

The Mandelbrot Set

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PHYS 305
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Introduction

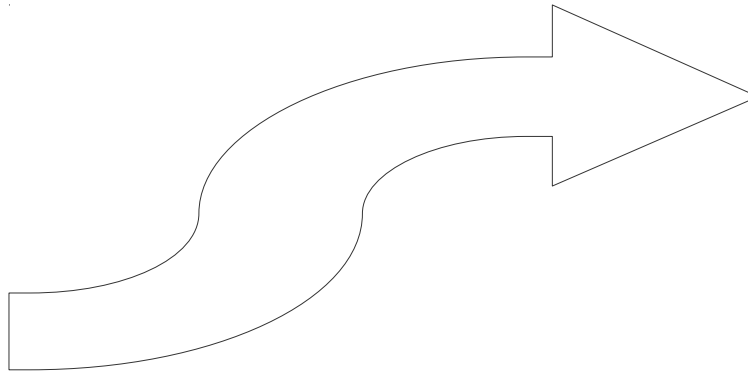
What is the Mandelbrot Set?

$$M = \{c \in \mathbb{C}, \forall n \geq N, |P_c^n| \leq s\}$$

where,

$$c = a + bi$$

$$P(0): z \rightarrow z^2 + c$$



$$z_0 = c$$



$$z_1 = c^2 + c = z_0^2 + c$$



