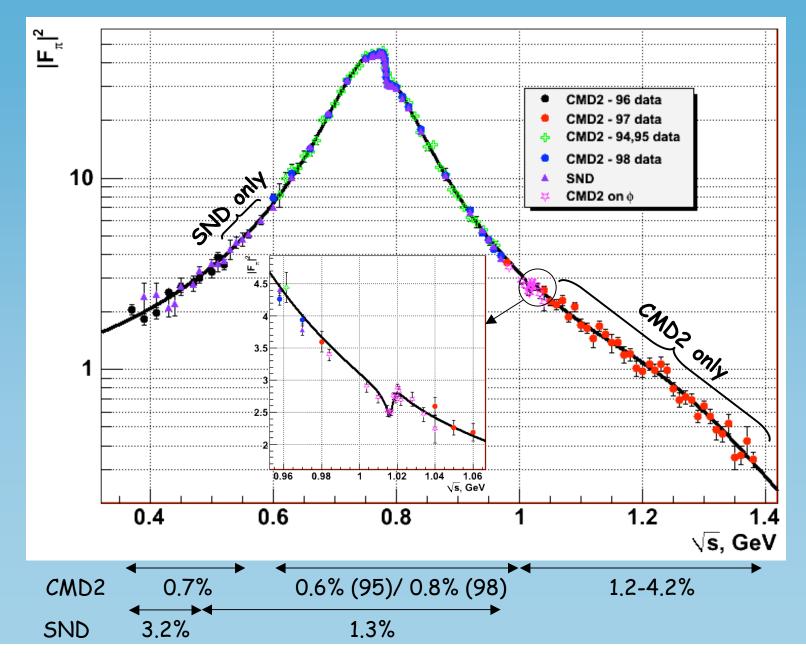
- 5 compensating magnet 6 - **BGO** endcap calorimeter
- 9 iron yoke
- 10 storage ring lenses
- 7 Csl barrel calorimeter
- 8 muon range system

SND detector

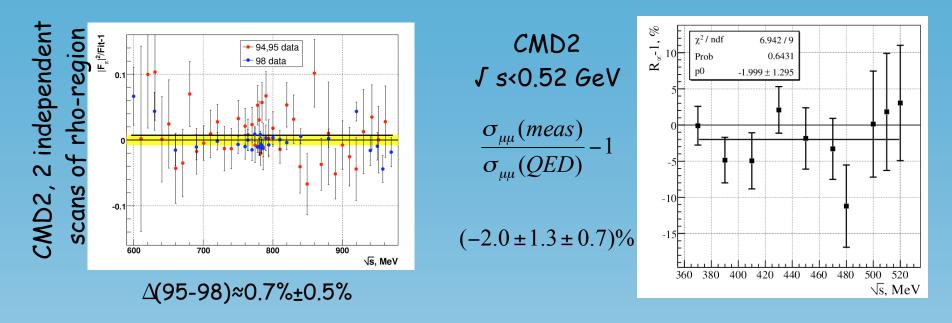


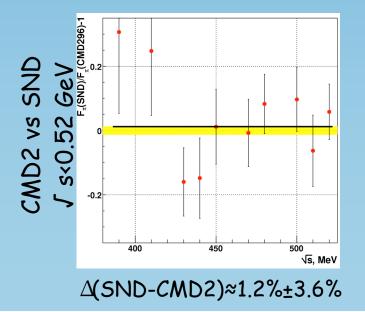
1 - beam pipe, 2 - drift chambers, 3 - coincidence counter, 4 - fibre light guide, 5 - PMTs, 6 - NaI(Tl) crystals, 7 - phototriodes, 8 - iron absorber, 9 - muon tubes, 10 - 1cm iron plate, 11 - muon counters, 12 magnetic lenses, 13 - bending magnets

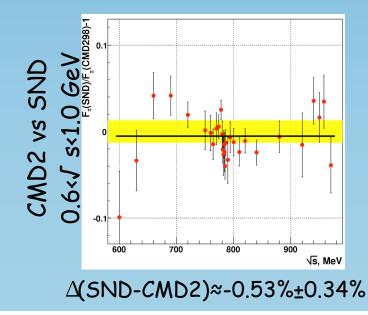
Pion formfactor - results



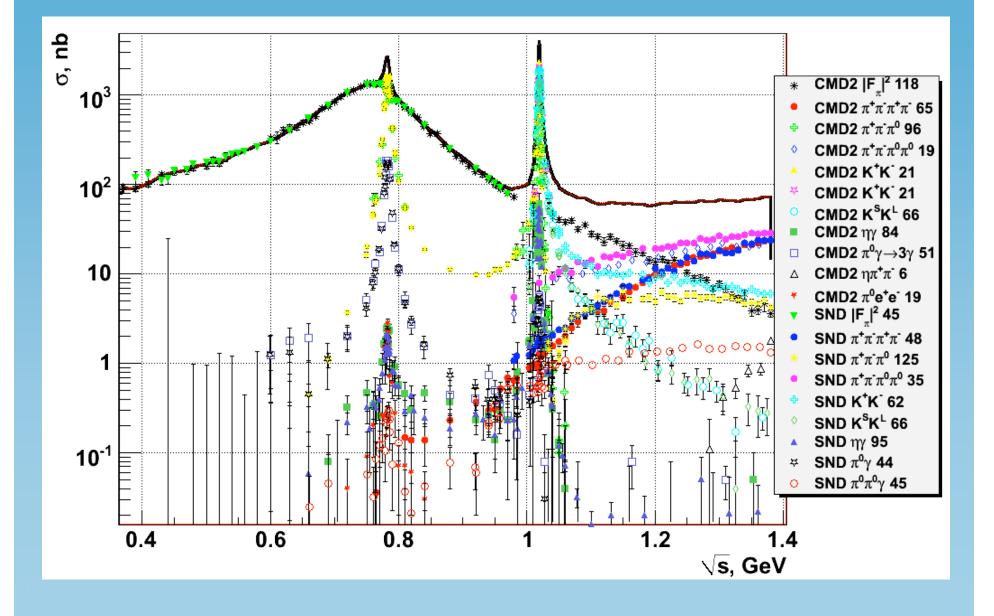
Internal Cross-checks





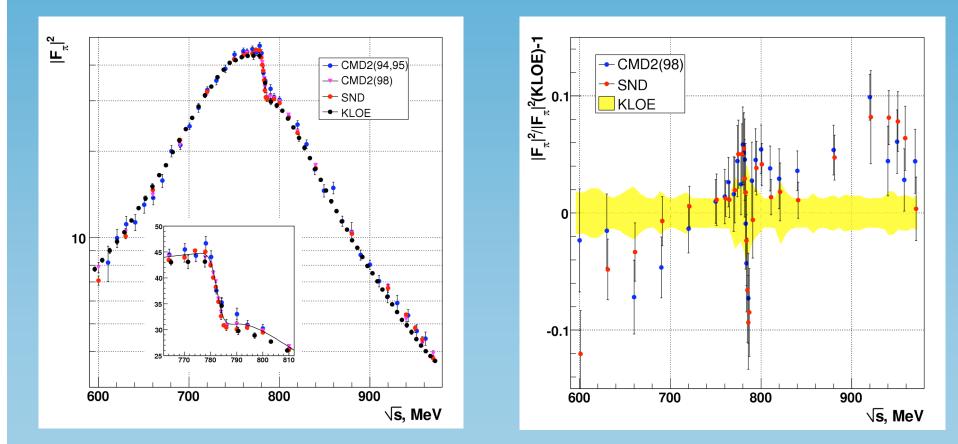


Overview of the results

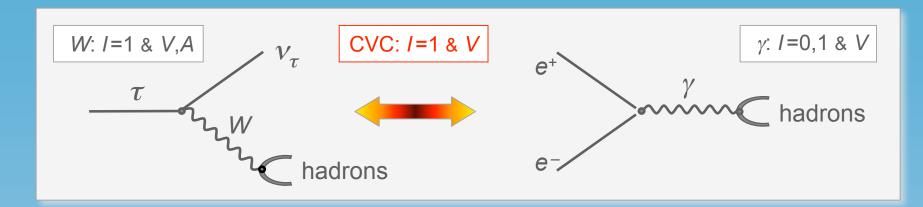


Comparison with KLOE (2005)

KLOE studied $e^+e^- \rightarrow \pi_+\pi_-\gamma$ working at DAFNE ϕ -factory - first ISR experiment



The Role of τ Data through CVC – SU(2)



Hadronic physics factorizes in Spectral Functions :

Isospin symmetry connects $I=1 e^+e^-$ cross section to vector τ spectral functions:

$$\sigma^{(l-1)}\left[e^+e^- \to \pi^+\pi^-\right] = \frac{4\pi\alpha^2}{s}\upsilon\left[\tau^- \to \pi^-\pi^0\nu_\tau\right]$$