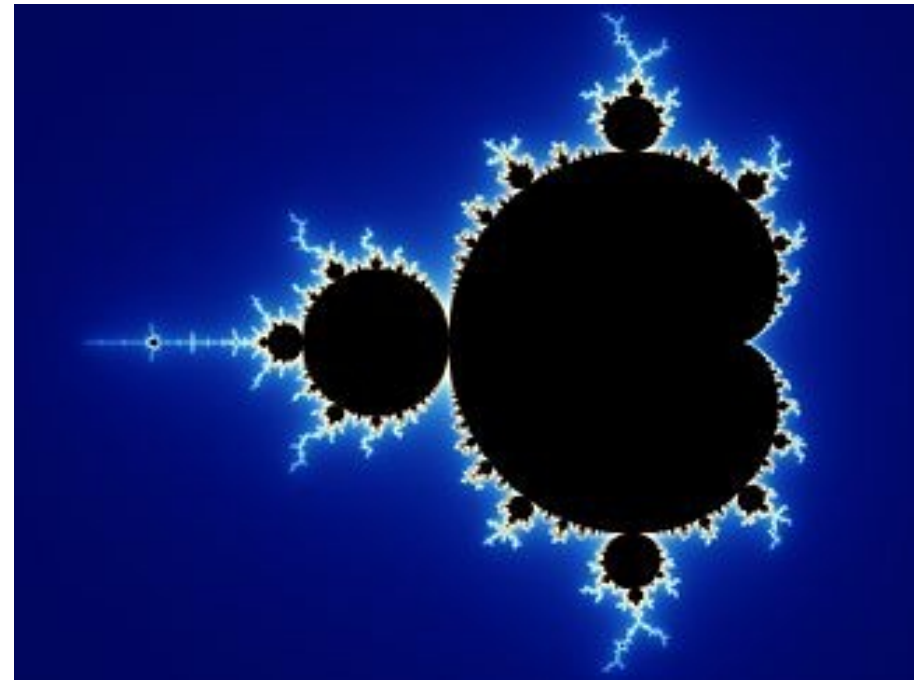
$$z_2 = (c^2 + c)^2 + c = z_1^2 + c$$



$$z_n = z_{n-1}^2 + c$$

Overview

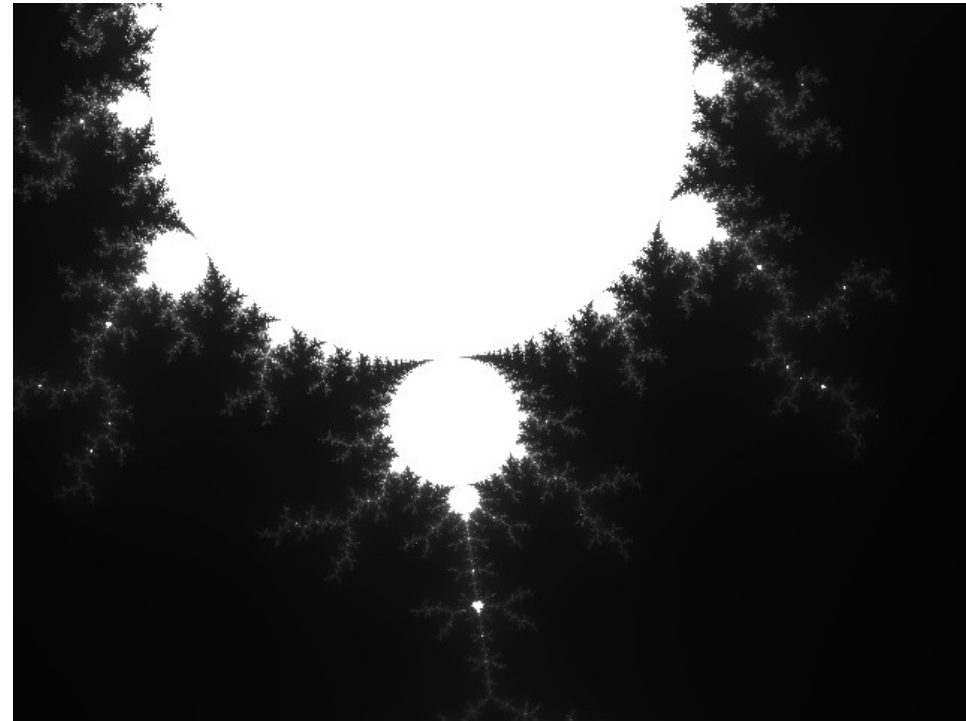
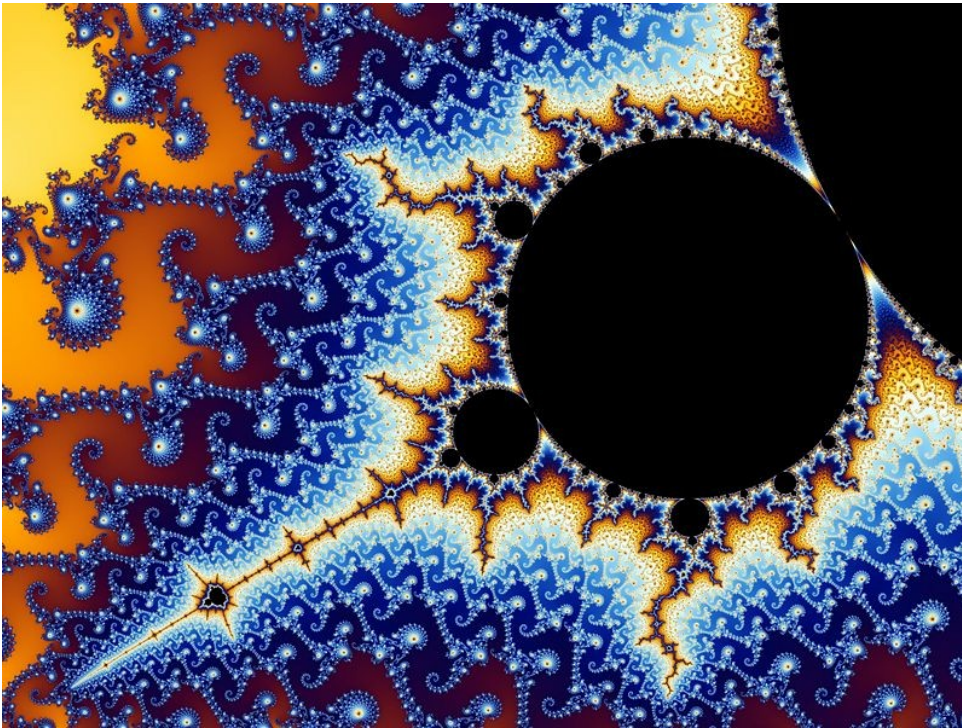
- In everyday terms?
 - A collection of numbers whose properties produce a fractal!
- Black area = in the set
 - Everything else = not an element of the set
- Color due to speed of divergence