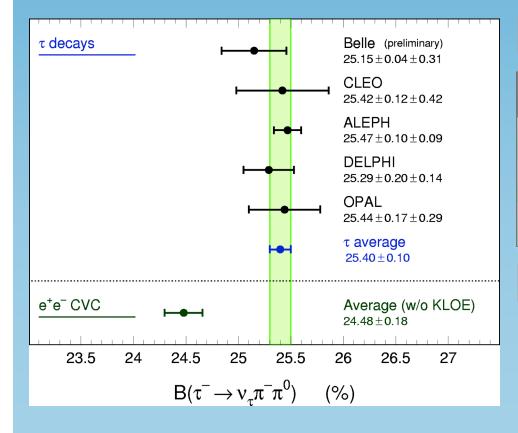
fundamental ingredient relating long distance (resonances) to short distance description (QCD)

$$\upsilon \left[\tau^{-} \rightarrow \pi^{-} \pi^{0} \upsilon_{\tau}\right] \propto \begin{bmatrix} \mathsf{BR}\left[\tau^{-} \rightarrow \pi^{-} \pi^{0} \upsilon_{\tau}\right] & 1 & dN_{\pi\tau^{0}} \\ \mathsf{BR}\left[\tau^{-} \rightarrow e^{-} \upsilon_{0} \upsilon_{\tau}\right] & N_{\pi\tau^{0}} & ds \end{bmatrix} \begin{bmatrix} m_{\tau}^{2} \\ \left(1 - s/m_{\tau}^{2}\right)^{2} \left(1 + s/m_{\tau}^{2}\right) \\ \mathsf{branching fractions} & \mathsf{mass spectrum \ kinematic factor (PS)} \end{bmatrix}$$

Testing CVC with one number

Infer τ branching fractions (more robust than spectral functions) from e^+e^- data:

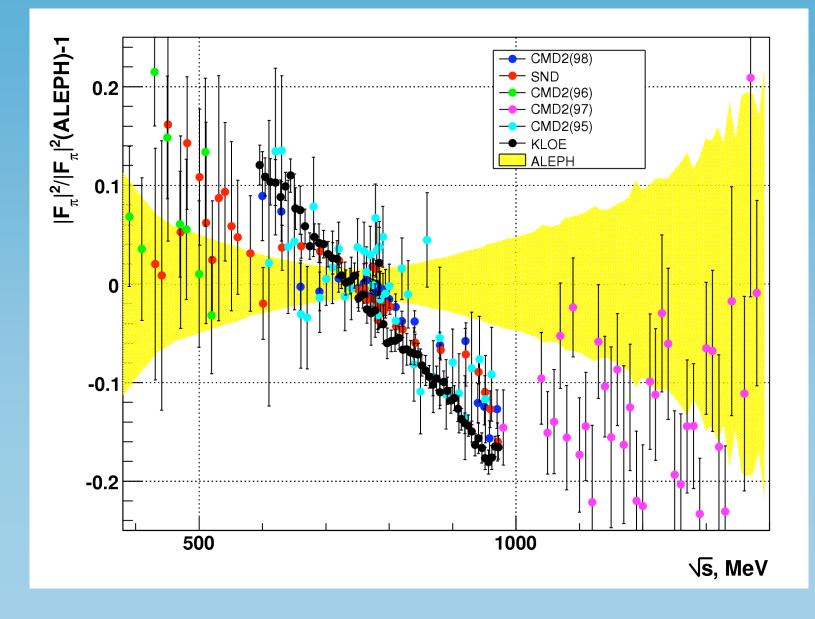
$$\mathsf{BR}_{\mathsf{CVC}}\left(\tau^{-} \to \pi^{-}\pi^{0}v_{\tau}\right) = \frac{6\pi |V_{ud}|^{2} S_{\mathsf{EW}}}{m_{\tau}^{2}} \int_{0}^{m_{\tau}^{2}} ds \, \mathrm{kin}(s) \cdot v^{\mathsf{SU}(2)-\mathsf{corrected}}(s)$$



Difference: BR[τ] - BR[e^+e^- (CVC)]: Mode $\Delta(\tau - e^+e^-)$ "Sigma" $\tau^- \rightarrow \pi^- \pi^0 v_{\tau}$ + 0.92 ± 0.21 4.5 $\tau^- \rightarrow \pi^- 3\pi^0 v_{\tau}$ - 0.08 ± 0.11 0.7 $\tau^- \rightarrow 2\pi^- \pi^+ \pi^0 v_{\tau}$ + 0.91 ± 0.25 3.6

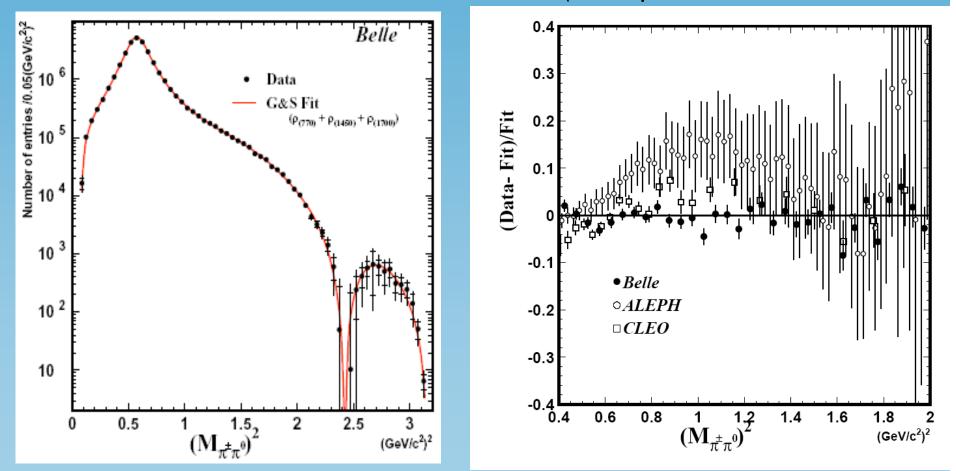
ee data on $\pi^-\pi^+\pi^0\pi^0$ not satisfactory

Comparison with ALEPH ($\tau \rightarrow \pi \pi^0 \nu$)



Belle analysis of tau decays

Pion formfactor, calculated from the spectral function of $\tau^- \rightarrow \pi^- \pi^0 v_{\tau}$ decay

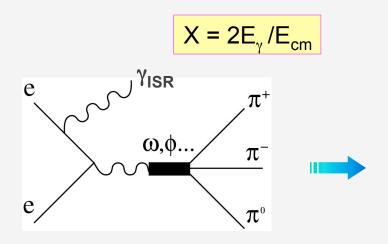


EPS2005 Proceedings - hep-ex/0512071

BaBar R measurement program using ISR

Other exclusive channels: BaBar ISR

- systematic program underway using ISR from Y(4S) energies, taking advantage of high luminosity (B-factory)
- statistics comparable to CMD-2/SND for E_{cm} <1.4 GeV, much better than DM1/DM2 above
- full energy range covered at the same time