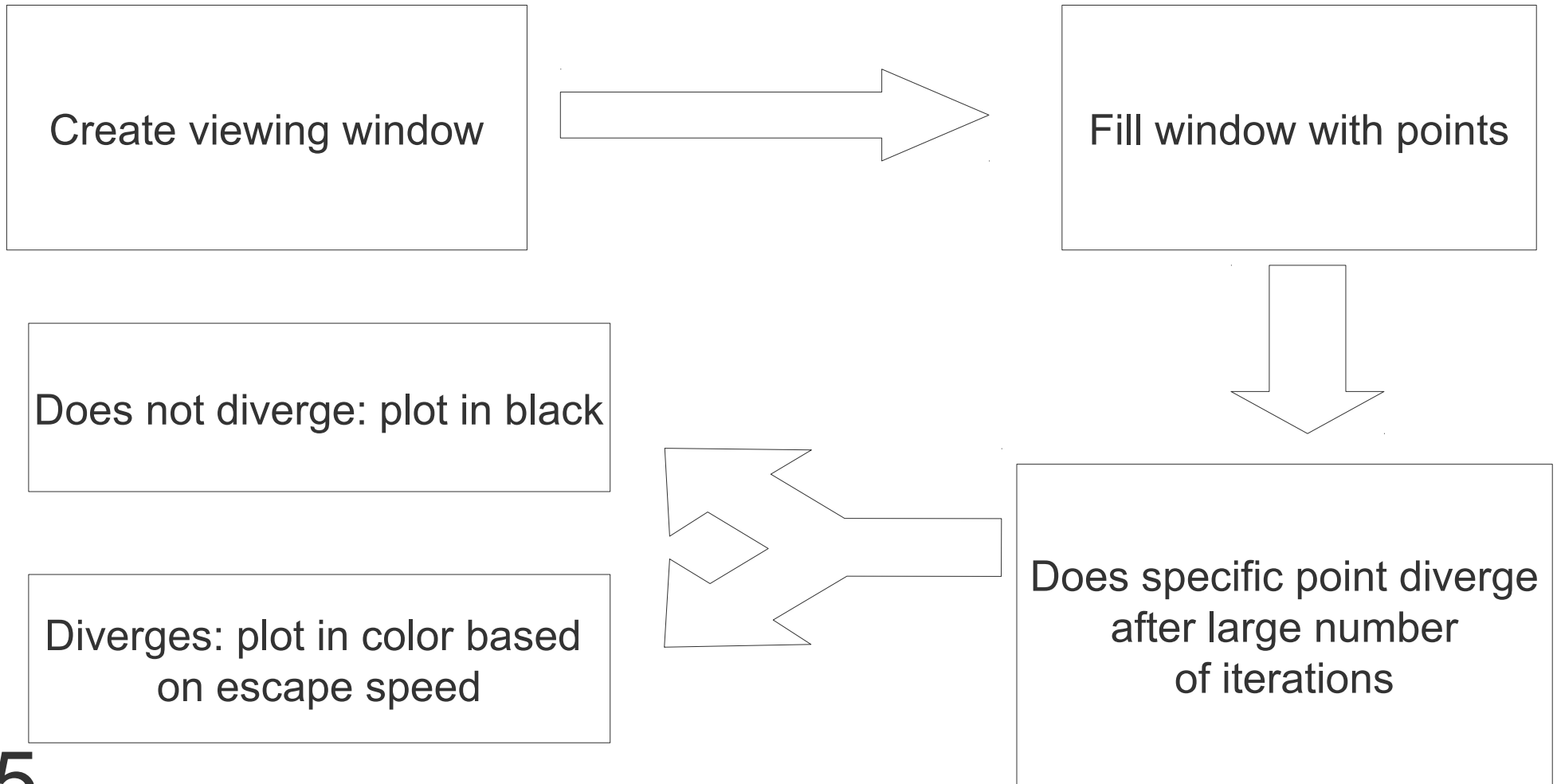
[1] <http://en.wikipedia.org/wiki/Mandelbrot_set>