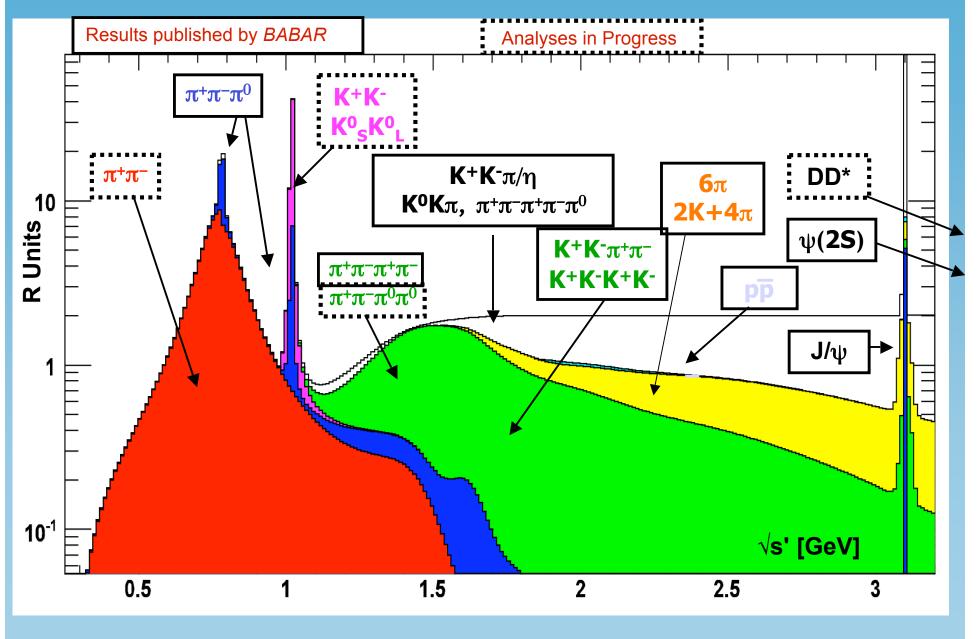


$$\frac{d\sigma(s,x)}{dxd(\cos\theta)} = H(s,x,\theta) \cdot \sigma_0(s(1-x))$$

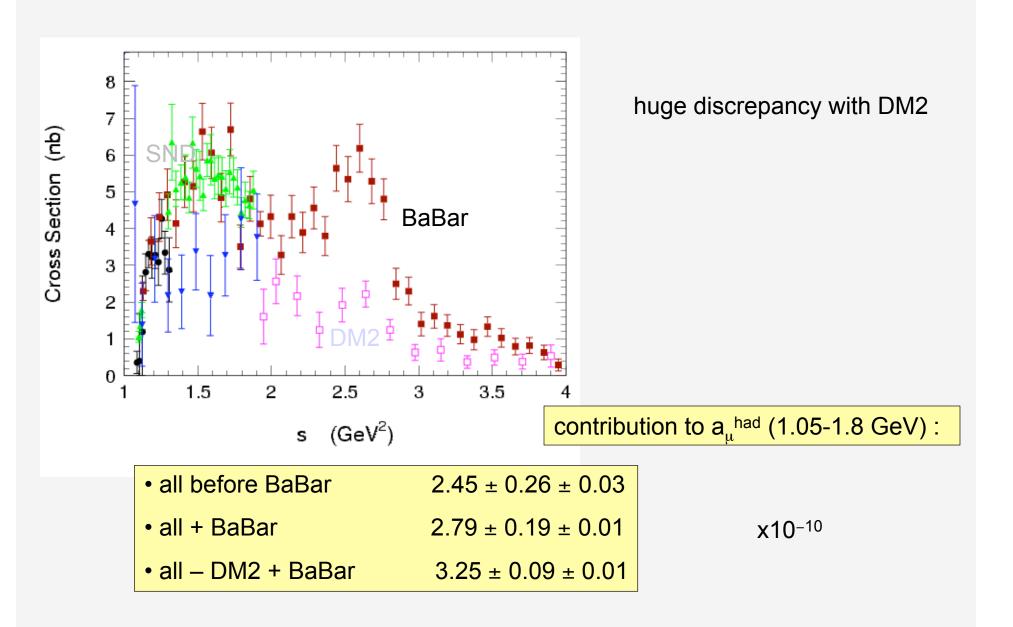
$$H(s, x, \theta) = \frac{\alpha}{\pi x} \left(\frac{2 - 2x + x^2}{\sin^2 \theta} - \frac{x^2}{2} \right), \quad x = \frac{2E_{\gamma}}{\sqrt{s}}$$

H is radiation function

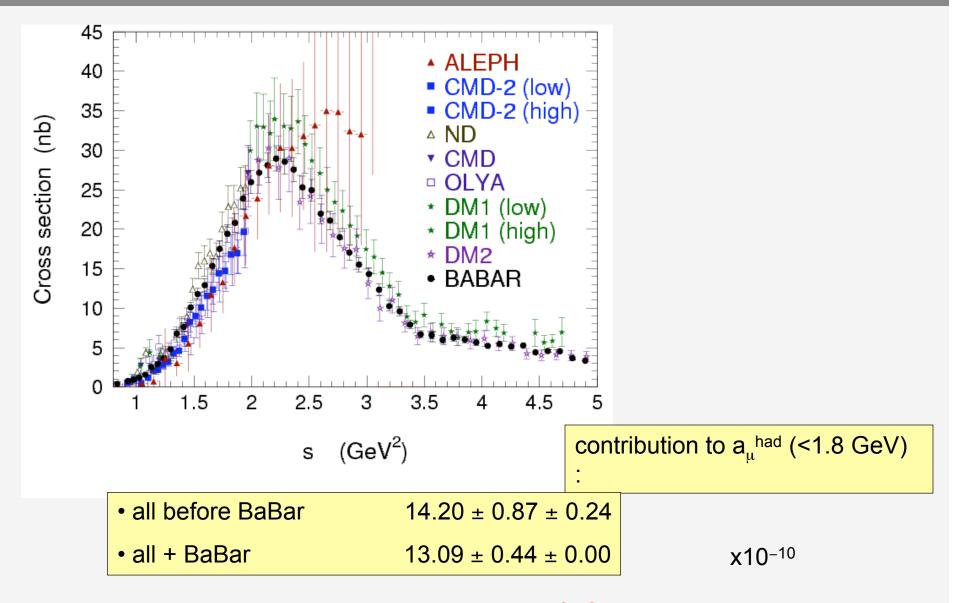
Build R from Sum Over Exclusive Final States (MC)



BaBar ISR: $\pi^+\pi^-\pi^0$

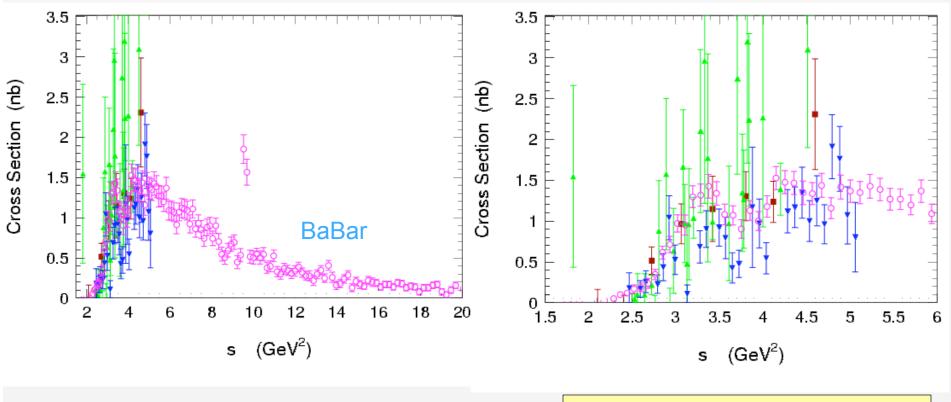


BaBar ISR: $2\pi^+2\pi^-$

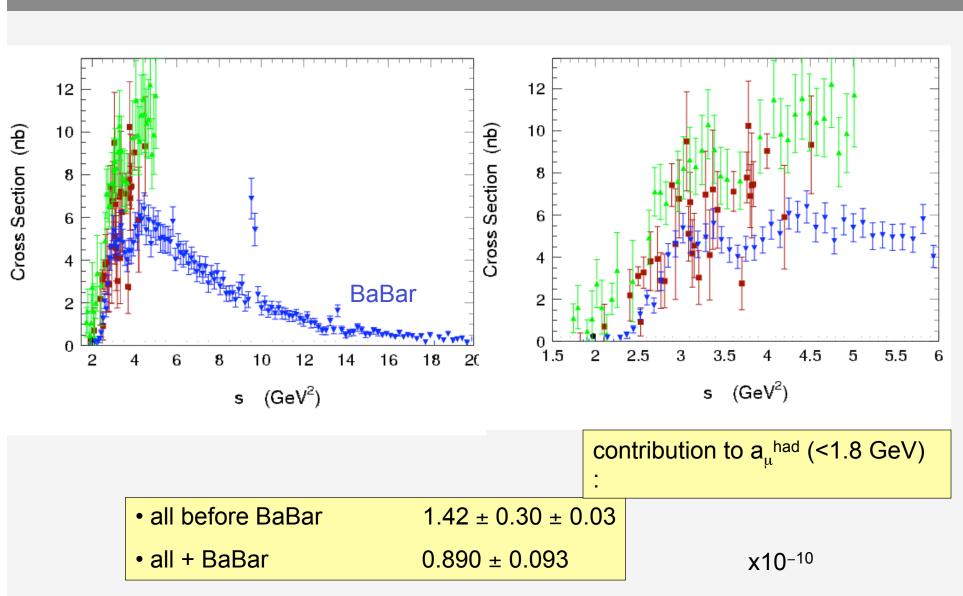


Waiting for a similar results from $\pi^+\pi^-\pi^0\pi^0$ mode !

BaBar ISR: $3\pi^+3\pi^-$

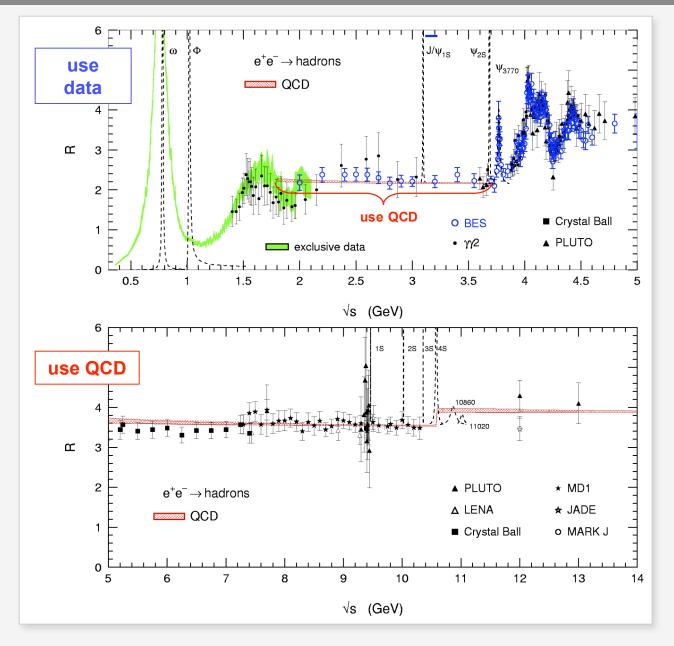


		contribution to a_{μ}^{had} (<1.8 GeV)	
all before BaBar	0.10 ± 0.10		
• all + BaBar	0.108 ± 0.016	x10 ^{−10}	