Problem/Goals

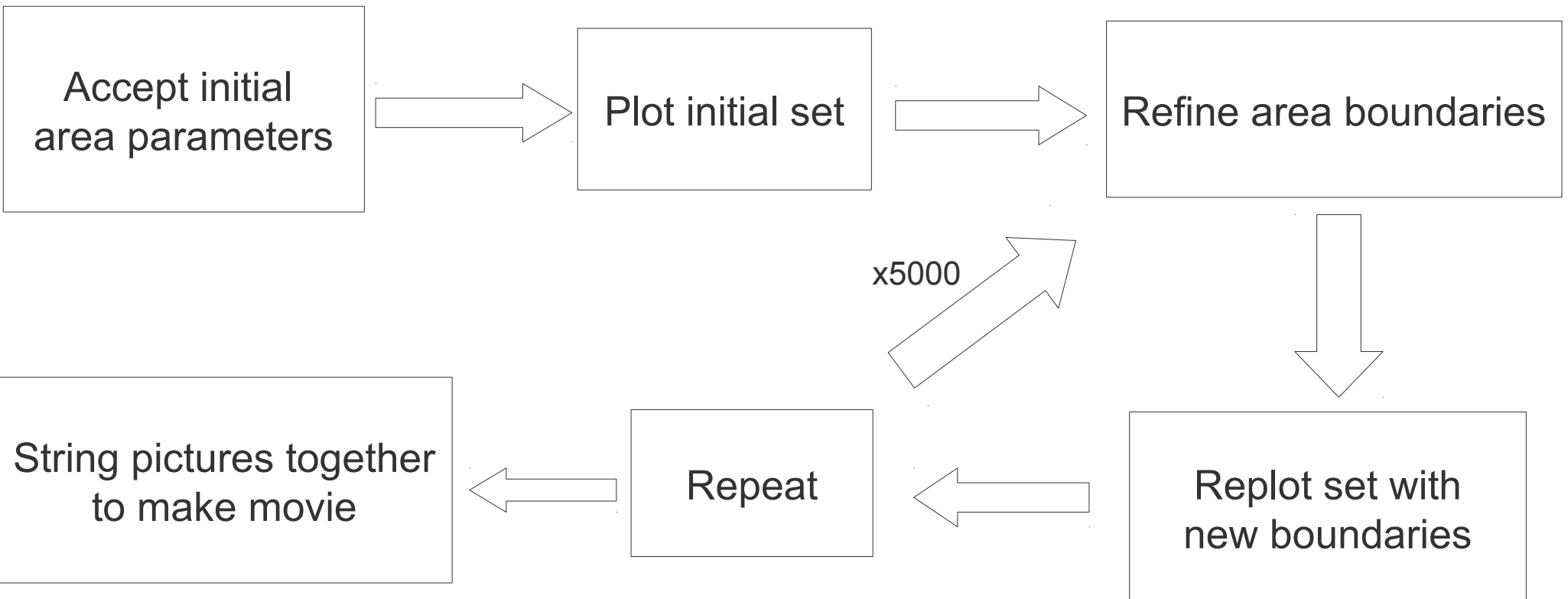
- Two parts to this project:
 - Static plotting of the set (first)
 - Dynamic zooming (second)