BaBar ISR: $2\pi^+2\pi^-2\pi^0$

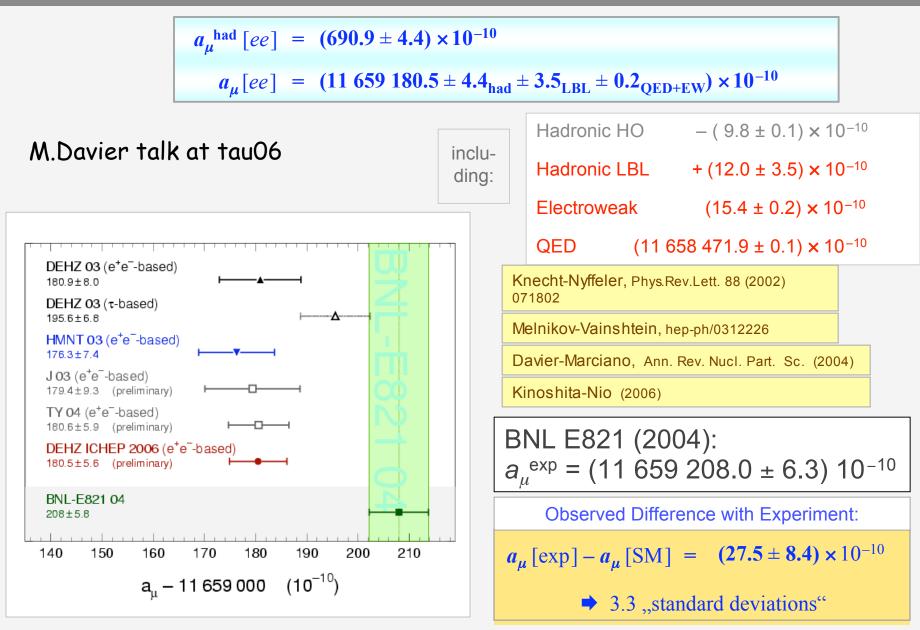
Evaluating the Dispersion Integral



Agreement between Data (BES) and pQCD (within correlated systematic errors)

Better agreement between exclusive and inclusive (γγ2) data than in 1997-1998 analyses

Update for ICHEP-Tau06

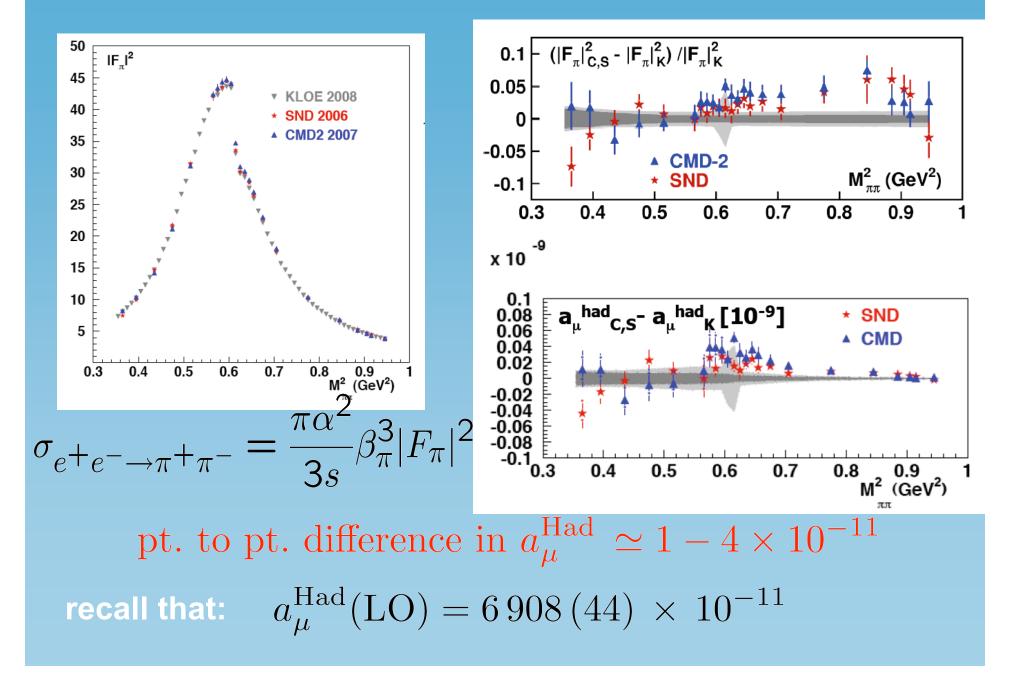


Contributions to a_{μ}^{had} [in 10⁻¹⁰] from the different energy domains

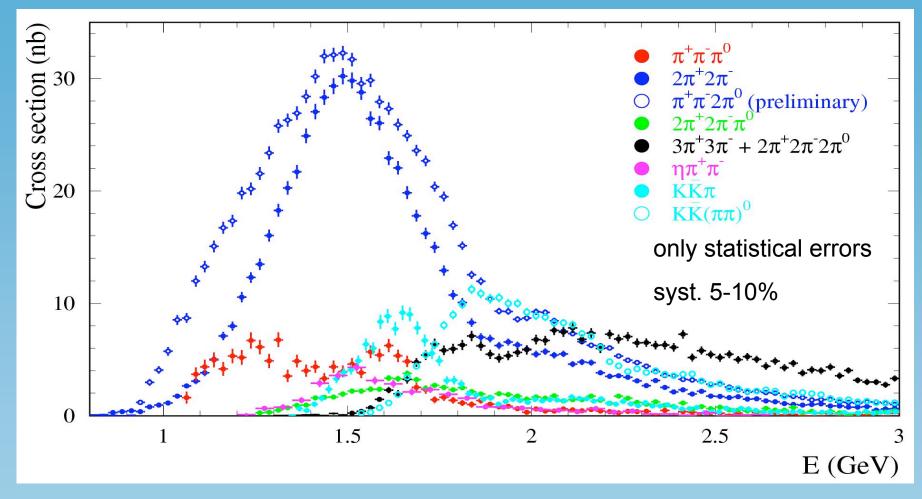
Modes	Energy [GeV]	<i>e</i> ⁺ <i>e</i> ⁻	τ
Low s expansion	$2m_{\pi} - 0.5$	$55.6 \pm 0.8 \pm 0.1_{rad}$	$56.0 \pm 1.6 \pm 0.3_{\rm SU(2)}$
$\pi^+\pi^-$ (+SND+CMD2)	0.5 - 1.8	$449.0 \neq 3.0 \neq 0.9_{\rm rad}$	$464.0 \pm 3.0 \pm 2.3_{\rm SU(2)}$
			With MV corr. $456.0 \pm 3.0 \pm 6.0_{SU(2)}$
$\pi^+\pi^-2\pi^0$	$2m_{\pi} - 1.8$	$16.8 \pm 1.3 \pm 0.2_{rad}$	${\bf 21.4 \pm 1.3 \pm 0.6_{\rm SU(2)}}$
$2\pi^+2\pi^-$ (+BaBar)	$2m_{\pi} - 1.8$	$13.1 \pm 0.4 \pm 0.0_{rad}$	$12.3 \pm 1.0 \pm 0.4_{\rm SU(2)}$
ω (782)	0.3 – 0.81	$38.0 = 1.0 \pm 0.3_{rad}$ 2	2.4 –
φ (1020)	1.0 – 1.055	$35.7 \pm 0.8 \pm 0.2_{rad}$	-
Other excl. (+BaBar)	$2m_{\pi} - 1.8$	$24.3 \pm 1.3 \pm 0.2_{rad}$	-
$J/\psi, \psi(2S)$	3.08 - 3.11	$7.4 \pm 0.4 \pm 0.0_{rad}$	-
<i>R</i> [QCD]	1.8 – 3.7	$33.9 \pm 0.5_{\text{theo}}$	-
R [data]	3.7 – 5.0	$\textbf{7.2} \pm \textbf{0.3} \pm \textbf{0.0}_{rad}$	-
<i>R</i> [QCD]	$5.0 - \infty$	$9.9 \pm 0.2_{\rm theo}$	-
Sum (w/o KLOE)	$2m_{\pi}-\infty$	$690.8 \pm 3.9 \pm 1.9_{rad} \pm 0.7_{QCD}$	$710.1 \pm 5.0 \pm 0.7_{\rm rad} \pm 2.8_{\rm SU(2)}$

What we have now?

$|F_{\pi}|^2$ from KLOE (2008), CMD2 and SND agree well



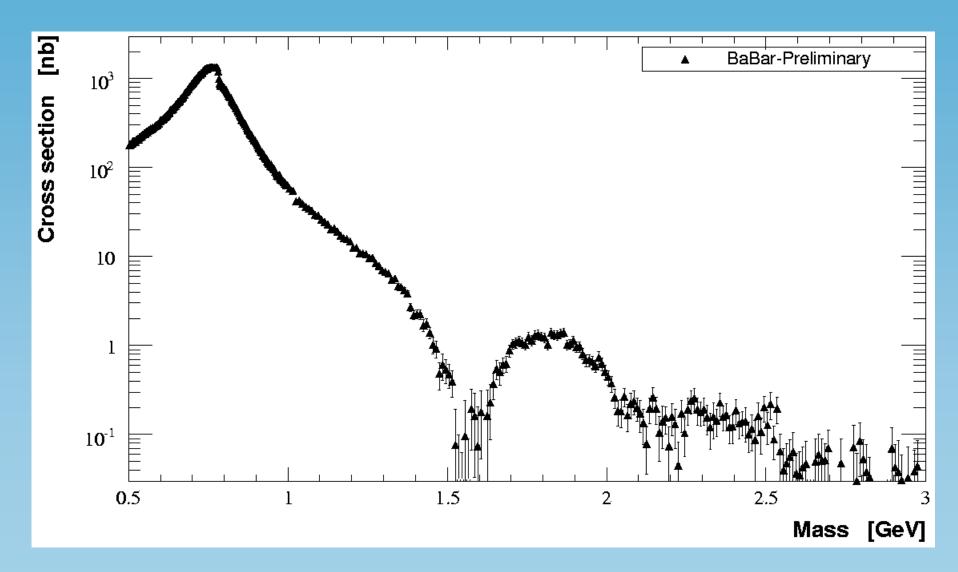
More BaBar data are available



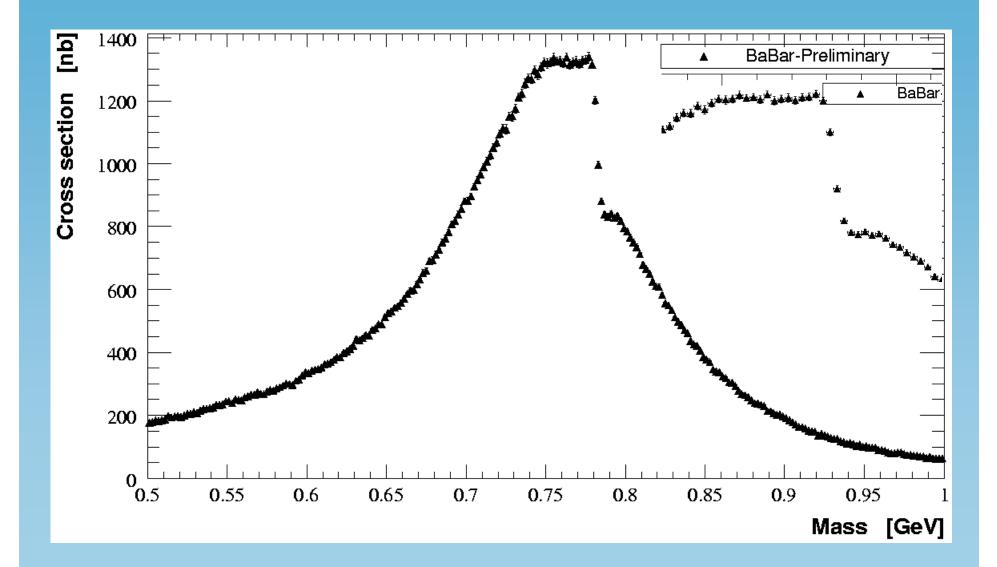
to obtain R in the energy range 1-2 GeV the processes $\pi^+\pi^-3\pi^0$, $\pi^+\pi^-4\pi^0$, K^+K^- , K_SK_L , $K_SK_L\pi\pi$, $K_SK^+\pi^-\pi^0$ remain to be measured

New in 2008: BaBar results (preliminary)

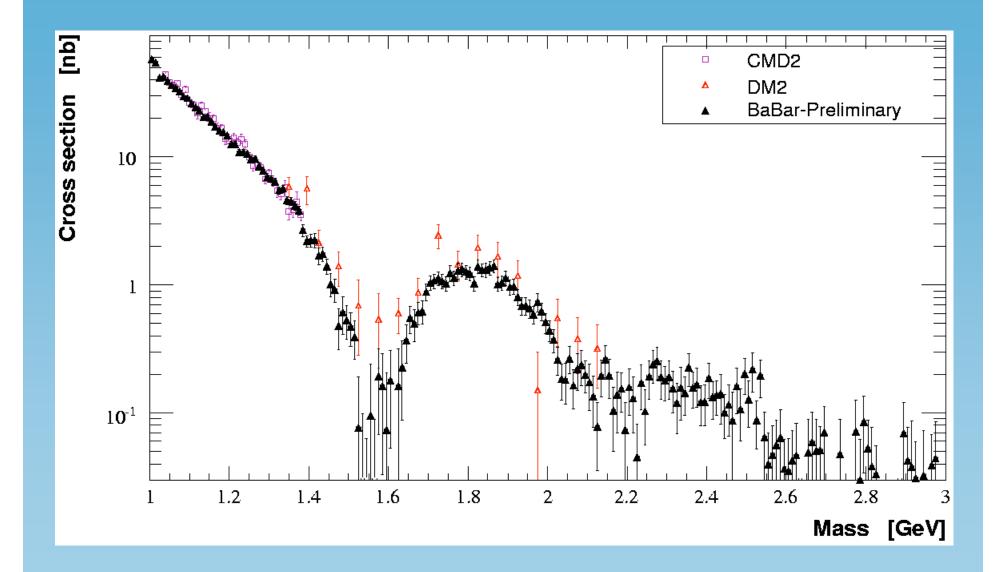
The eter $\rightarrow \pi^{+}\pi^{-}$ cross section via ISR



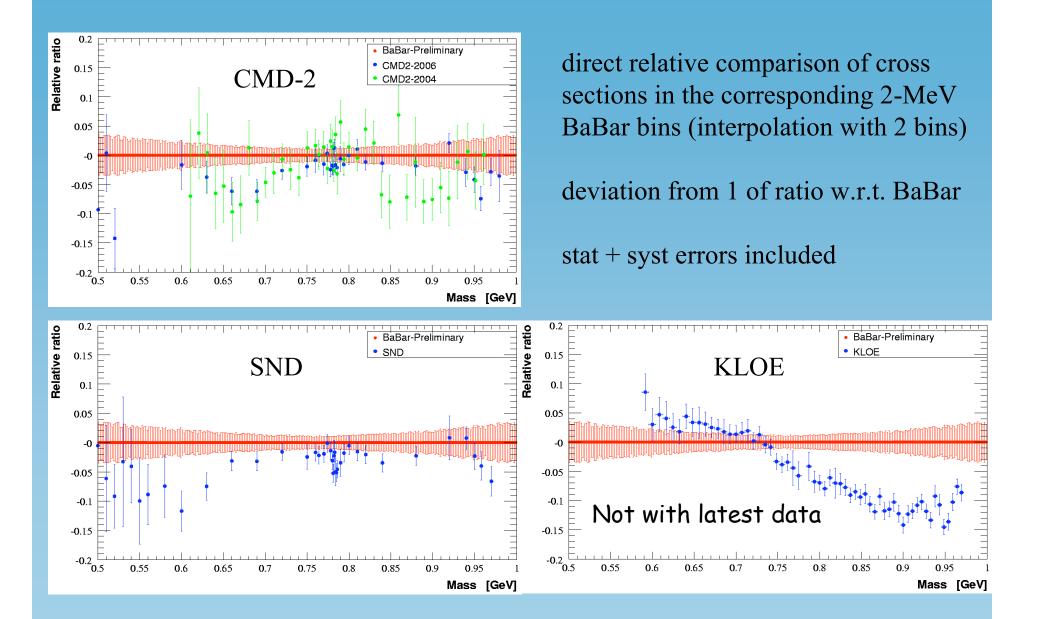
BaBar results in ρ region



BaBar vs. other experiments at large mass

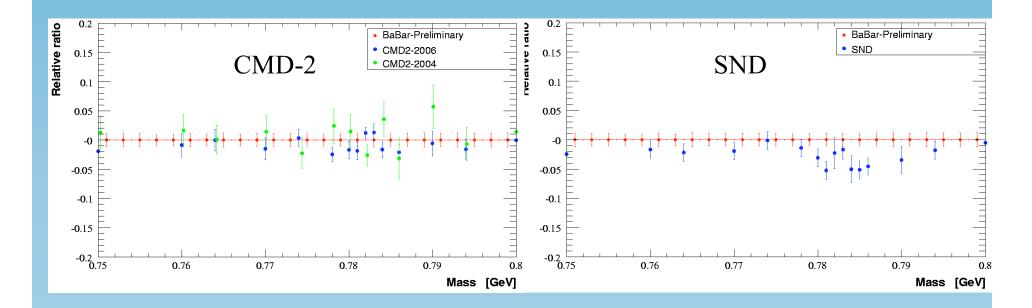


BaBar vs.other ee data (0.5-1.0 GeV)

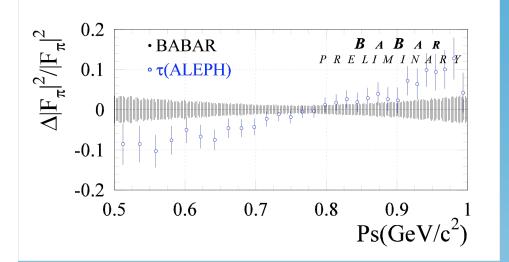


BaBar vs.other ee data (ρ - ω interference region)

- mass calibration of BaBar checked with ISR-produced $J/\psi \rightarrow \mu\mu$
- expect $-(0.16 \pm 0.16)$ MeV at ρ peak
- ω mass can be determined through mass distribution fit (in progress)
- Novosibirsk data precisely calibrated using resonant depolarization
- comparison BaBar/CMD-2/SND in ρ-ω interference region shows no evidence for a mass shift

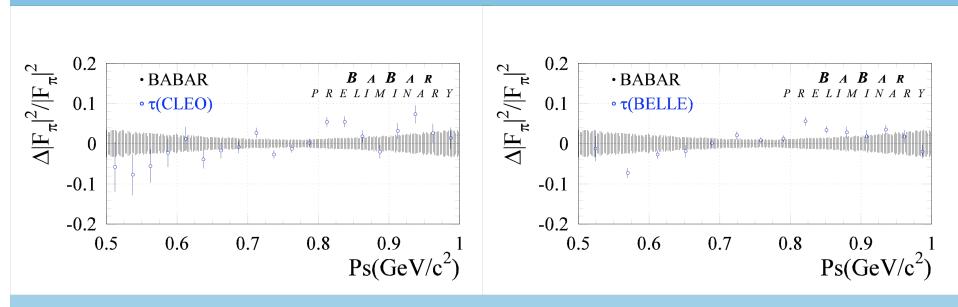


BaBar vs. IB-corrected τ data (0.5-1.0 GeV)