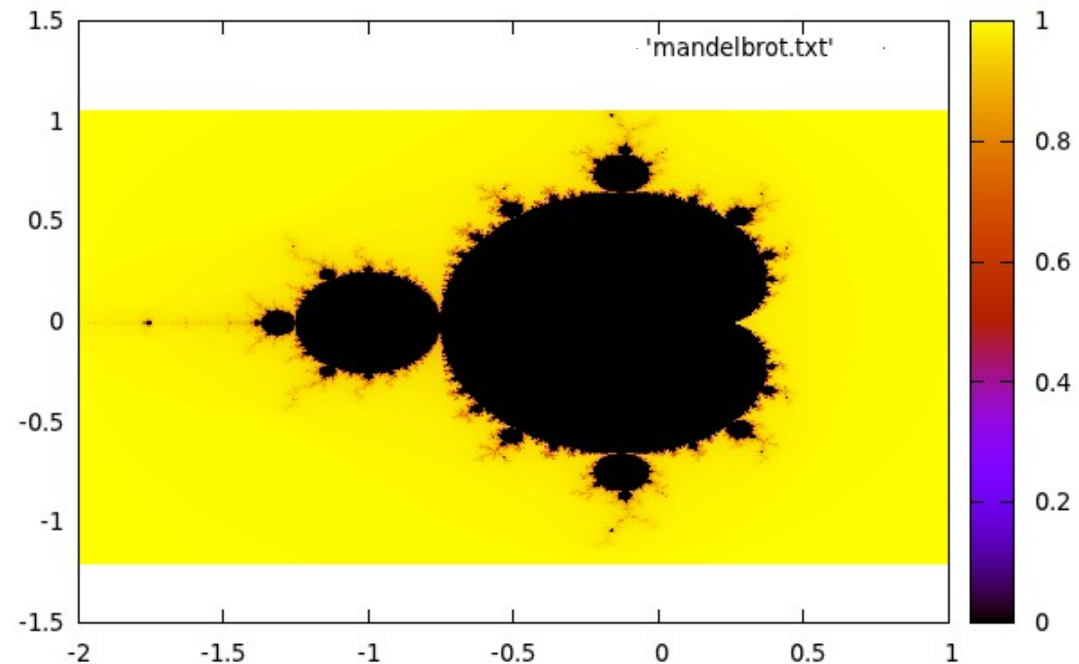
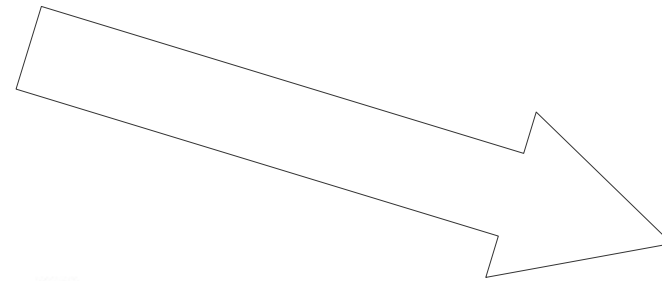
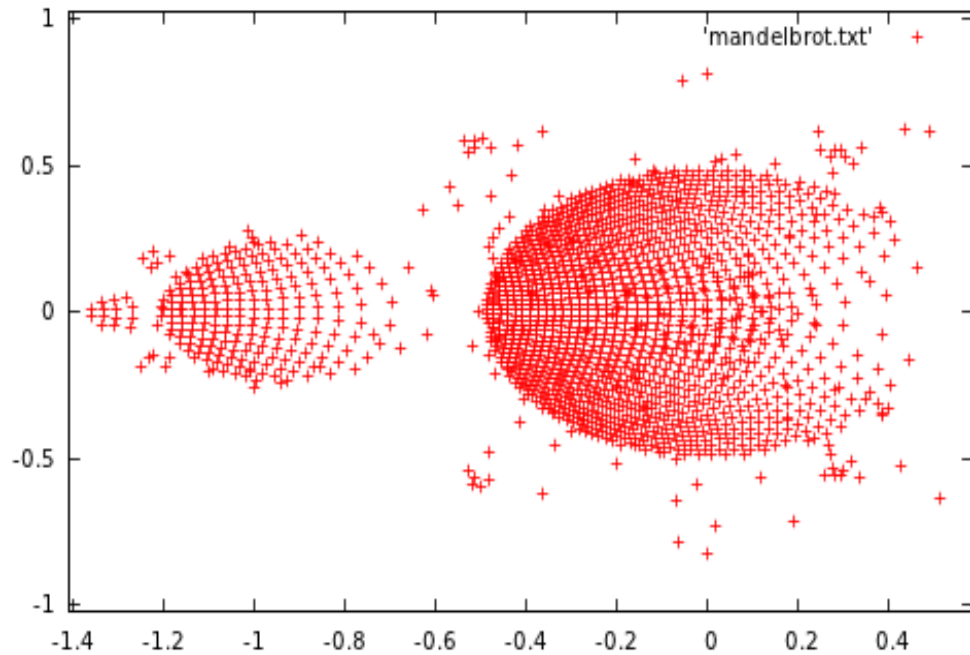
Part 1: Static Plotting Structure



Part 2: Dynamic Zooming Structure



Results: Part 1



Results: Part 2

Watch the movie!!!!

Acknowledgments

Special thanks to Kevin Croker!

Code can be found at <http://www2.hawaii.edu/~neillwar/>