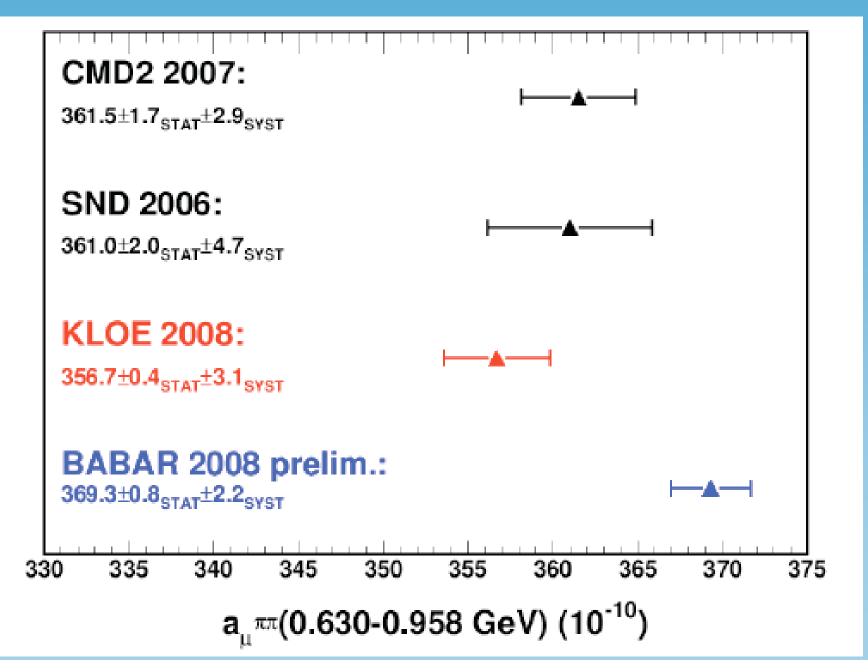


relative comparison w.r.t. BaBar of isospin-breaking corrected τ spectral functions

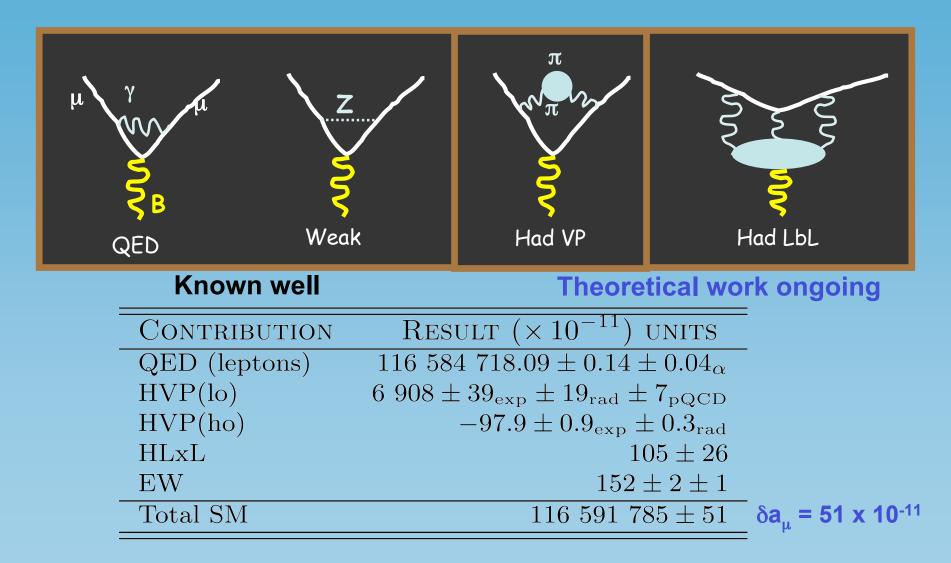
BaBar data averaged in wider τ bins and corrected for ρ - ω interference



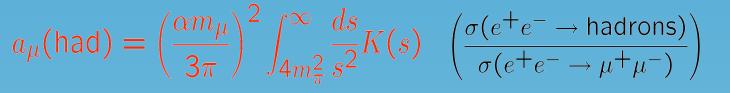
Different measurements in 630-958 MeV

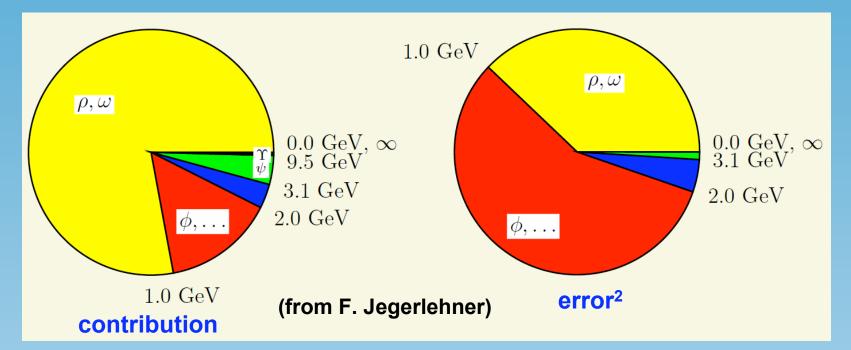


$a_{\mu} = (g - 2)/2$ Latest evaluation



Analyticity and the optical theorem:

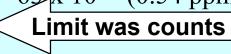




- Future efforts will reduce errors
 - Additional KLOE data (in hand, near term)
 - BaBar finalize $\pi\pi$, more multihadrons, perhaps Belle
 - CMD3 at VEPP2000, up to 2.0 GeV (next 5 years)

New $a_{\mu} = (g - 2)/2$ measurement is proposed at FNAL

- Present Status E821:
 - Experimental uncertainty = $63 \times 10^{-11} (0.54 \text{ ppm})$
 - 0.46 ppm statistical



- 0.28 ppm systematic
- Theory uncertainty = $51 \times 10^{-11} (0.44 \text{ ppm})$

Leads to Δa_{μ} (Expt – Thy) = 295 ± 81 x 10⁻¹¹ 3.6 σ

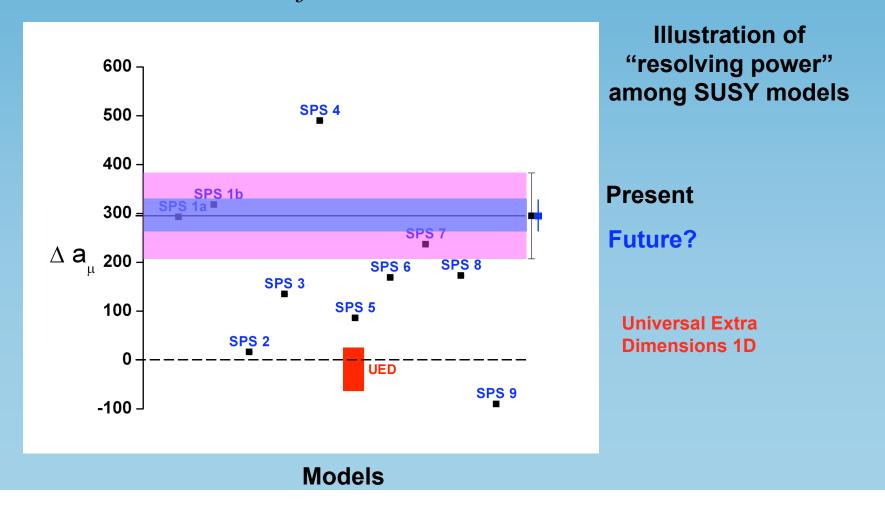
- Expected situation after FNAL experiment:
 - Experimental uncertainty: $63 \rightarrow 16 \times 10^{-11}$
 - 0.1 ppm statistical \rightarrow 21x the E821 events
 - 0.1 ppm systematic overall
 - − 0.07 ppm field \rightarrow 0.17 \rightarrow 0.07
 - 0.07 ppm $ω_a$ → 0.21 → 0.07

- Theory uncertainty: $51 \rightarrow 30 \times 10^{-11}$

Future: $\Delta a_{\mu}(\text{Expt} - \text{Thy}) = xx \pm 34 \times 10^{-11}$

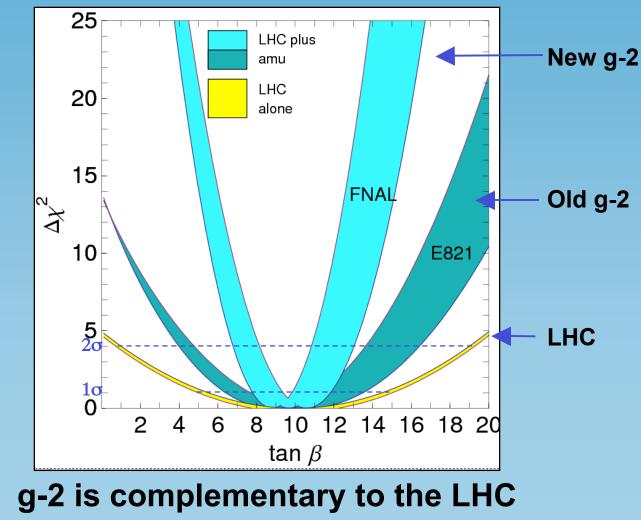
(If xx remains 295, the deviation from zero would be close to 9σ)

The Snowmass Points and Slopes are 10 representative SUSY models with typical parameters for M_{SUSY} masses and tanβ, etc. They serve as test points to indicate the discrimination power of experiments.
 Muon g-2 is a powerful discriminator *no matter where the final value lands*



Suppose the MSSM reference point SPS1a* is realized and parameters are determined by global fit from full LHC data

- sign(μ) difficult to obtain from the collider
- $\tan \beta$ poorly determined by collider



Conclusions

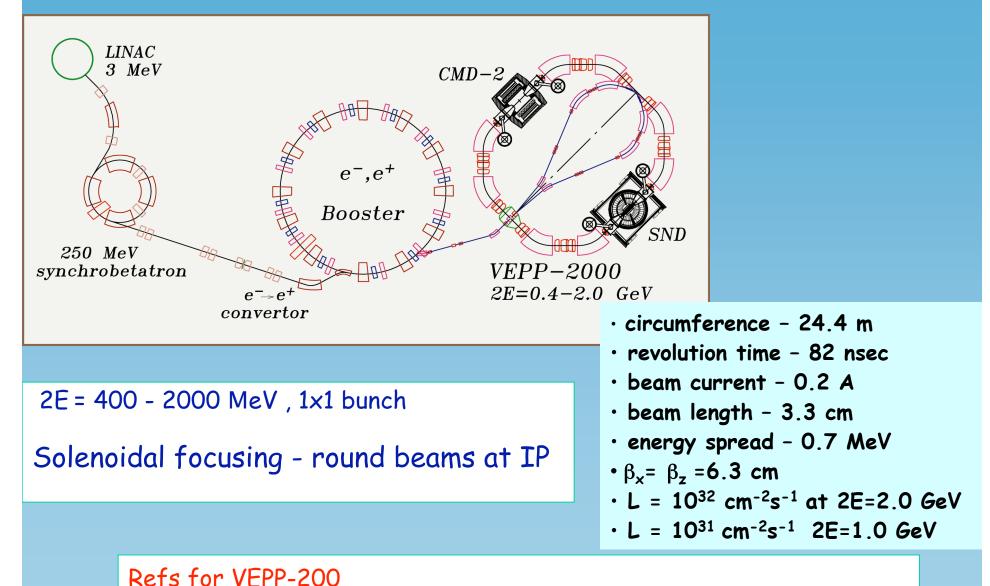
- Hadronic vacuum polarization is still the dominant systematics for SM prediction of the muon g 2
- Significant step in precision from new experimental input

CMD-2 + SND +KLOE for 2π BaBar for multi-pion channels

- Precision of SM prediction (±5.1) now exceeds experimental precision (±6.3)
- Discrepancy with τ data (ALEPH & CLEO & OPAL) still remain
- Final result from BELLE awaited only 1.5 σ from e⁺e⁻ data now
- Until τ / e^+e^- puzzle is solved, only e^+e^- data used in dispersion integral
- SM prediction for a_{μ} differs by 3.6 σ [e^+e^-] from experiment (BNL 2004)
- New proposal to measure muon g 2 with $1,6 \ge 10^{-10}$ accuracy is submitted
- The high interest to low energy cross section measurement motivates new project VEPP2000

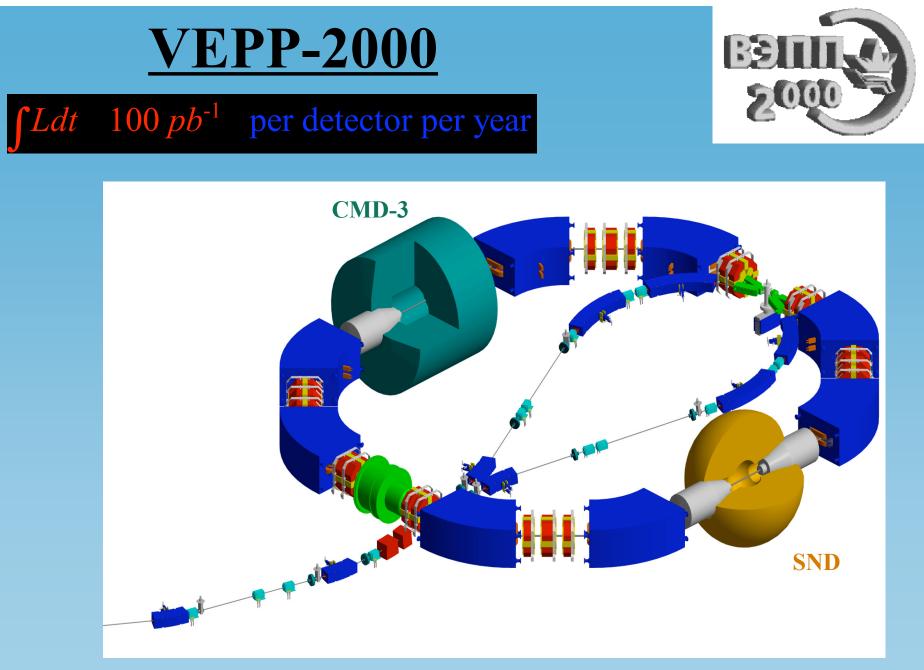
VEPP2000 project

VEPP-2000 e⁺e⁻ collider

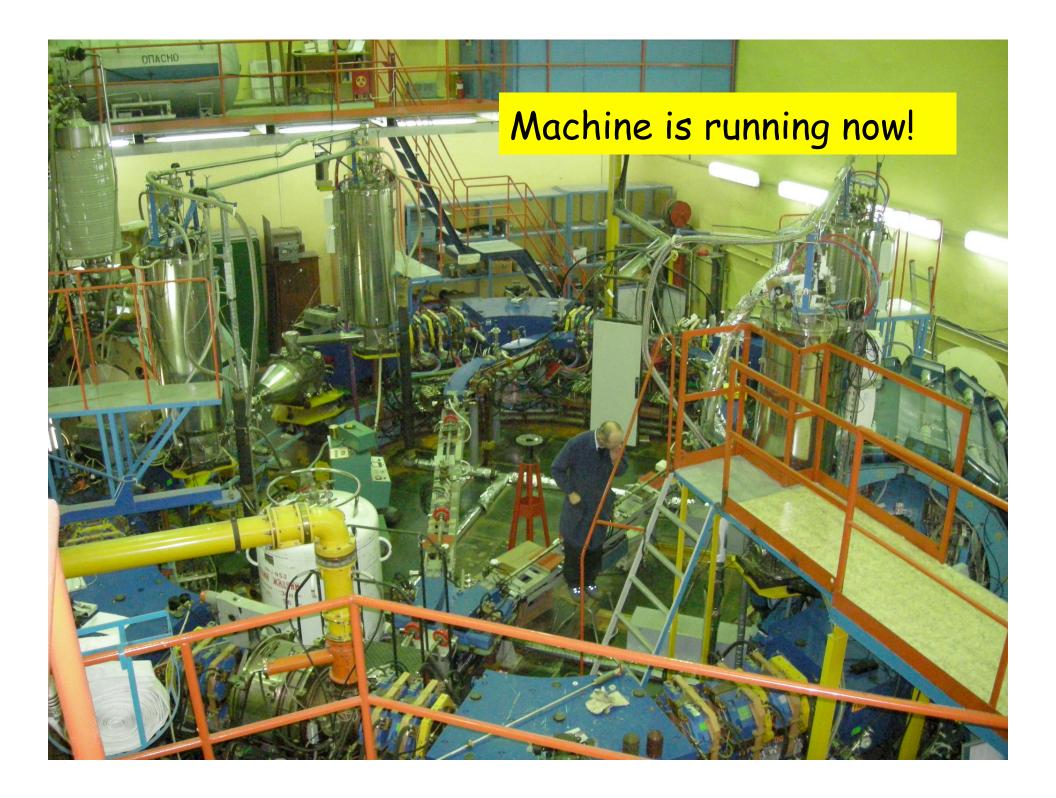


1. In: Proc.Frascati Phys.Series, v XVI, p.393, Nov.16-19, 1999

2. In: Proc. 7-th Europ.Part.Accel.Conf., EPAC 2000, p.439, Vienna, 2000



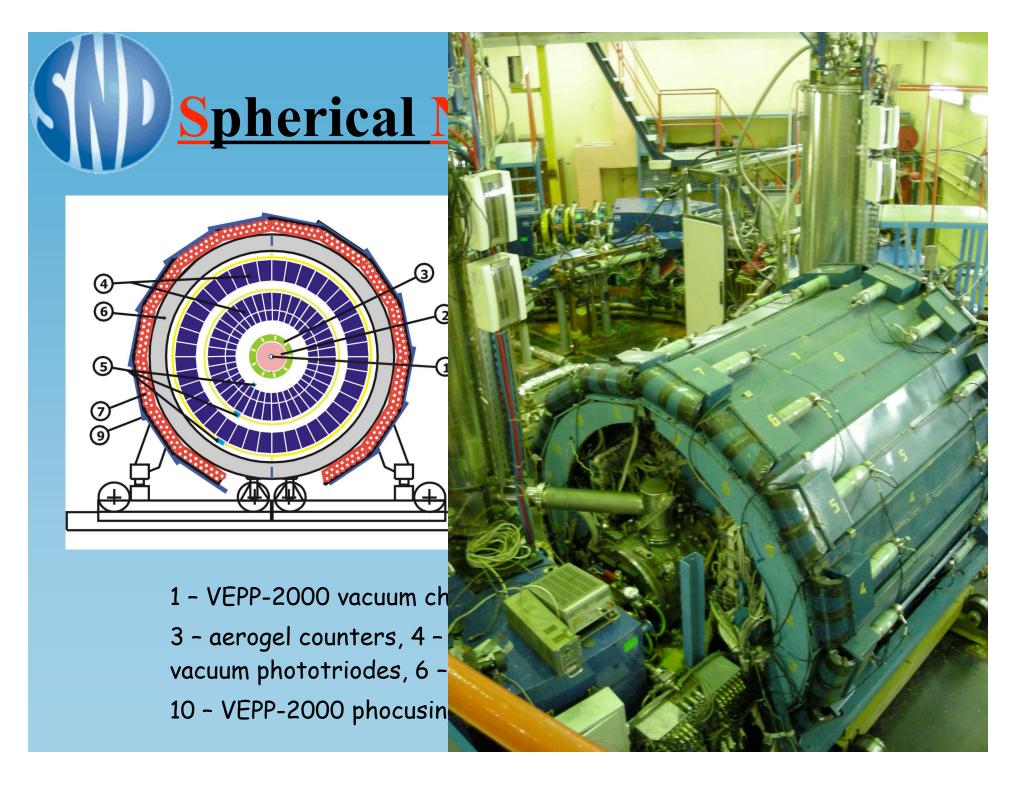
Total integrated luminosity with all detectors on VEPP-2M $\sim 70 \text{ pb}^{-1}$

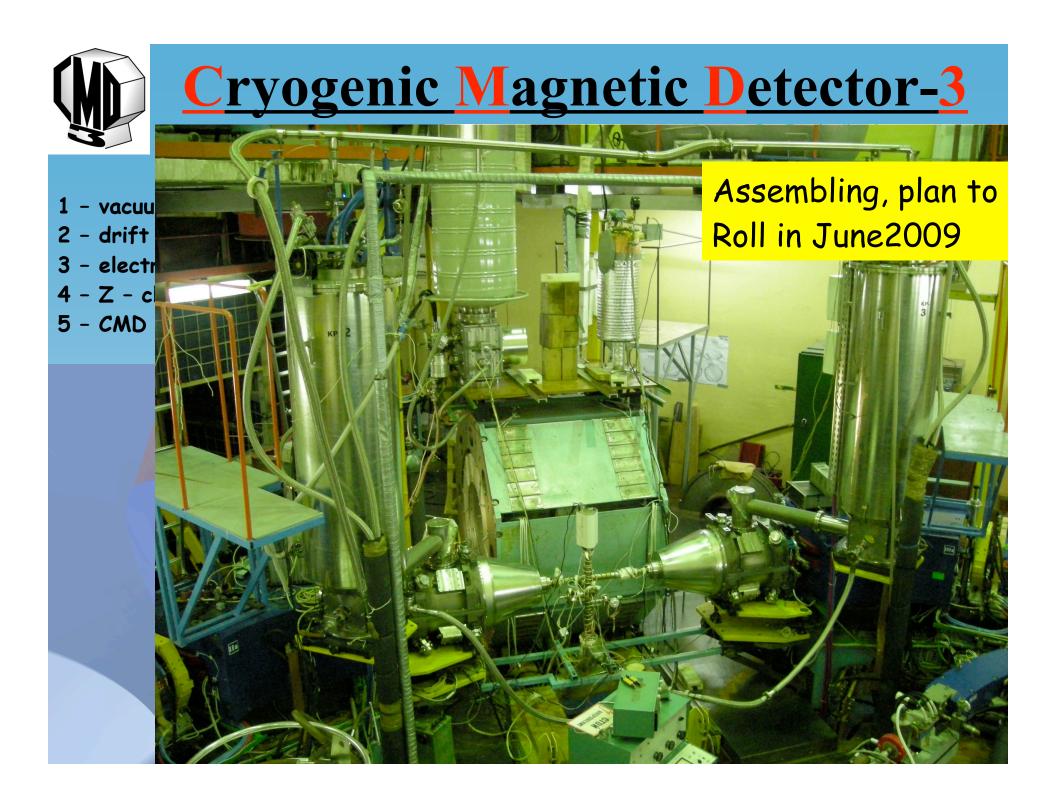


Physics program at VEPP-2000

- 1. Precise measurement of the quantity R= $\sigma(e+e^{--} > hadrons) / \sigma(e+e^{--}) + \mu^{--})$
- 2. Study of hadronic channels: $e+e^{--} > 2h$, 3h, 4h ..., $h=\pi, K, \eta$
- 3. Study of 'excited' vector mesons: $\rho', \rho'', \omega', \phi', ...$
- 4. CVC tests: comparison of $e+e^{--}$ > hadr. (T=1) cross section with τ -decay spectra
- Study of nucleon-antinucleon pair production nucleon electromagnetic form factors, search for NNbar resonances, ...
- 6. Hadron production in 'radiative return' (ISR) processes
- 7. Two photon physics
- 8. Test of the QED high order processes 2-> 4,5

With L_{peak} = 10³² cm⁻²sec⁻¹ luminosity x10-100 statistical improvement over existing BaBar ISR data in 1-2 GeV energy range





How can we improve measurement of R?

We expect to get the following improvements:

- high statistics! (x10-x100) current measurement is still statistics-limited
- radiative corrections to 0.1% add photon jet + large angle γ
- measure radiative tails and compare them to calculations (ISR?)
- luminosity to 0.5%, use $\gamma\gamma$ in addition to Bhabha for cross-check

• much better separation (LXe @CMD-3, Cerenkov @SND) - smaller systematic error, try to measure e+e- $\rightarrow \mu$ + μ -

- precise trigger efficiency monitoring
- better drift chambers higher resolution, efficiencies

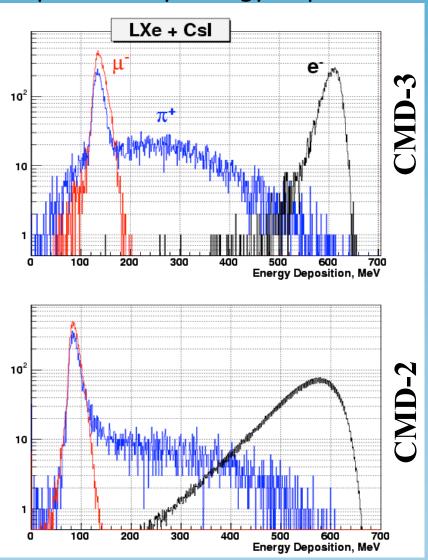
We expect to:

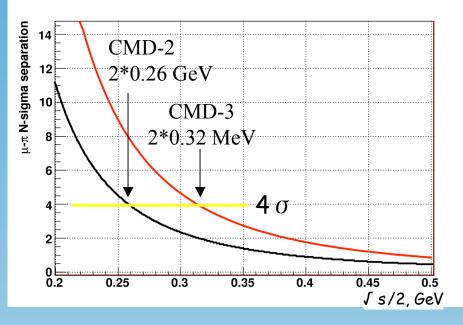
- measure 2π mode to 0.3-0.4%, 4π mode to 2%
- overall improvement in R precision by factor 2-3

Examples of improvements (CMD-3)

Separation by energy deposition

Separation by momentum





Because of better resolution of the drift chamber, the separation by momentum should work up to $\int s \approx 0.65$ GeV

Conclusion

- Measurement of R is still very active and important field
- Important for interpretation of g-2 experiment, evaluation of α (M_Z), tests of QCD
- Recent improvements: VEPP-2M, BES
- Lots of data are being analyzed: VEPP-2M, KLOE, BaBar, CLEO
- Current projects: VEPP-2000, BESIII
- ISR experiments have demonstrated impressive potential: KLOE, BaBar.
- Expect to reach 0.3-5% precision over the whole 0-10 GeV range in few years (factor of 2 improvement)

Thank you

• Objective :

Precise cross section measurements for all significant processes,

 $e^+ e^- \rightarrow f$, from threshold to c.m. energy ~ 4.5-5.0 GeV

• Purpose :

Significantly improve understanding of the spectroscopy of $J^{PC} = 1^{--}$

states, and of their resonant substructure

Combine the cross section measurements to obtain improved

precision on the c.m. energy dependence of \mathbf{R} in this region

• Reactions for which results have been published < 2006:

 $e^{+}e^{-} \rightarrow p\overline{p}$ $e^{+}e^{-} \rightarrow \pi^{+}\pi^{-}\pi^{0}$ $e^{+}e^{-} \rightarrow 2\pi^{+}2\pi^{-}, K^{+}K^{-}\pi^{+}\pi^{-}, 2K^{+}2K^{-}$ $e^{+}e^{-} \rightarrow 3\pi^{+}3\pi^{-}, 2\pi^{+}2\pi^{-}\pi^{0}\pi^{0}, K^{+}K^{-}2\pi^{+}2\pi^{-}$

• New results published in 2006-2008 :

 $e^+e^- \rightarrow K^+K^-\pi^+\pi^-, K^+K^-\pi^0\pi^0, \phi\pi\pi, \phi f_0(980)$

a resonance structure at m=2.175 GeV/c² decaying to $\phi f_0(980)$

 $2\pi^+2\pi^-\pi^0$, K $\overline{K}\pi^0$, K $\overline{K}\eta$, $\Lambda \overline{\Lambda}$, $\Lambda \overline{\Sigma}$, $\Sigma \Sigma$

• Work in progress on :

 $\pi^{+}\pi^{-}, K \overline{K}, \pi^{+}\pi^{-}\pi^{0}\pi^{0}, \pi^{+}\pi^{-}3(\pi^{0}), \dots$